

# Introduction to Optimization: Benchmarking

September 20, 2017

TC2 - Optimisation

Université Paris-Saclay, Orsay, France



Dimo Brockhoff  
Inria Saclay – Ile-de-France

# Course Overview

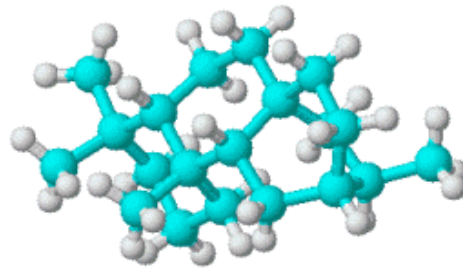
1	Mon, 18.9.2017 Tue, 19.9.2017	first lecture groups defined via wiki everybody went (actively!) through the Getting Started part of <a href="https://github.com/numbbo/coco">github.com/numbbo/coco</a>
2	Wed, 20.9.2017	today's lecture: "Benchmarking", final adjustments of groups everybody can run and postprocess the example experiment (~1h for final questions/help during the lecture)
3	Fri, 22.9.2017	lecture "Introduction to Continuous Optimization"
4	Fri, 29.9.2017	lecture "Gradient-Based Algorithms"
5	Fri, 6.10.2017	lecture "Stochastic Algorithms and DFO"
6	Fri, 13.10.2017	lecture "Discrete Optimization I: graphs, greedy algos, dyn. progr." deadline for submitting data sets
	Wed, 18.10.2017	deadline for paper submission
7	Fri, 20.10.2017	final lecture "Discrete Optimization II: dyn. progr., B&B, heuristics"
	Thu, 26.10.2017 / Fri, 27.10.2017	oral presentations (individual time slots)
	after 30.10.2017	vacation aka learning for the exams
	Fri, 10.11.2017	written exam

All deadlines:  
23:59pm Paris time

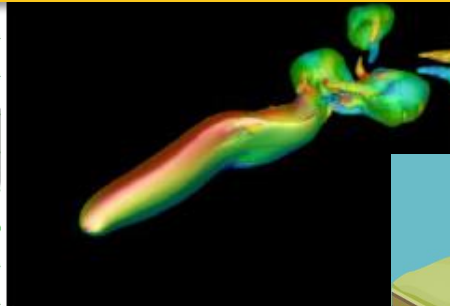
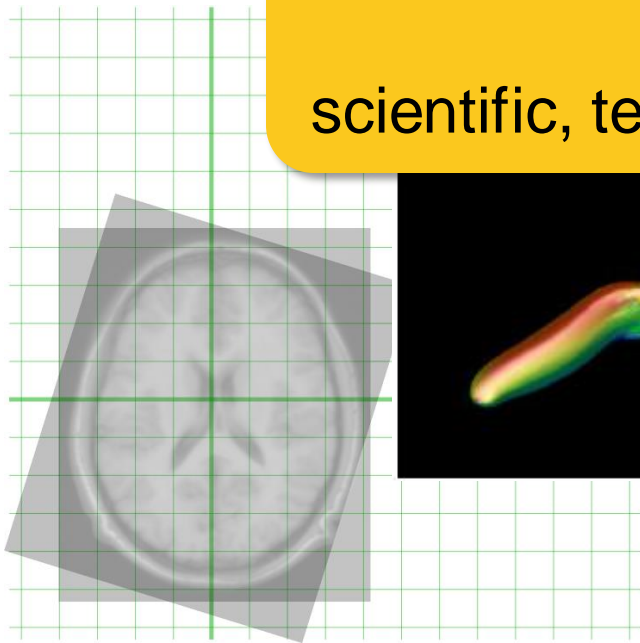
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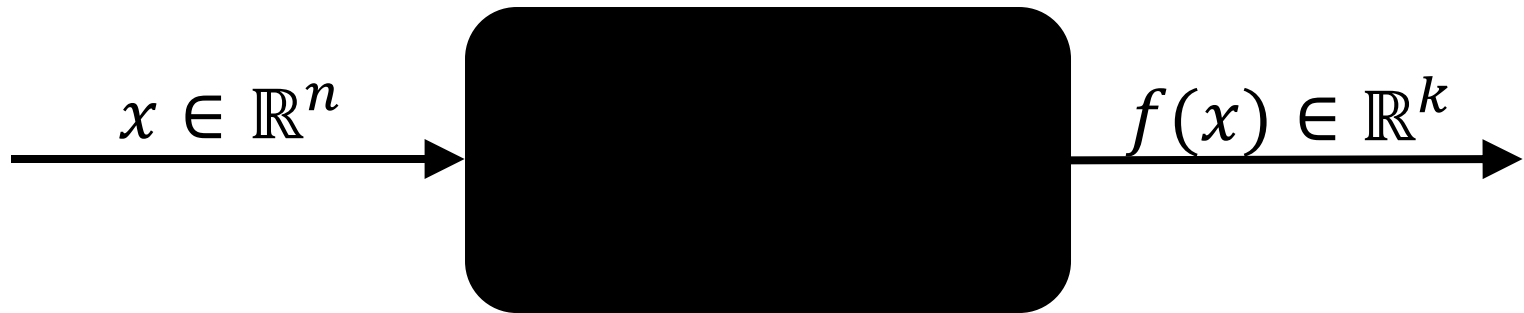


challenging optimization problems  
appear in many  
scientific, technological and industrial domains



# Numerical Blackbox Optimization

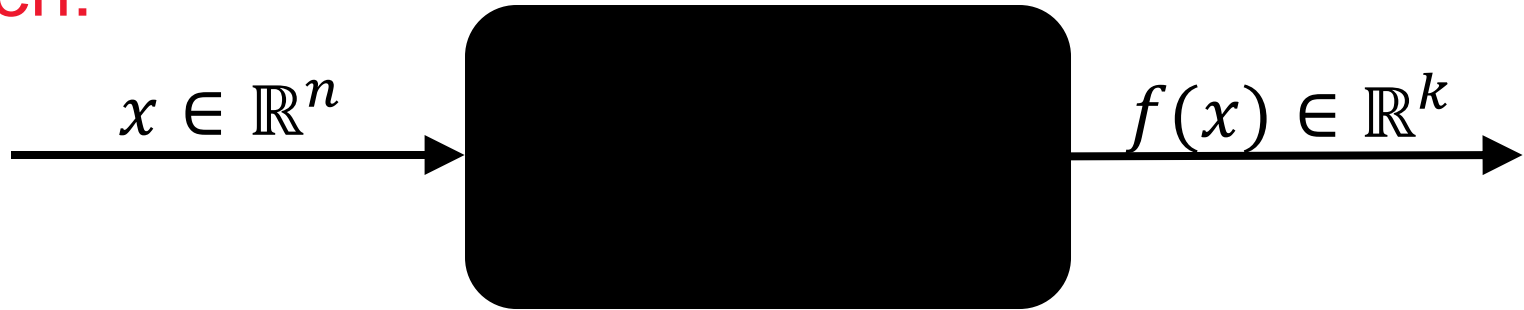
Optimize  $f: \Omega \subset \mathbb{R}^n \mapsto \mathbb{R}^k$



*derivatives not available or not useful*

# Practical Blackbox Optimization

Given:



Not clear:

which of the many algorithms should I use on my problem?

# Numerical Blackbox Optimizers

## Deterministic algorithms

- Quasi-Newton with estimation of gradient (**BFGS**) [Broyden et al. 1970]
- Simplex downhill [Nelder & Mead 1965]
- Pattern search [Hooke and Jeeves 1961]
- Trust-region methods (NEWUOA, BOBYQA) [Powell 2006, 2009]

## Stochastic (randomized) search methods

Evolutionary Algorithms (continuous domain)

- Differential Evolution [Storn & Price 1997]
- Particle Swarm Optimization [Kennedy & Eberhart 1995]
- **Evolution Strategies, CMA-ES**  
[Rechenberg 1965, Hansen & Ostermeier 2001]
- Estimation of Distribution Algorithms (EDAs)  
[Larrañaga, Lozano, 2002]
- Cross Entropy Method (same as EDA) [Rubinstein, Kroese, 2004]
- Genetic Algorithms [Holland 1975, Goldberg 1989]

Simulated annealing [Kirkpatrick et al. 1983]

Simultaneous perturbation stochastic approx. (SPSA) [Spall 2000]

# Numerical Blackbox Optimizers

## Deterministic algorithms

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Pattern search [Hooke and Jeeves 1961]

Trust-region methods (NEWUOA, BOBYQA) [Powell 2006, 2009]

choice typically not immediately clear although practitioners have knowledge about which difficulties their problem has (e.g. multi-modality, non-separability, ...)

- Evolution Strategies, CMA-ES

[Rechenberg 1965, Hansen & Ostermeier 2001]

- Estimation of Distribution Algorithms (EDAs)

[Larrañaga, Lozano, 2002]

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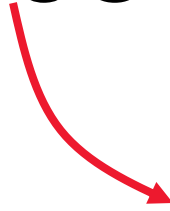
# Need: Benchmarking

- understanding of algorithms
- algorithm selection
- putting algorithms to a standardized test
  - simplify judgement
  - simplify comparison
  - regression test under algorithm changes

Kind of everybody has to do it (and it is tedious):

- choosing (and implementing) problems, performance measures, visualization, stat. tests, ...
- running a set of algorithms

**that's where COCO comes into play**



**Comparing Continuous Optimizers Platform**

**`https://github.com/numbbo/coco`**

**automatized benchmarking**

**benchmarking is non-trivial**

[remember the tutorial of Antonio]

**hence, COCO implements a  
reasonable, well-founded, and  
well-documented  
pre-chosen methodology**

# **How to benchmark algorithms with COCO?**

# https://github.com/numbbo/coco

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Add topics

16,007 commits 11 branches 31 releases 15 contributors

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brockho committed on GitHub Merge pull request #1352 from numbbo/development Latest commit 4b1497a on 20 Apr

code-experiments	A little more verbose error message when suite regression test fails	a month ago
code-postprocessing	Hashes are back on the plots.	a month ago
code-preprocessing	Fixed preprocessing to work correctly with the extended biobjective s...	3 months ago
howtos	Update create-a-suite-howto.md	4 months ago
.clang-format	raising an error in bbob2009_logger.c when best_value is NULL. Plus s...	2 years ago
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AUTHORS	small correction in AUTHORS	a year ago
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Use Git or checkout with SVN using the web URL.

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README.md

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<https://github.com/numbbo/coco.git>

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# https://github.com/numbbo/coco

The screenshot shows a web browser displaying the GitHub repository page for `numbbo/coco`. The browser's address bar shows the URL `https://github.com/numbbo/coco`. The repository page includes a navigation bar with options like "Branch: master", "New pull request", "Create new file", "Upload files", "Find file", and "Clone or download". A dropdown menu is open under "Clone or download", showing "Clone with HTTPS" and "Use SSH". The "Clone with HTTPS" option is selected, and the URL `https://github.com/numbbo/coco.git` is displayed. Below the dropdown, there are two buttons: "Open in Desktop" and "Download ZIP". The "Download ZIP" button is highlighted with a red box. The main content area shows a list of files and folders, including `code-experiments`, `code-postprocessing`, `code-preprocessing`, `howtos`, `.clang-format`, `.hgignore`, `AUTHORS`, `LICENSE`, `README.md`, `do.py`, and `doxygen.ini`. The repository title is "numbbo/coco: Comparing Continuous Optimizers".

numbbo/coco: Numerical ... x +

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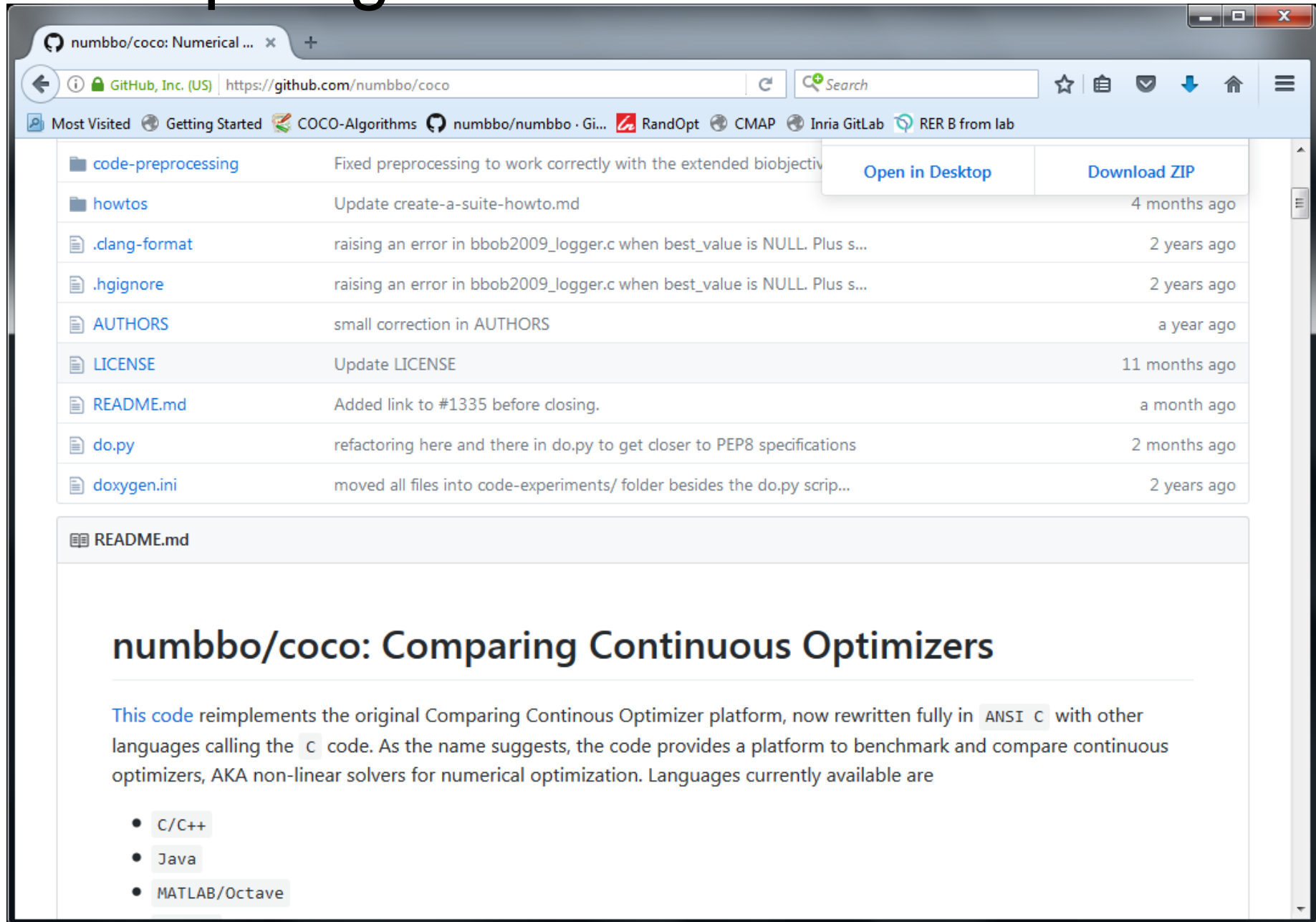
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README.md

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This code reimplements the original Comparing Continuous Optimizer platform, now rewritten fully in ANSI C with other languages calling the C code. As the name suggests, the code provides a platform to benchmark and compare continuous optimizers, AKA non-linear solvers for numerical optimization. Languages currently available are

- C/C++
- Java
- MATLAB/Octave

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The screenshot shows a web browser window with the URL `https://github.com/numbbo/coco`. The browser's address bar and tabs are visible at the top. Below the browser window, the GitHub repository page is shown. It features a list of recent commits on the left and the README content on the right.

File	Commit Message	Time Ago
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Contributions to link further languages (including a better example in C++) are more than welcome.

For more information,

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- read the [COCO experimental setup](#) description

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- see the [bbob-biobj](#) and [bbob-biobj-ext](#) [COCO multi-objective functions testbed](#) documentation and the [specificities of the performance assessment for the bi-objective testbeds](#).
- consult the [BBOB workshops series](#),
- consider to [register here](#) for news,
- see the [previous COCO home page here](#) and
- see the [links below](#) to learn more about the ideas behind CoCO.

# https://github.com/numbbo/coco

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## Getting Started

0. Check out the [Requirements](#) above.

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The record of official releases can be found [here](#). The latest release corresponds to the [master branch](#) as linked above.

2. In a system shell, `cd` into the `coco` or `coco-<version>` folder (framework root), where the file `do.py` can be found. Type, i.e. execute, one of the following commands once

```
python do.py run-c
python do.py run-java
python do.py run-matlab
python do.py run-octave
python do.py run-python
```

depending on which language shall be used to run the experiments. `run-*` will build the respective code and run the example experiment once. The build result and the example experiment code can be found under `code-experiments/build/<language>` (`<language>=matlab` for Octave). `python do.py` lists all available commands.

3. On the computer where experiment data shall be post-processed, run

```
python do.py install-postprocessing
```



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**installation I: experiments**



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example experiment once. The build result and the example experiment code can be found under `code-experiments/build/<language>` (`<language>=matlab` for Octave). `python do.py` lists all available commands.

3. On the computer where experiment data shall be stored, run the following command:

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```

**installation II: postprocessing**

to (user-locally) install the post-processing. From here on, `do.py` has done its job and is only needed again for updating the builds to a new release.

4. Copy the folder `code-experiments/build/YOUR-FAVORITE-LANGUAGE` and its content to another location. In Python it is sufficient to copy the file `example_experiment.py`. Run the example experiment (it already is compiled). As the details vary, see the respective read-me's and/or example experiment files:

- C [read me](#) and [example experiment](#)
- Java [read me](#) and [example experiment](#)
- Matlab/Octave [read me](#) and [example experiment](#)
- Python [read me](#) and [example experiment](#)

If the example experiment runs, connect your favorite algorithm to Coco: replace the call to the random search optimizer in the example experiment file by a call to your algorithm (see above). Update the output `result_folder`, the `algorithm_name` and `algorithm_info` of the observer options in the example experiment file.

Another entry point for your own experiments can be the `code-experiments/examples` folder.

5. Now you can run your favorite algorithm on the `bbob` suite (for single-objective algorithms) or on the `bbob-biobj` and `bbob-biobj-ext` suites (for multi-objective algorithms). Output is automatically generated in the specified data `result_folder`. By now, more suites might be available, see below.

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**coupling algo + COCO**

# Simplified Example Experiment in Python

```
import cocoex
import scipy.optimize

### input
suite_name = "bbob"
output_folder = "scipy-optimize-fmin"
fmin = scipy.optimize.fmin

### prepare
suite = cocoex.Suite(suite_name, "", "")
observer = cocoex.Observer(suite_name,
                           "result_folder: " + output_folder)

### go
for problem in suite: # this loop will take several minutes
    problem.observe_with(observer) # generates the data for
                                   # cocopp post-processing
    fmin(problem, problem.initial_solution)
```

**Note:** the actual `example_experiment.py` contains more advanced things like restarts, batch experiments, other algorithms (e.g. CMA-ES), etc.

# https://github.com/numbbo/coco

The image shows a browser window displaying the GitHub repository page for numbbo/coco. The browser's address bar shows the URL https://github.com/numbbo/coco/tree/development. The page content includes a list of instructions for running experiments. A red rounded rectangle highlights the text: "5. Now you can run your favorite algorithm on the bbob suite (for single-objective algorithms) or on the bbob-biobj and bbob-biobj-ext suites (for multi-objective algorithms). Output is automatically generated in the specified data result\_folder . By now, more suites might be available, see below." Below this, another red rounded rectangle highlights the text: "6. Postprocess the data from the results folder by typing" followed by a code block: 

```
python -m cocopp [-o OUTPUT_FOLDERNAME] YOURDATA
```

. A third red rounded rectangle highlights the text: "tip: start with small #funevals (until bugs fixed 😊) then increase budget to get a feeling how long a 'long run' will take".

numbbo/coco at develop... x +

GitHub, Inc. (US) | https://github.com/numbbo/coco/tree/development

Most Visited Getting Started COCO-Algorithms numbbo/numbbo · Gi... RandOpt CMAP Inria GitLab RER B from lab

Another entry point for your own experiments can be the `code-experiments/examples` folder.

5. Now you can run your favorite algorithm on the `bbob` suite (for single-objective algorithms) or on the `bbob-biobj` and `bbob-biobj-ext` suites (for multi-objective algorithms). Output is automatically generated in the specified data `result_folder` . By now, more suites might be available, see below.

6. Postprocess the data from the results folder by typing

```
python -m cocopp [-o OUTPUT_FOLDERNAME] YOURDATA
```

Any subfolder in the folder arguments will be searched for... in different folders collected under a single "root" `YOURDATAFOLDER` folder. We can also compare more than one algorithm by specifying several data result folders generated by different algorithms.

A folder, p... file, usefu... the outpu...

A summa... template... template...

7. Once... indepe...

8. The experiments can be parallelized with any re-distribution of single problem instances to batches (see `example_experiment.py` for an example). Each batch must write in a different target folder (this should happen automatically). Results of each batch must be kept under their separate folder as is. These folders then must be

**running the experiment**

**tip:**  
**start with small #funevals (until bugs fixed 😊)**  
**then increase budget to get a feeling**  
**how long a "long run" will take**

# https://github.com/numbbo/coco

The image shows a browser window displaying the GitHub repository page for numbbo/coco. The browser's address bar shows the URL https://github.com/numbbo/coco/tree/development. The page content includes instructions for running algorithms and postprocessing data. A red box highlights a terminal command: `python -m cocopp [-o OUTPUT_FOLDERNAME] YOURDATAFOLDER [MORE_DATAFOLDERS]`. A red callout box with the text "postprocessing" is overlaid on the page. Another red callout box at the bottom contains the text "tip to reduce time: use parameter --omit-single (will become the default in v2.2)".

numbbo/coco at develop... x +

GitHub, Inc. (US) | https://github.com/numbbo/coco/tree/development

Most Visited Getting Started COCO-Algorithms numbbo/numbbo · Gi... RandOpt CMAP Inria GitLab RER B from lab

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6. Postprocess the data from the results folder by typing

```
python -m cocopp [-o OUTPUT_FOLDERNAME] YOURDATAFOLDER [MORE_DATAFOLDERS]
```

Any subfolder in the folder arguments will be searched for logged data. That is, experiments from different batches can be in different folders collected under a single "root" `YOURDATAFOLDER` specifying several data result folders generated by different algorithms.

A folder, `ppdata` by default, will be generated, which contains a `ppdata` file, useful as main entry point to explore the result with a browser.

the output folder name with the `-o OUTPUT_FOLDERNAME` option.

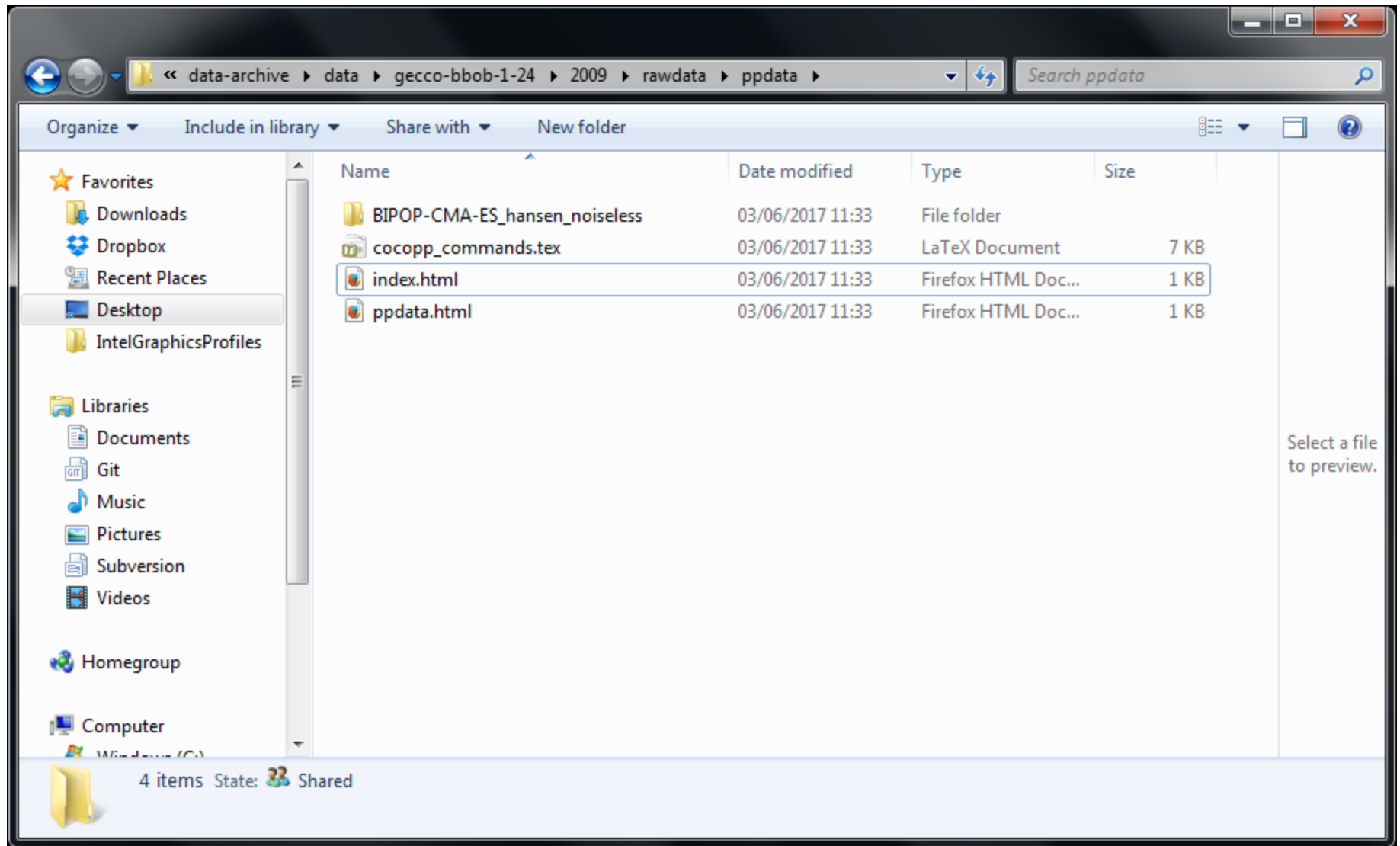
A summary pdf can be produced via LaTeX. The corresponding templates can be found in the `code-postprocessing/latex-templates` folder.

7. Omitting single results

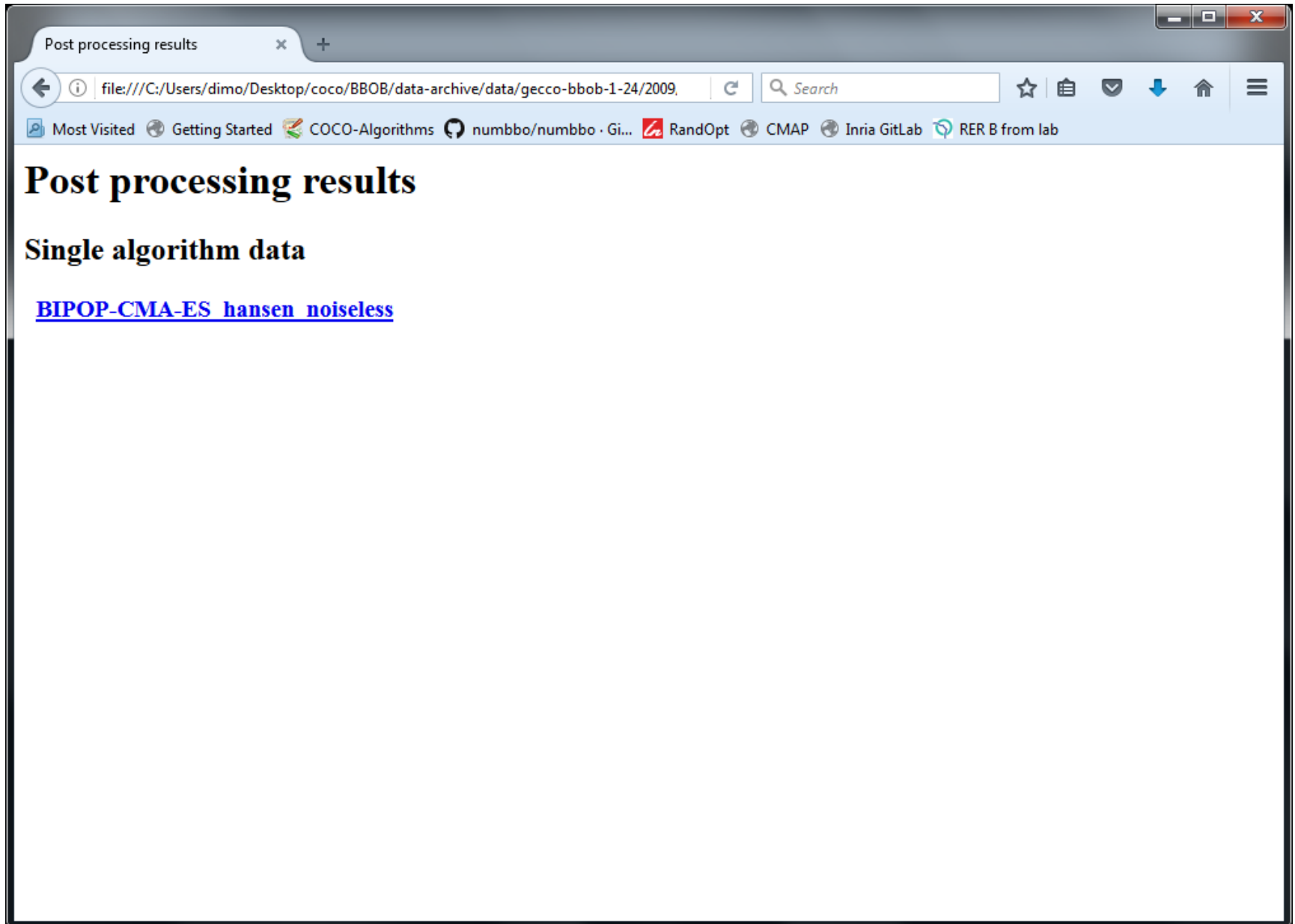
8. Tip to reduce time: use parameter `--omit-single` (will become the default in v2.2)

`example_experiment.py` for an example). Each batch must write in a different target folder (this should happen automatically). Results of each batch must be kept under their separate folder as is. These folders then must be

# Result Folder



# Automatically Generated Results



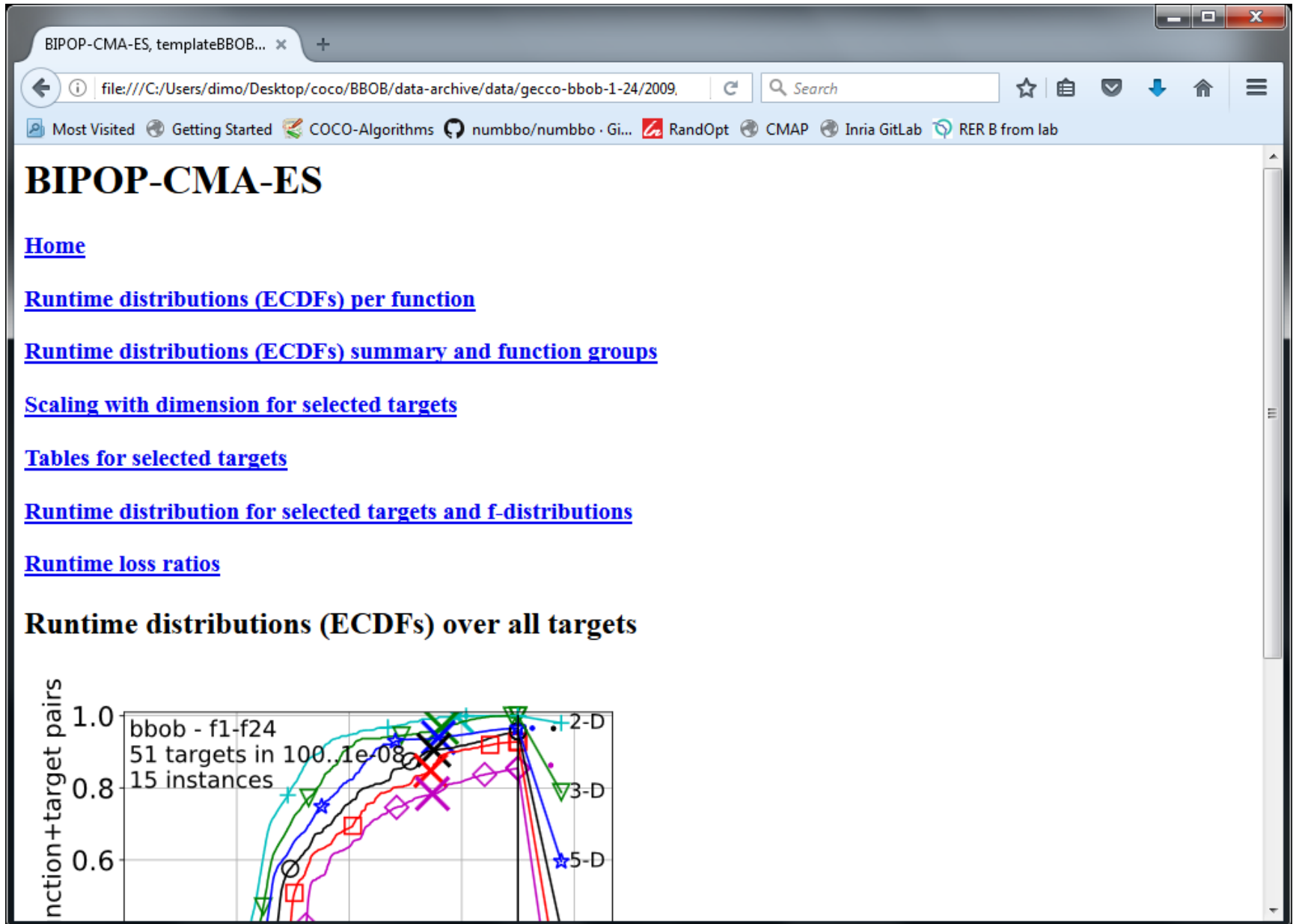
The image shows a web browser window with a single tab titled "Post processing results". The address bar contains the file path: `file:///C:/Users/dimo/Desktop/coco/BBOB/data-archive/data/gecco-bbob-1-24/2009`. The browser's toolbar includes a search bar and several navigation icons. Below the toolbar, a row of bookmarks is visible, including "Most Visited", "Getting Started", "COCO-Algorithms", "numbbo/numbbo · Gi...", "RandOpt", "CMAP", "Inria GitLab", and "RER B from lab". The main content area of the browser displays the following text:

## Post processing results

### Single algorithm data

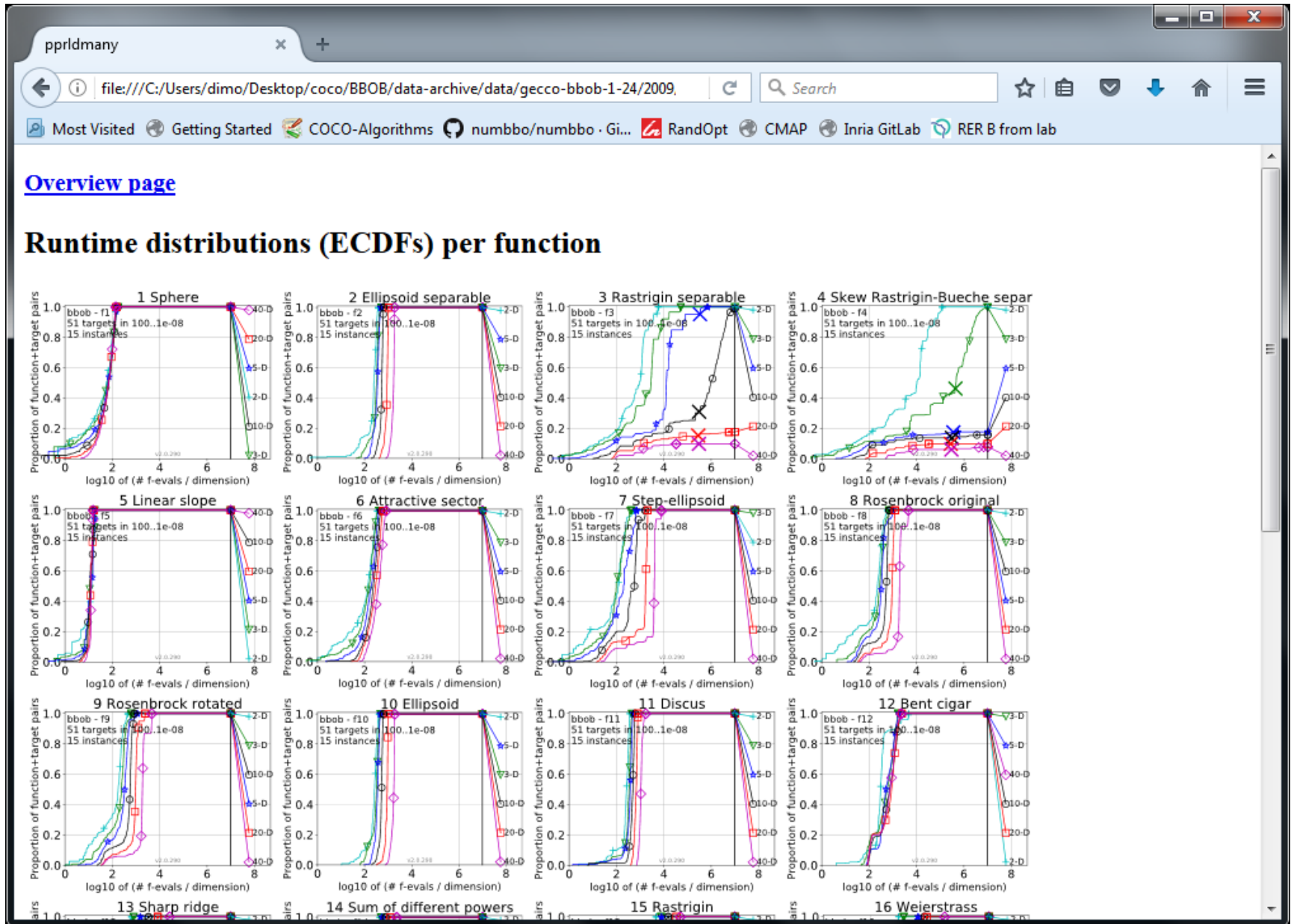
[BIPOP-CMA-ES hansen noiseless](#)

# Automatically Generated Results

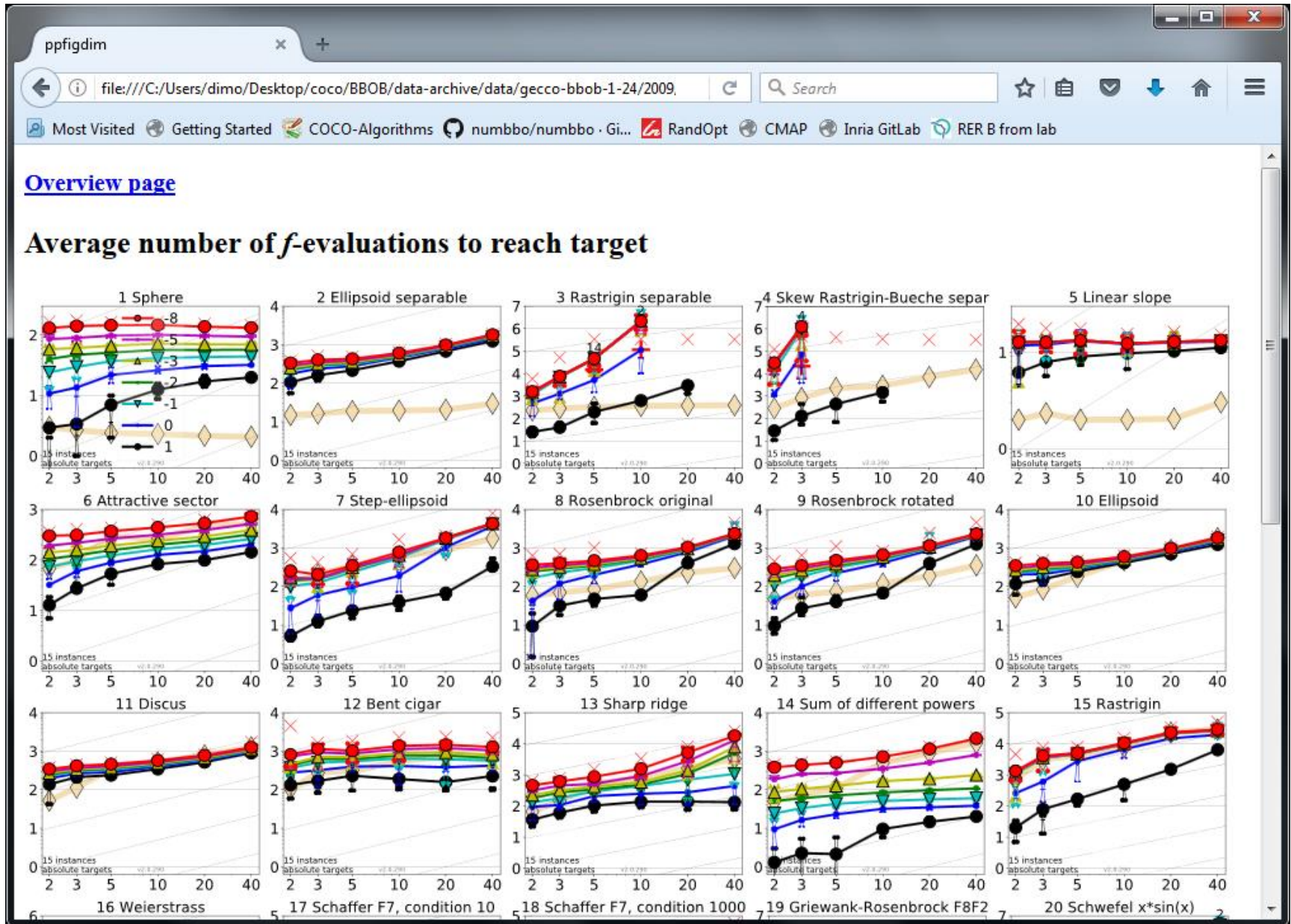




# Automatically Generated Results



# Automatically Generated Results



## **so far:**

data for about 170 algorithm variants  
(some of which on noisy or multiobjective test functions)  
132 workshop papers  
by 101 authors from 28 countries

# Measuring Performance

On

- **real world problems**
  - expensive
  - comparison typically limited to certain domains
  - experts have limited interest to publish
- **"artificial" benchmark functions**
  - cheap
  - controlled
  - data acquisition is comparatively easy
  - **problem of representativeness**

# Test Functions

- define the "scientific question"

the relevance can hardly be overestimated

- should represent "reality"

- are often too simple?

remind separability

- a number of testbeds are around

- account for **invariance properties**

prediction of performance is based on "similarity",  
ideally equivalence classes of functions

# Available Test Suites in COCO

bbob	24 noiseless fcts	140+ algo data sets
bbob-noisy	30 noisy fcts	40+ algo data sets
bbob-biobj	55 bi-objective fcts	16 algo data sets

# How Do We Measure Performance?

## Meaningful quantitative measure

- **quantitative** on the ratio scale (highest possible)  
"algo A is two *times* better than algo B" is a meaningful statement
- assume a wide range of values
- **meaningful (interpretable)** with regard to the real world  
possible to transfer from benchmarking to real world

**runtime** or **first hitting time** is the prime candidate  
(we don't have many choices anyway)



# How Do We Measure Performance?

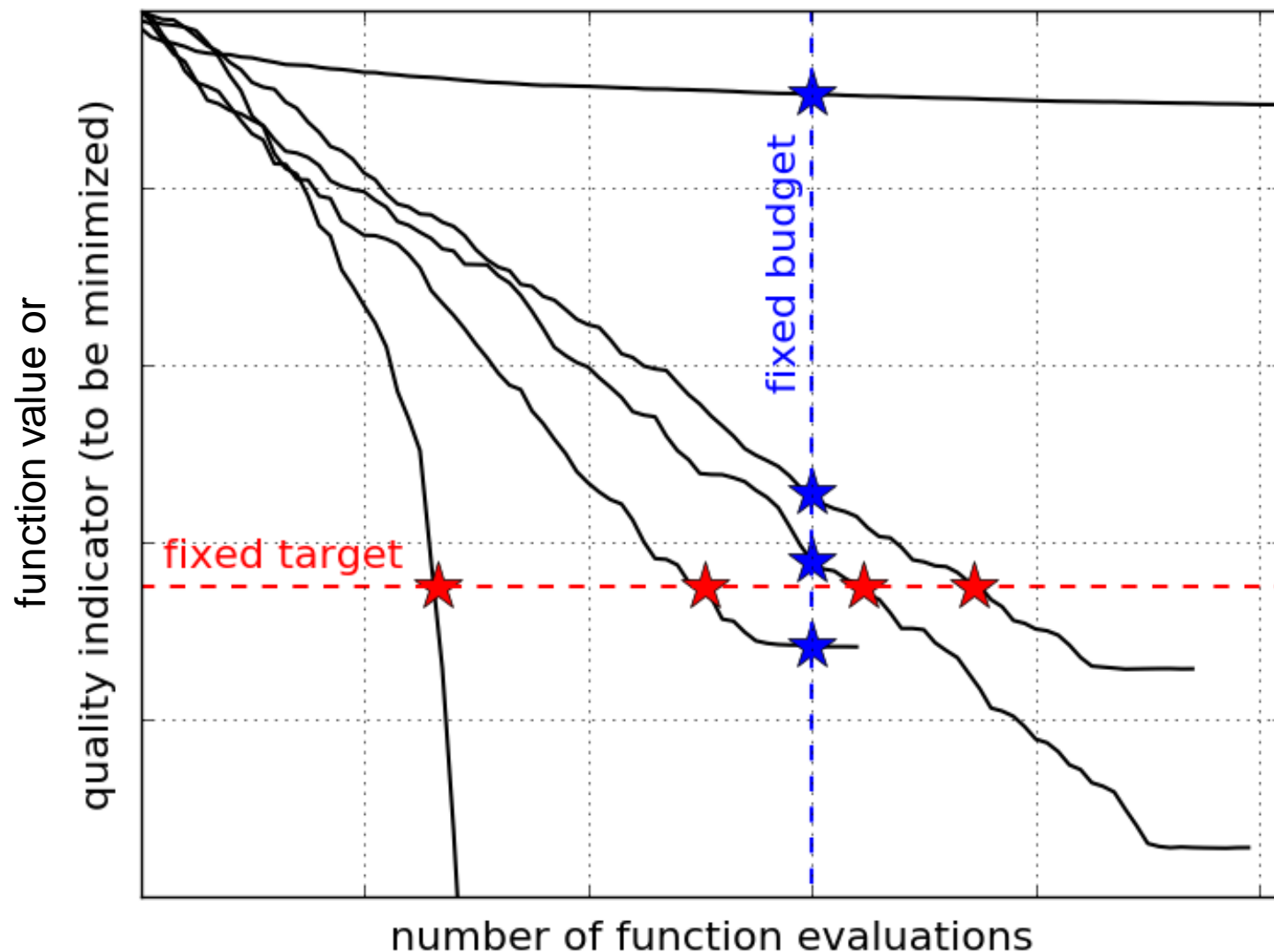
## Two objectives:

- Find solution with small(est possible) **function/indicator value**
- With the least possible **search costs** (number of function evaluations)

For measuring performance: fix one and measure the other

# Measuring Performance Empirically

convergence graphs is all we have to start with...

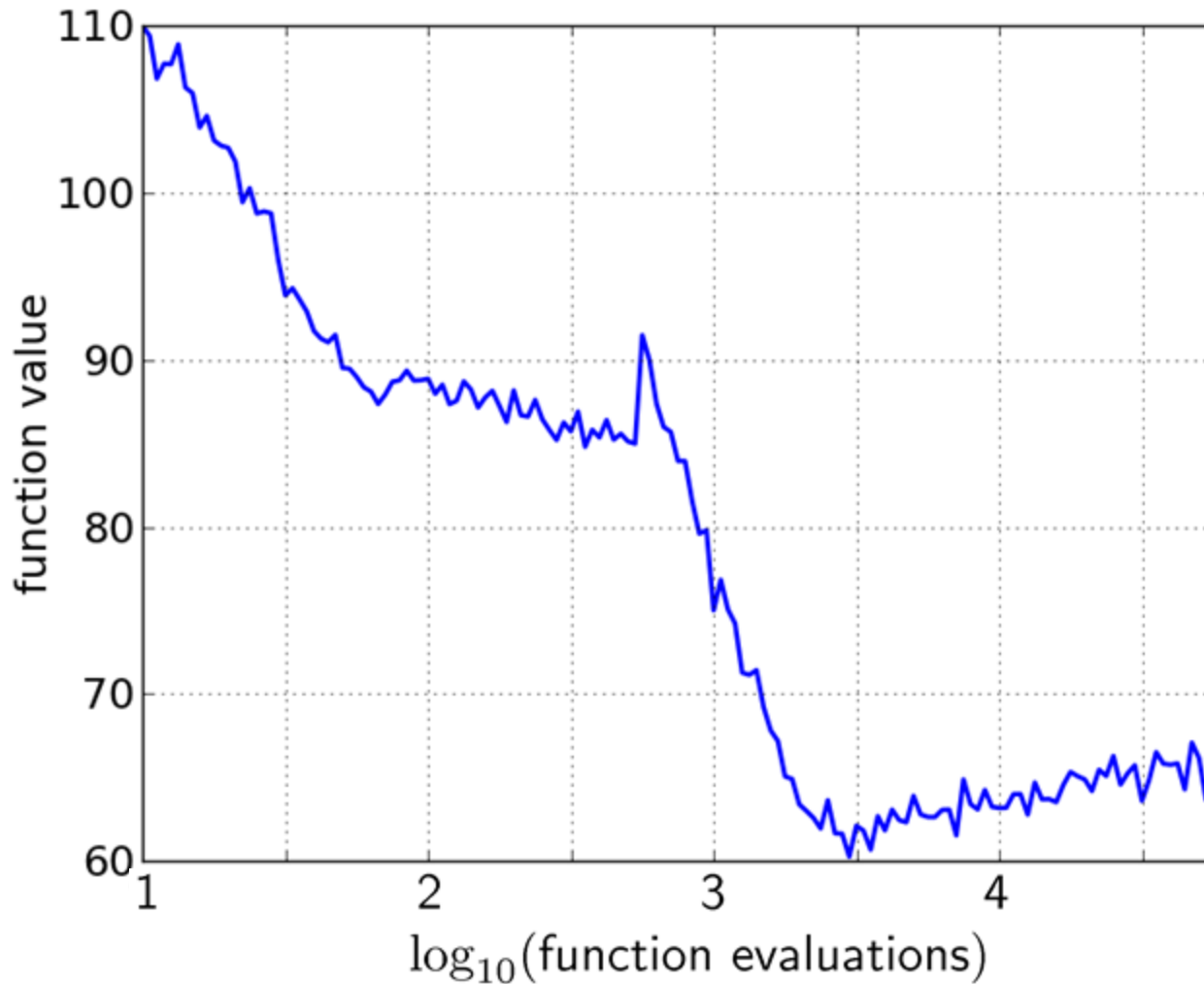


## **ECDF:**

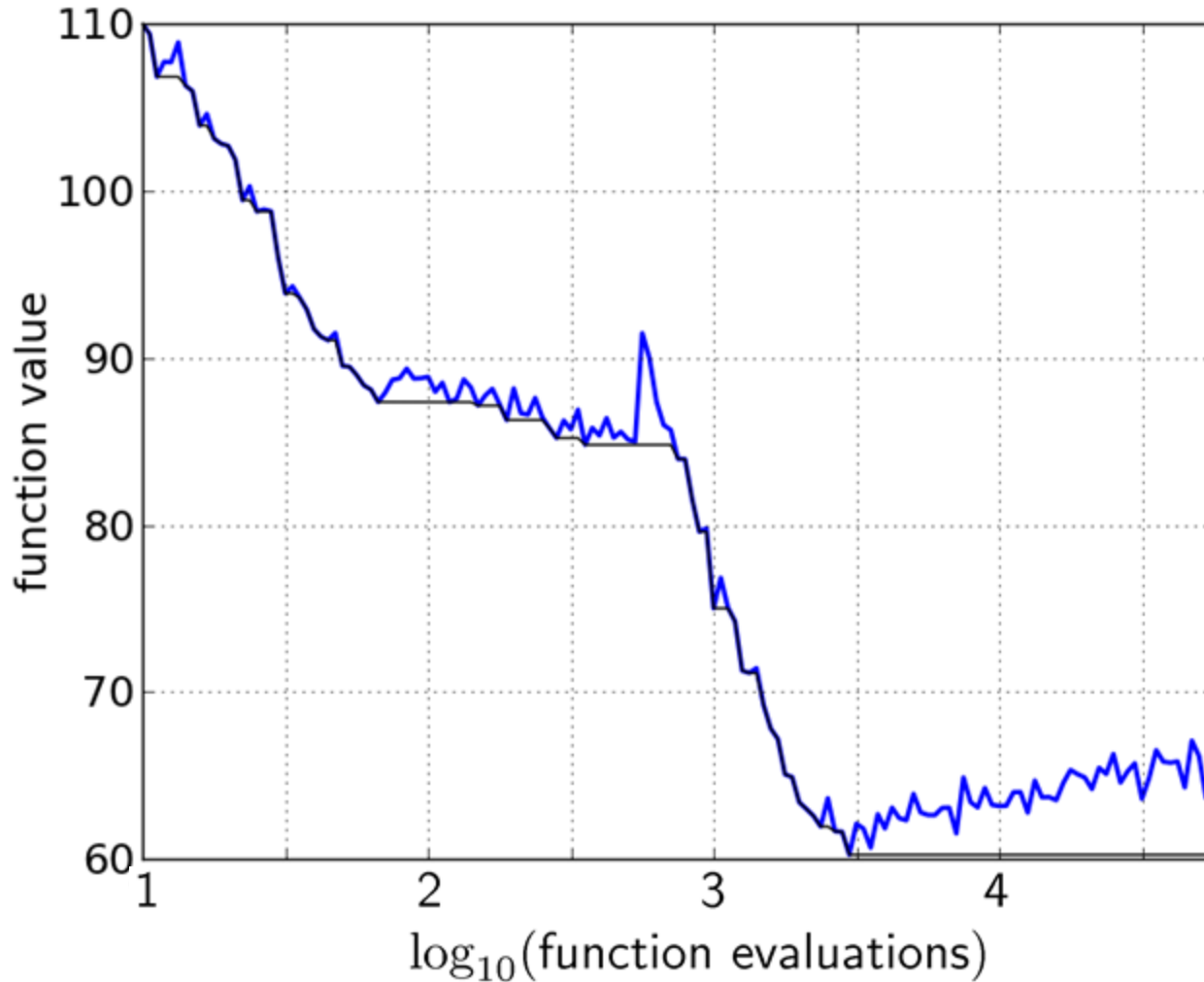
Empirical Cumulative Distribution Function of the  
Runtime

[aka data profile]

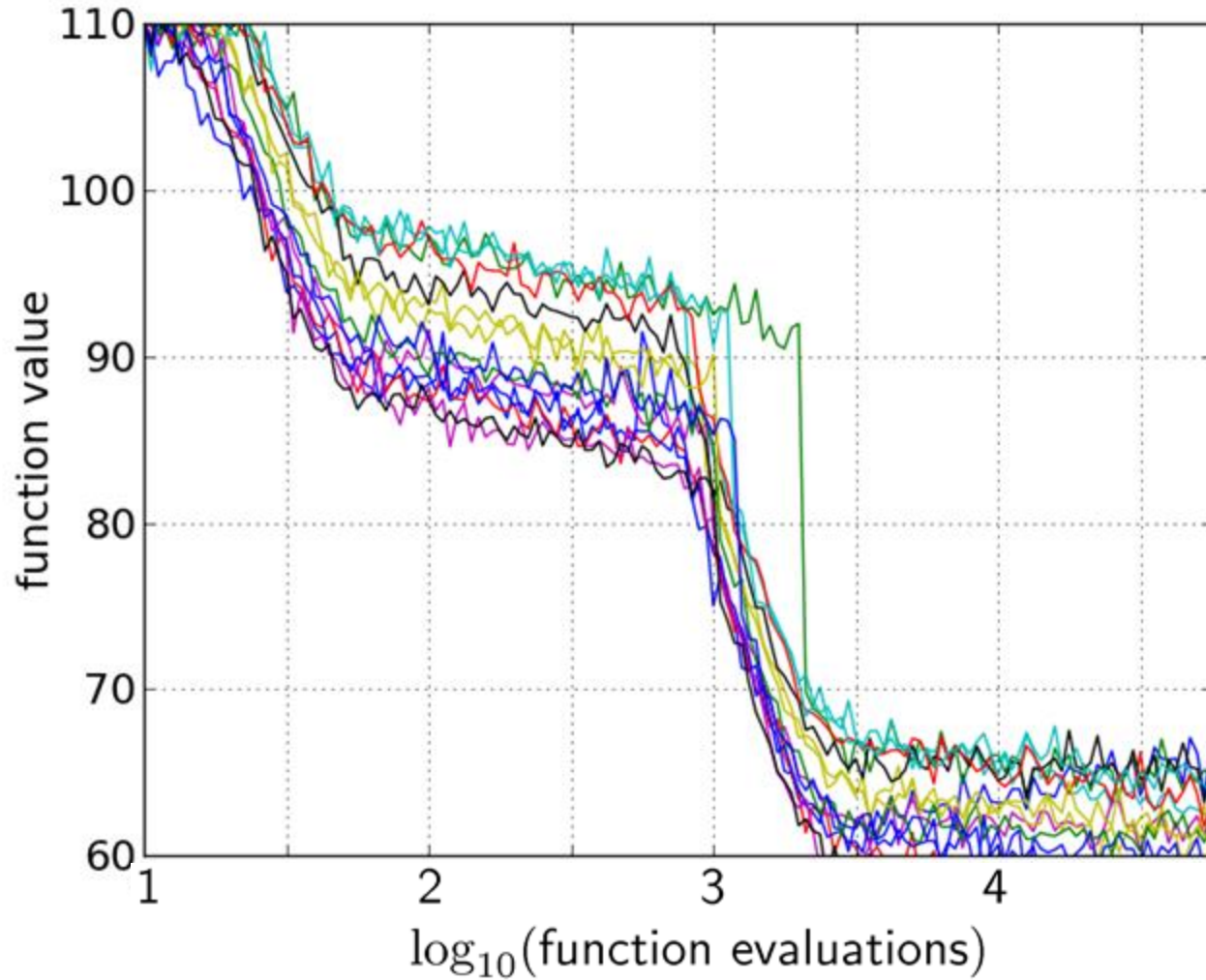
# A Convergence Graph



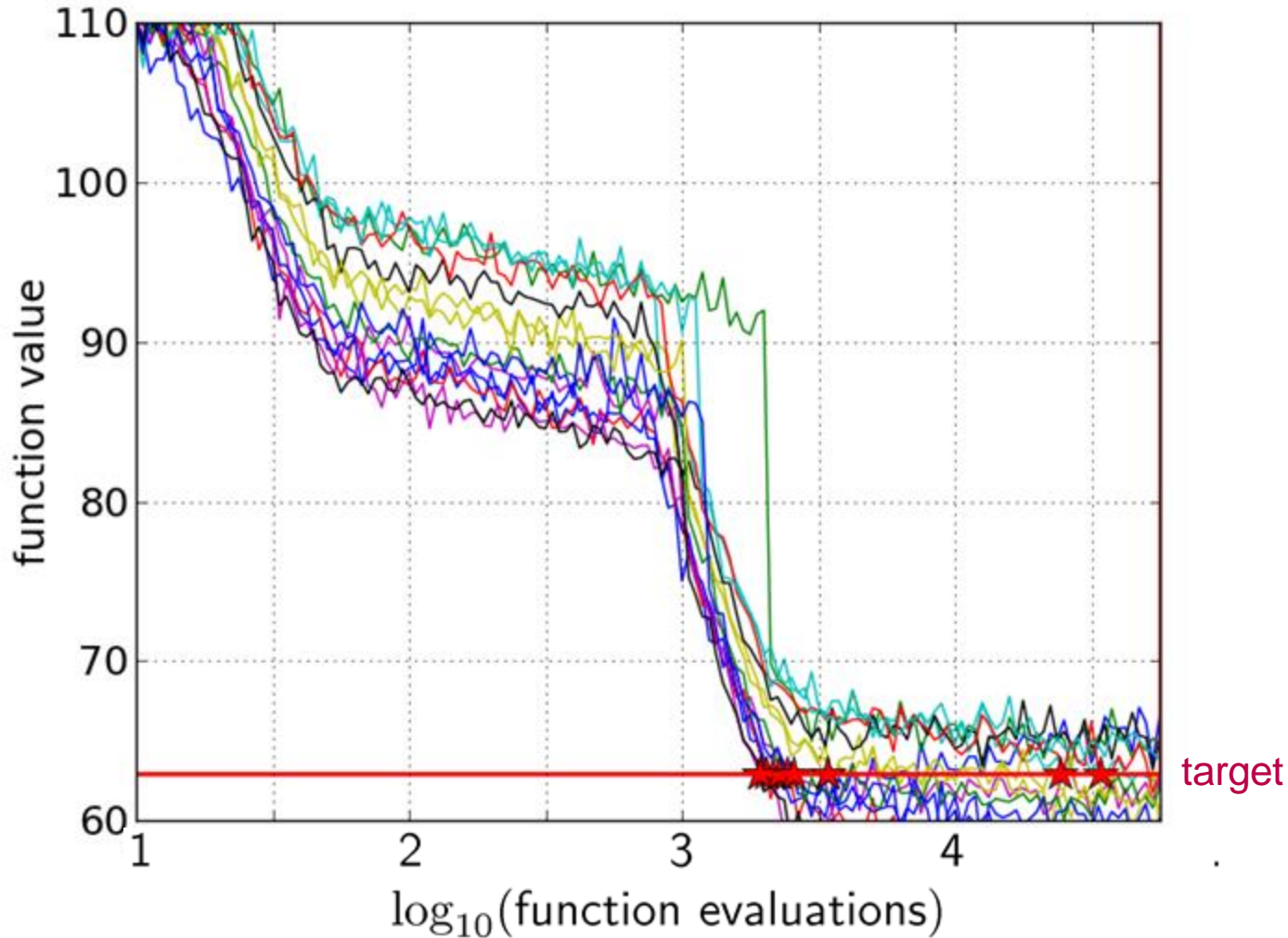
# First Hitting Time is Monotonous



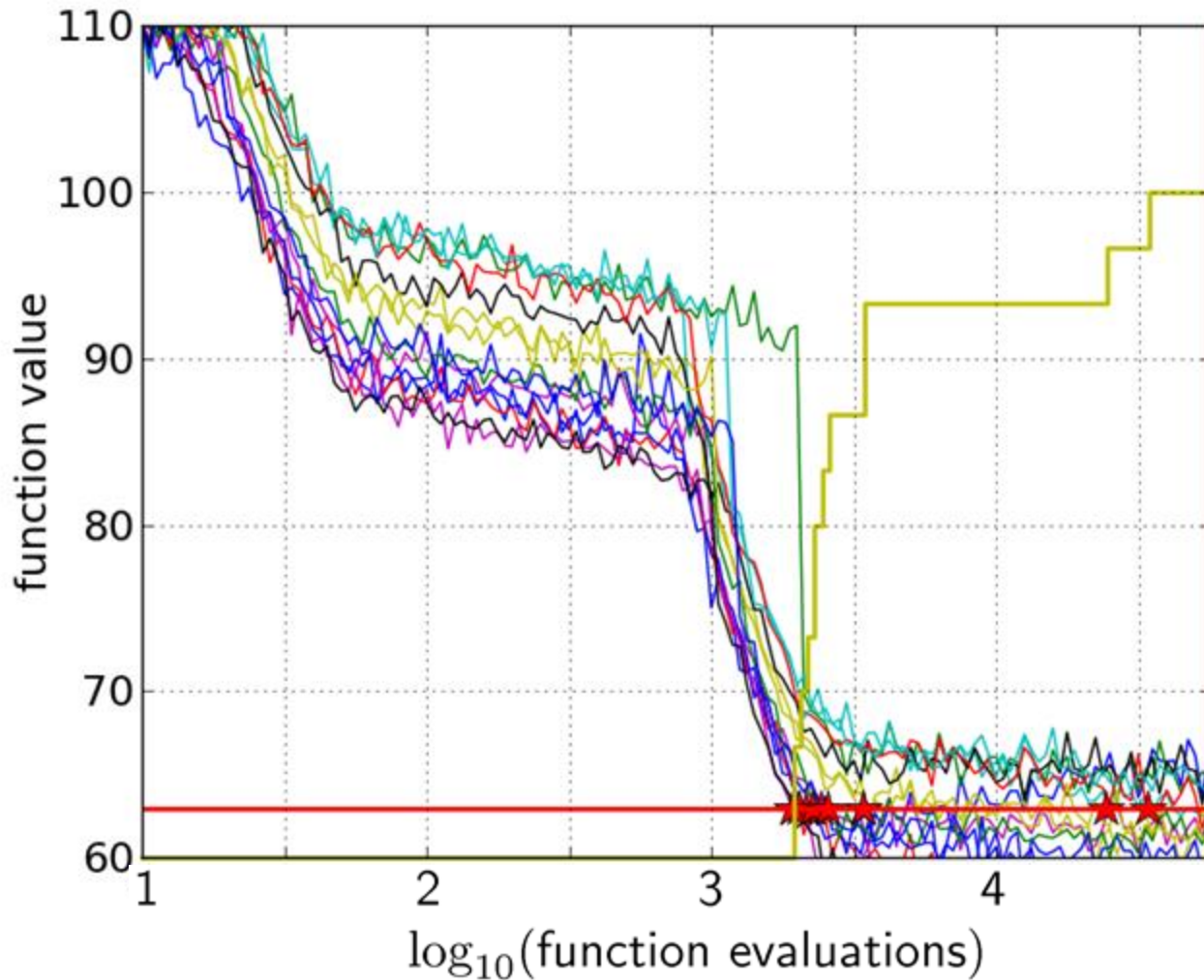
# 15 Runs



# 15 Runs $\leq$ 15 Runtime Data Points



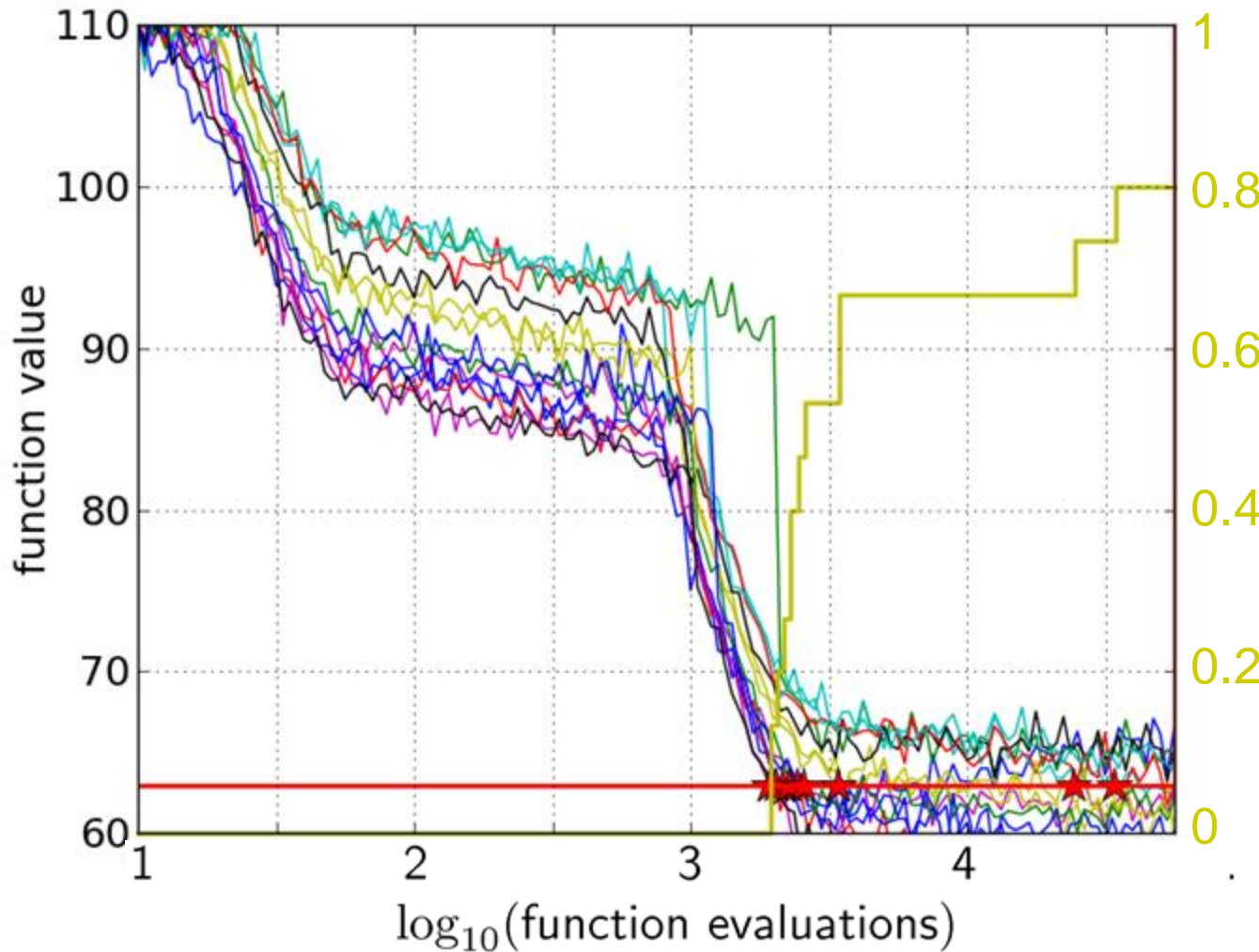
# Empirical Cumulative Distribution



- 1 the **ECDF** of run lengths to reach the target
  - has for each data point a **vertical step of constant size**
  - displays for each x-value (budget) the count of observations to the left (first hitting times)



# Empirical Cumulative Distribution



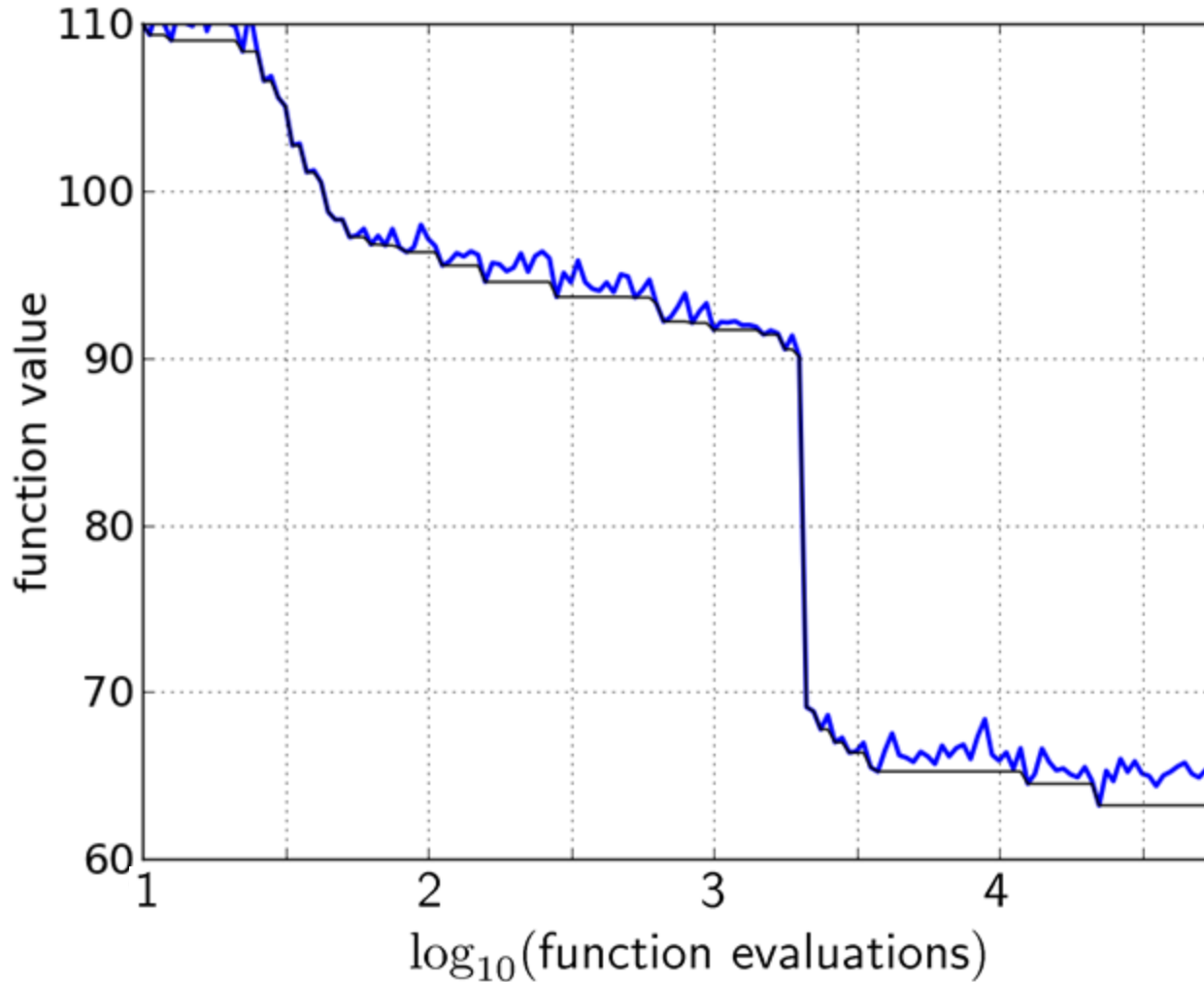
1 interpretations possible:

0.8. 80% of the runs reached the target

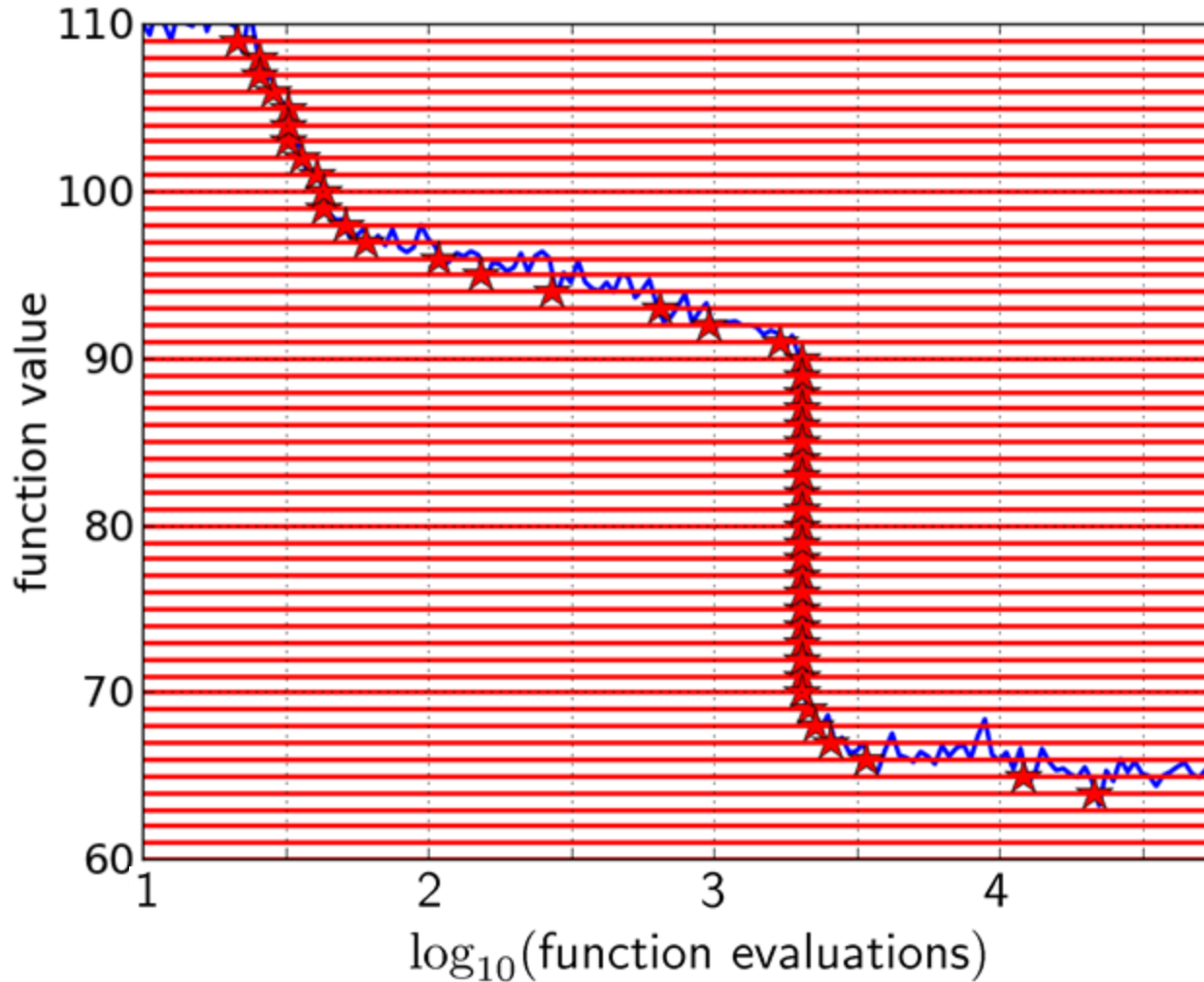
0.6  
• e.g. 60% of the runs need between 2000 and 4000 evaluations

0

# Reconstructing A Single Run

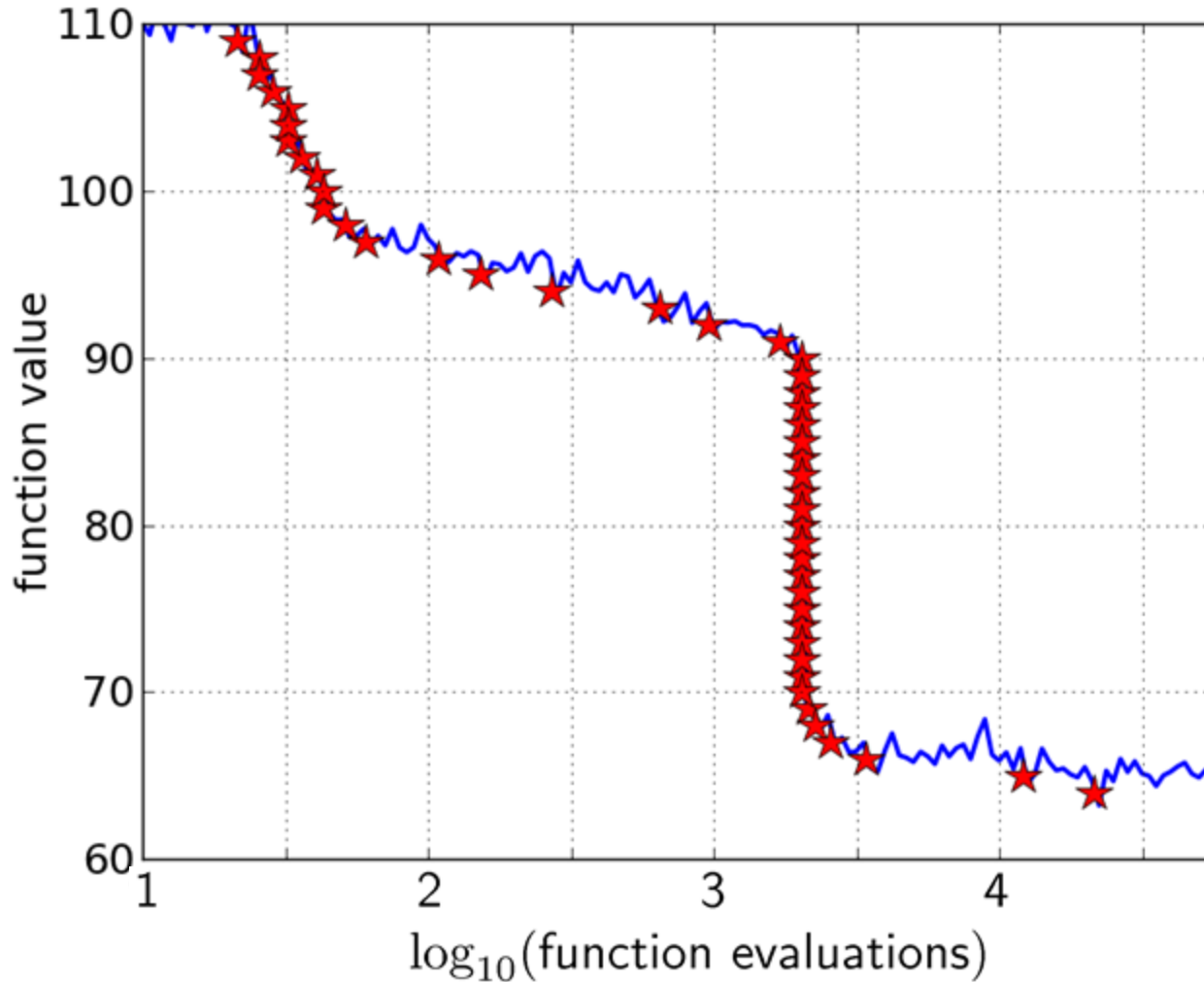


# Reconstructing A Single Run

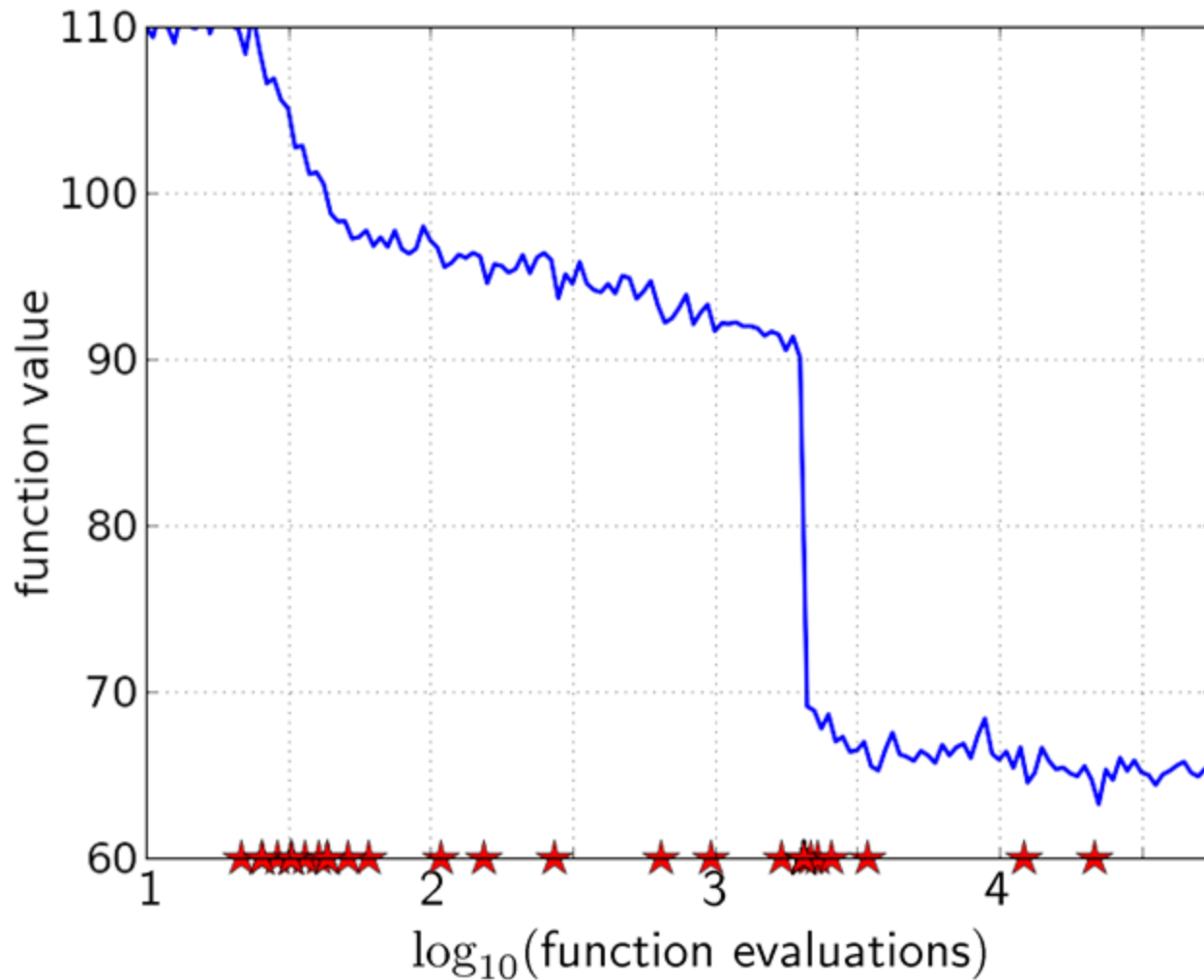


50 equally spaced targets

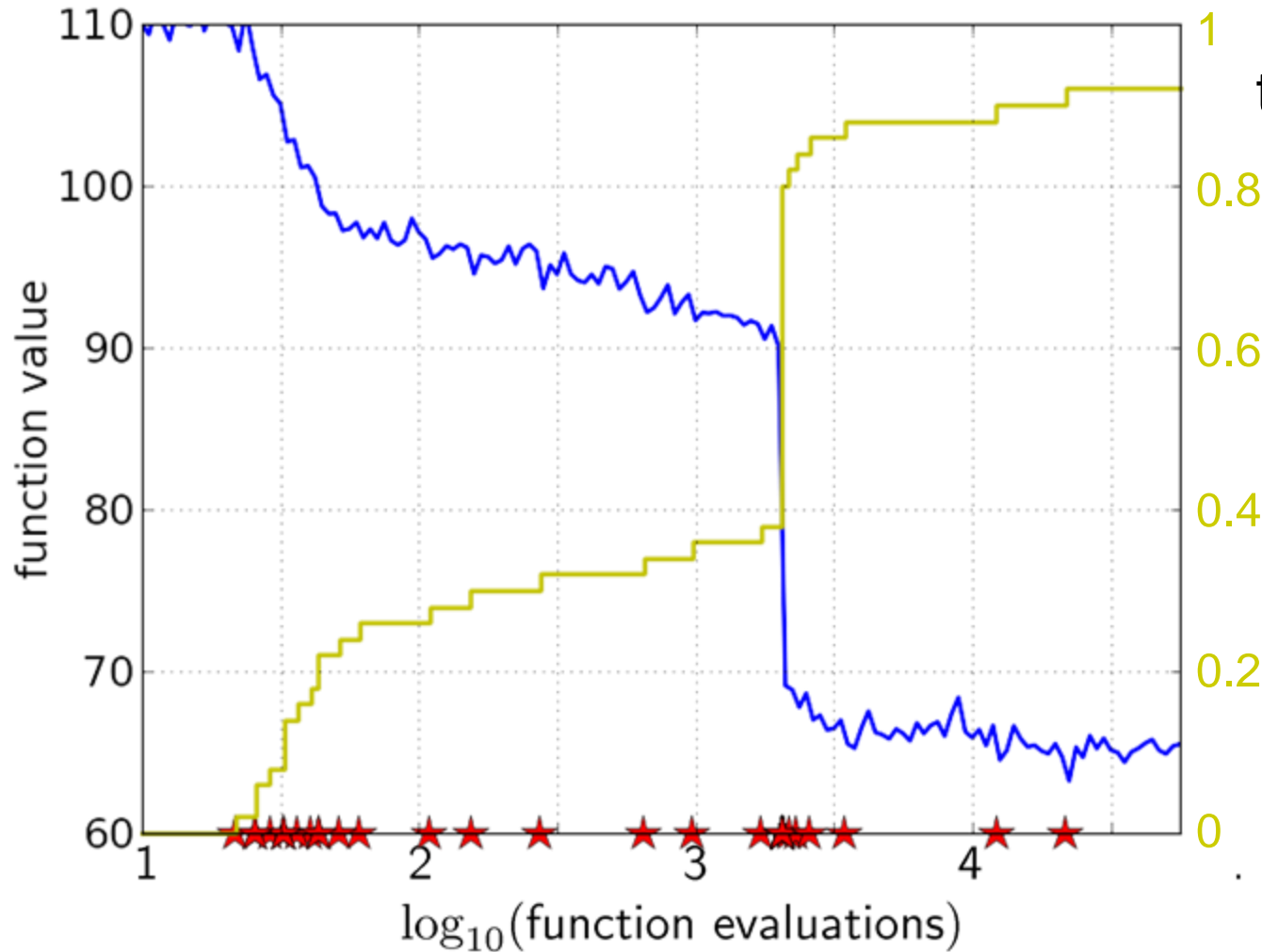
# Reconstructing A Single Run



# Reconstructing A Single Run

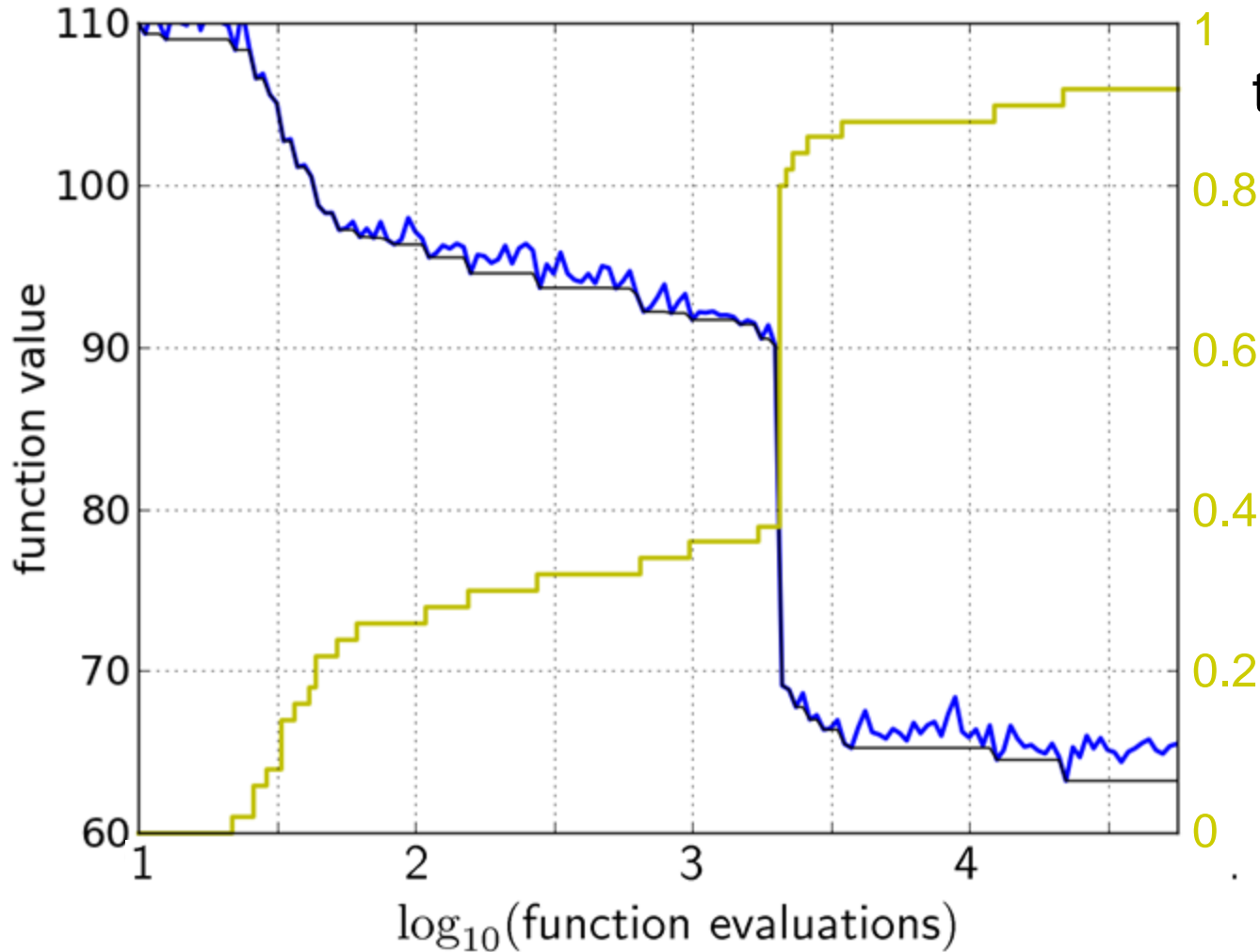


# Reconstructing A Single Run



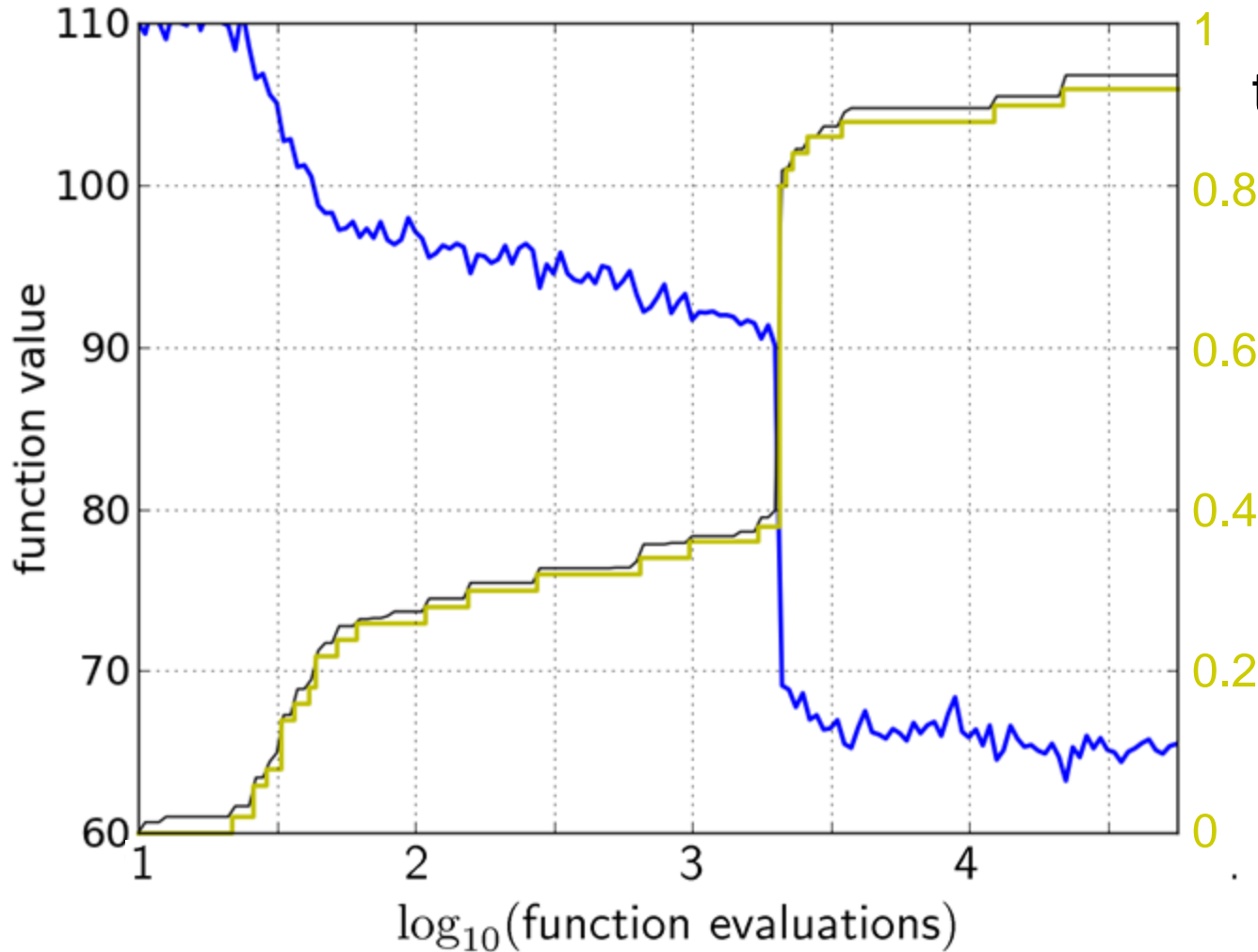
the **empirical CDF** makes a step for each star, is monotonous and displays for each budget the fraction of targets achieved within the budget

# Reconstructing A Single Run



the ECDF recovers  
the monotonous  
graph,  
discretized and  
flipped

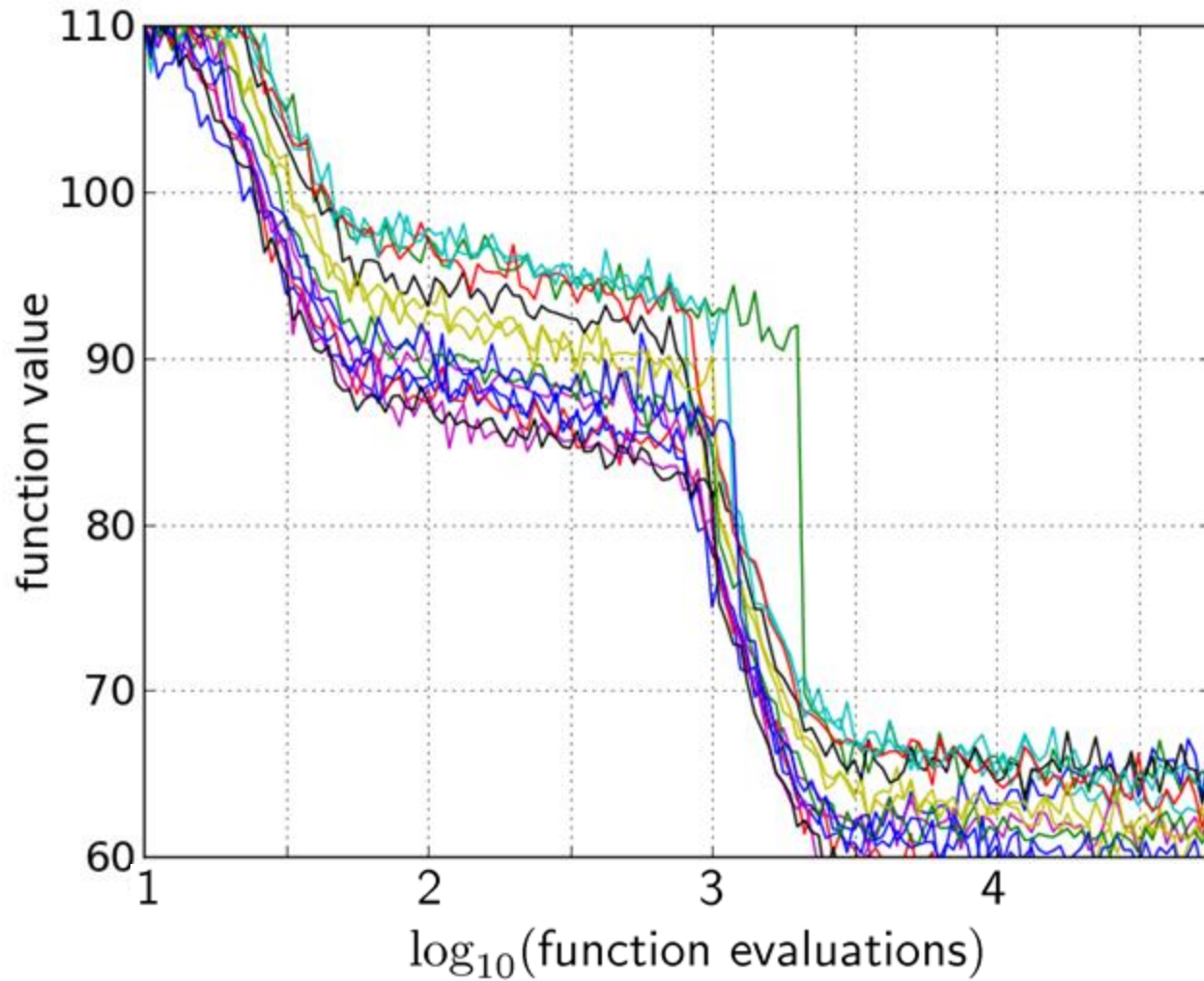
# Reconstructing A Single Run



the ECDF recovers  
the monotonous  
graph,  
discretized and  
flipped

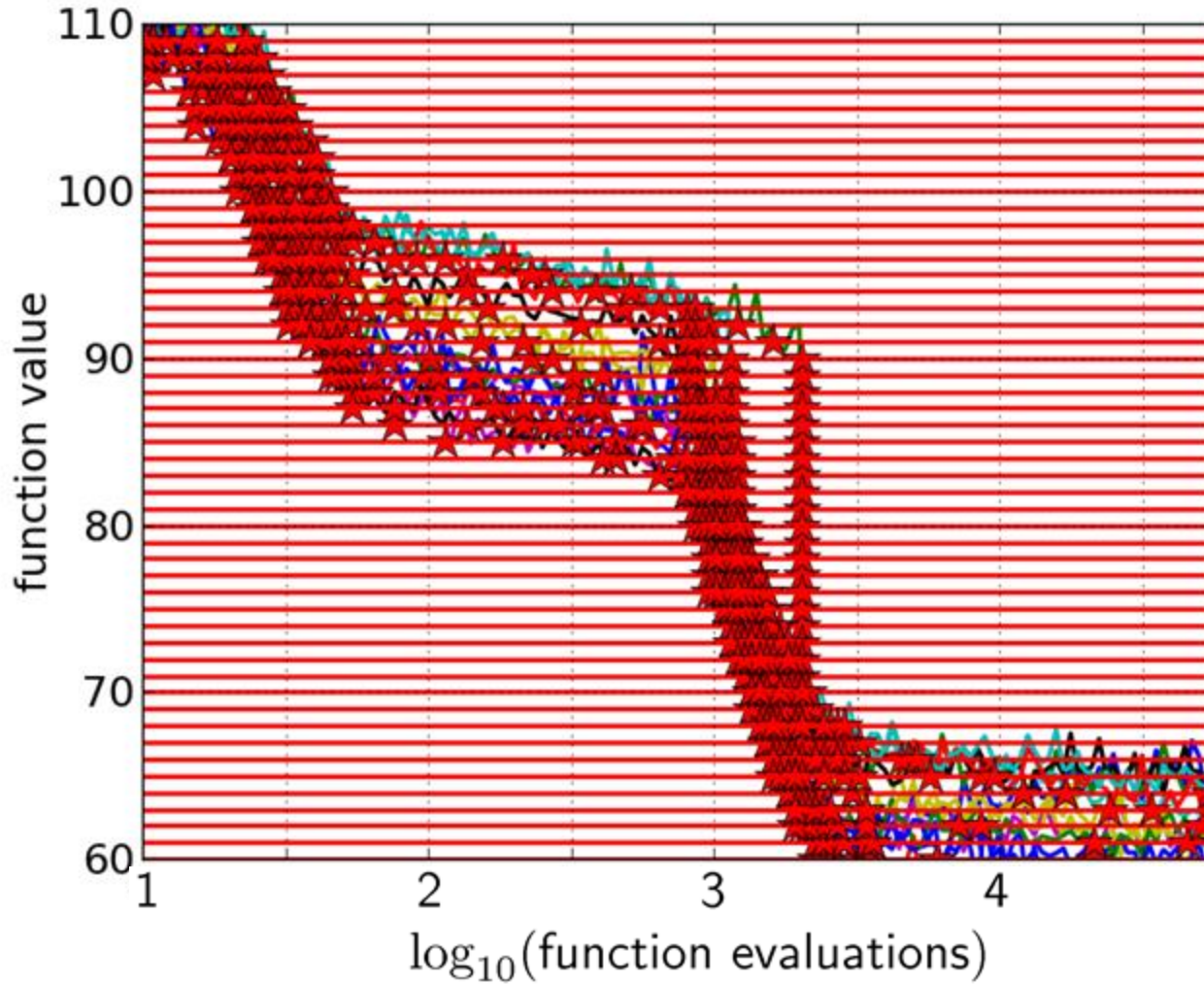


# Aggregation



15 runs

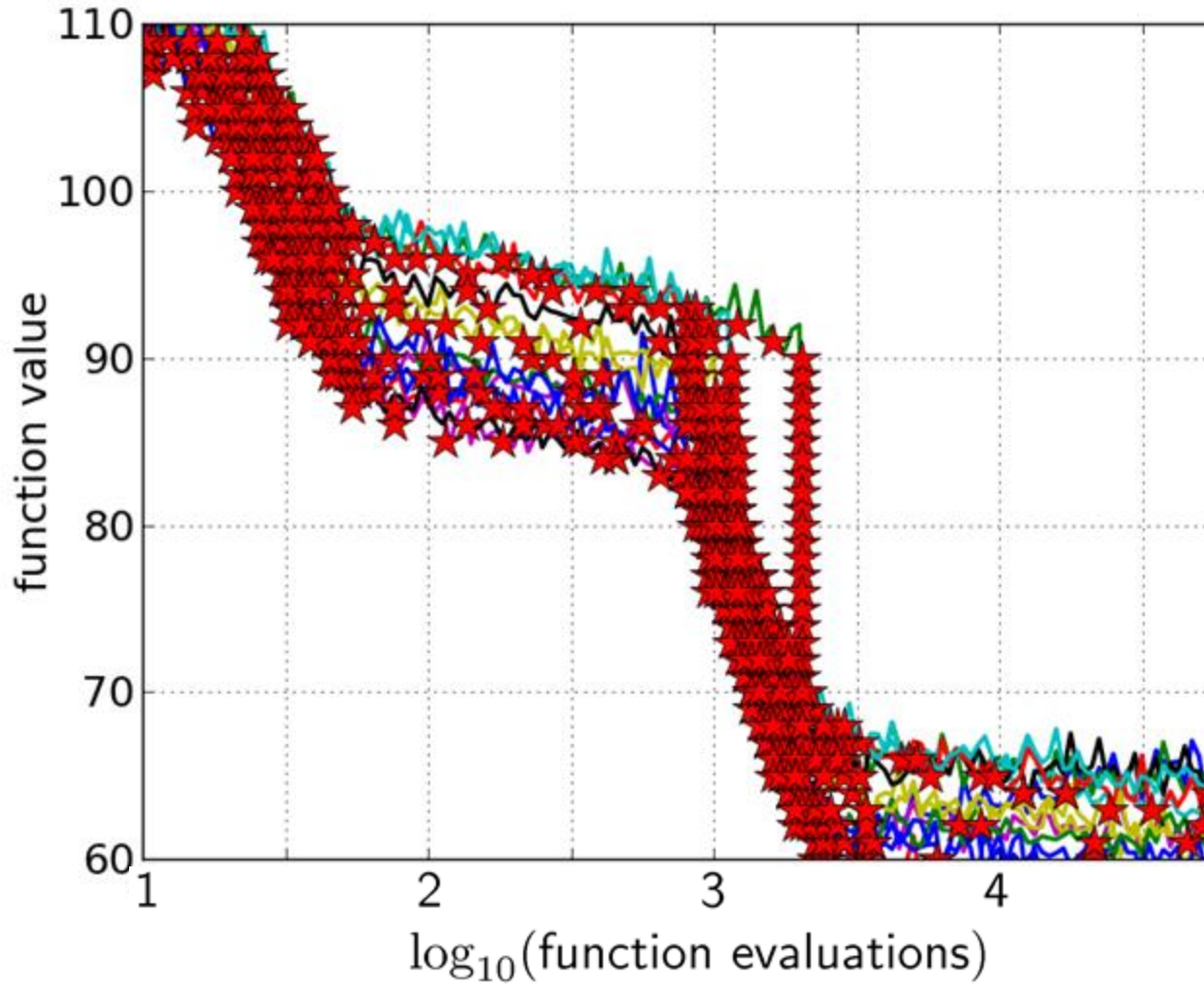
# Aggregation



15 runs

50 targets

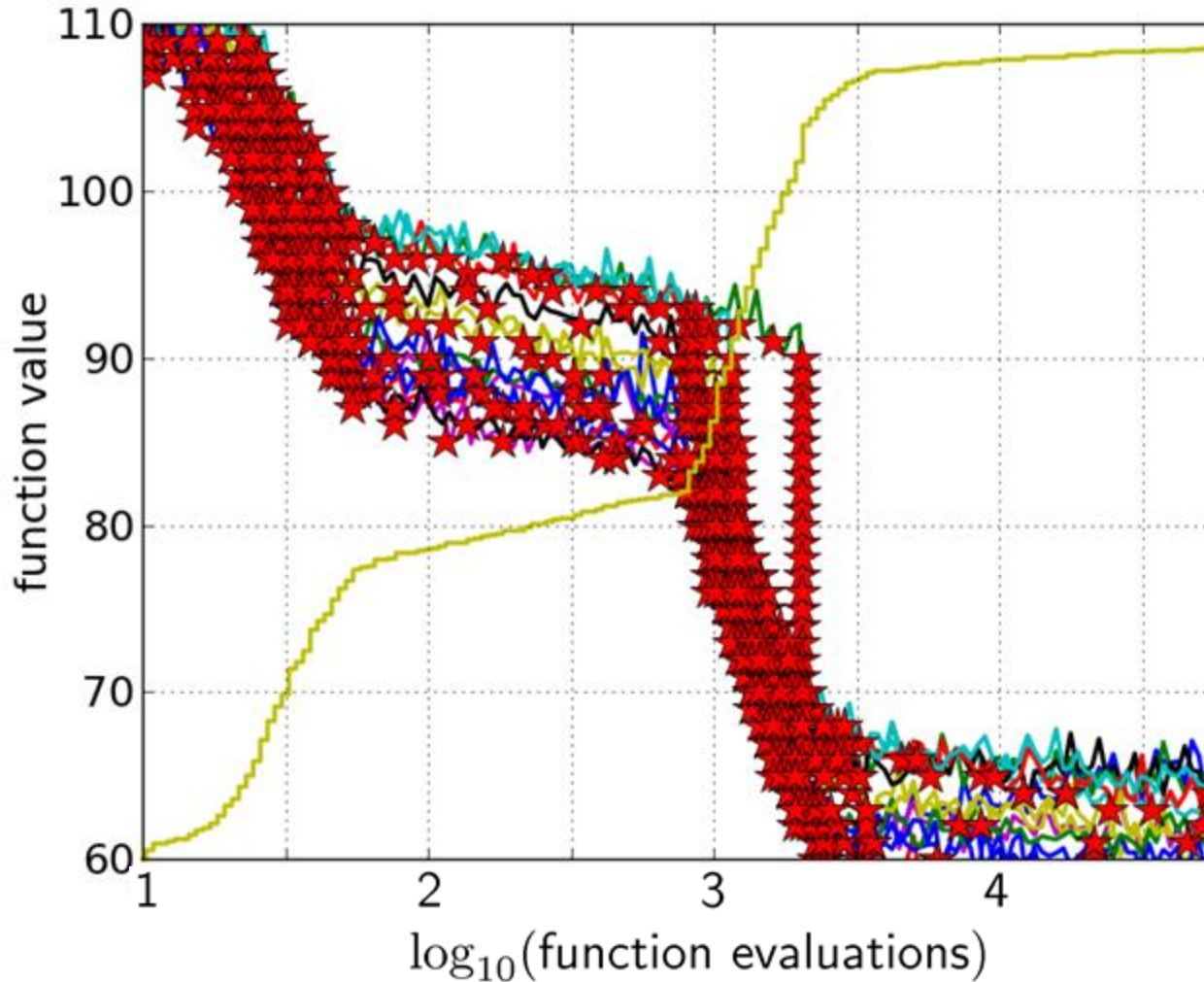
# Aggregation



15 runs

50 targets

# Aggregation

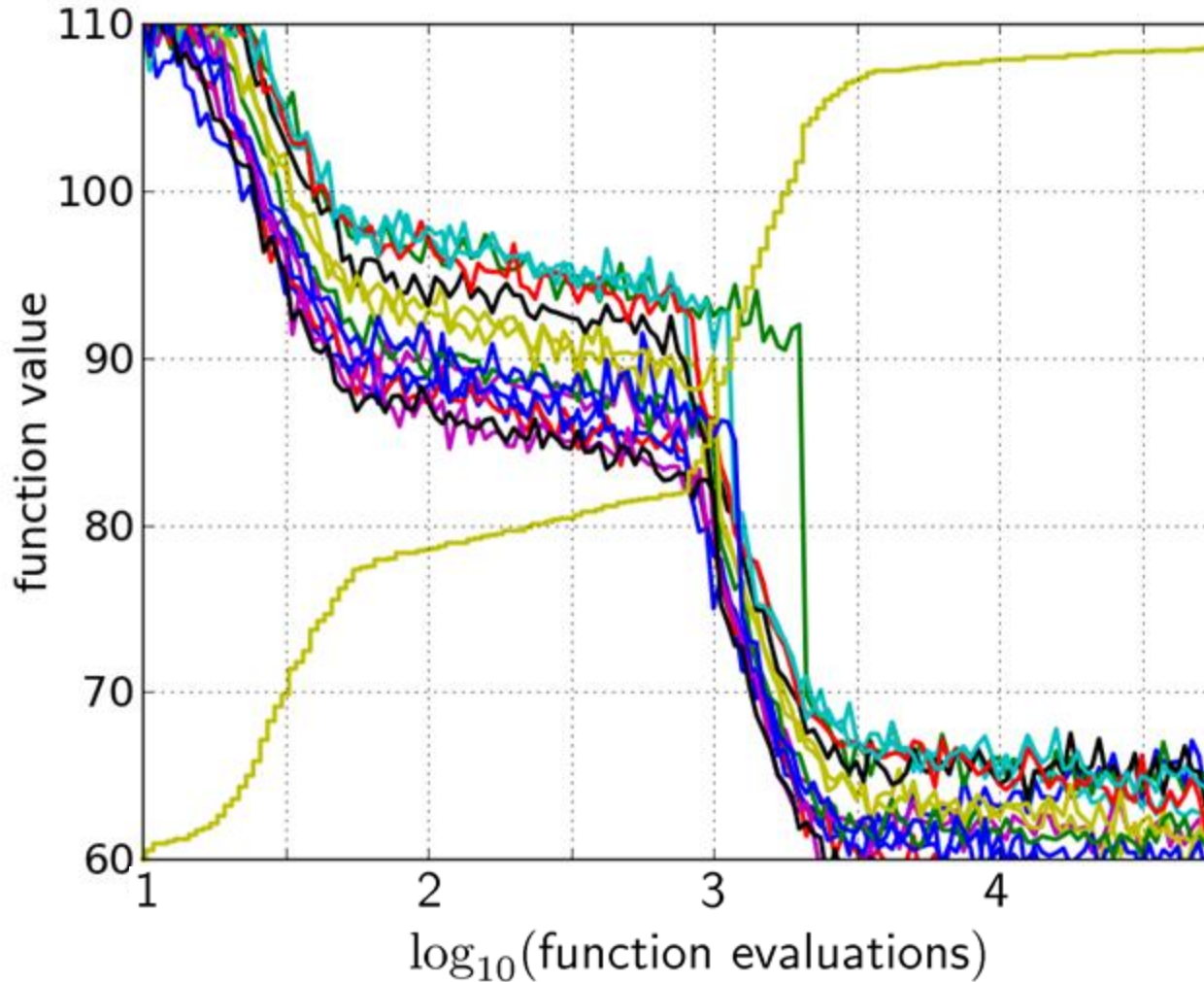


15 runs

50 targets

ECDF with 750  
steps

# Aggregation

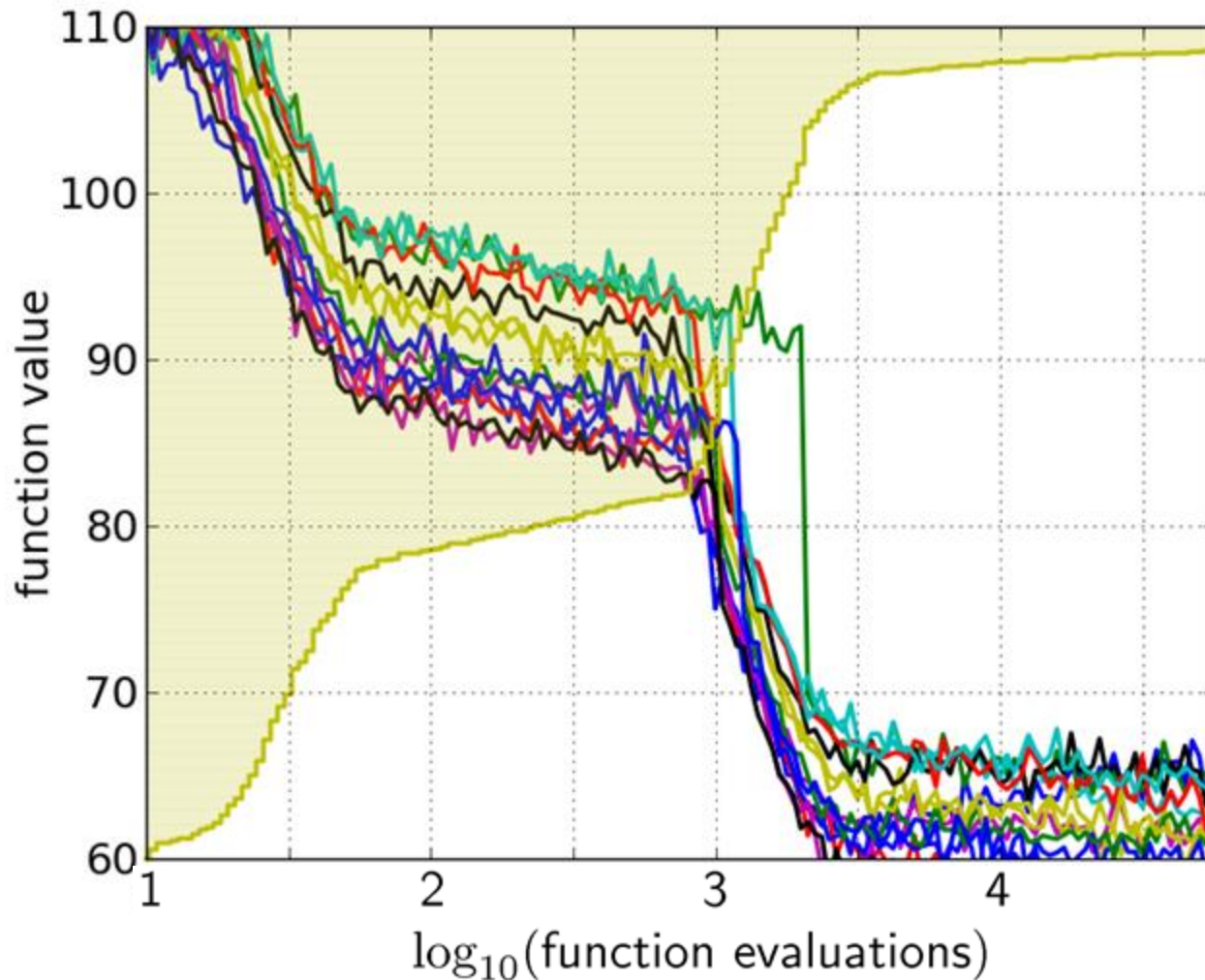


50 targets from  
15 runs

...integrated in a  
single graph



# Interpretation



50 targets from  
15 runs  
integrated in a  
single graph

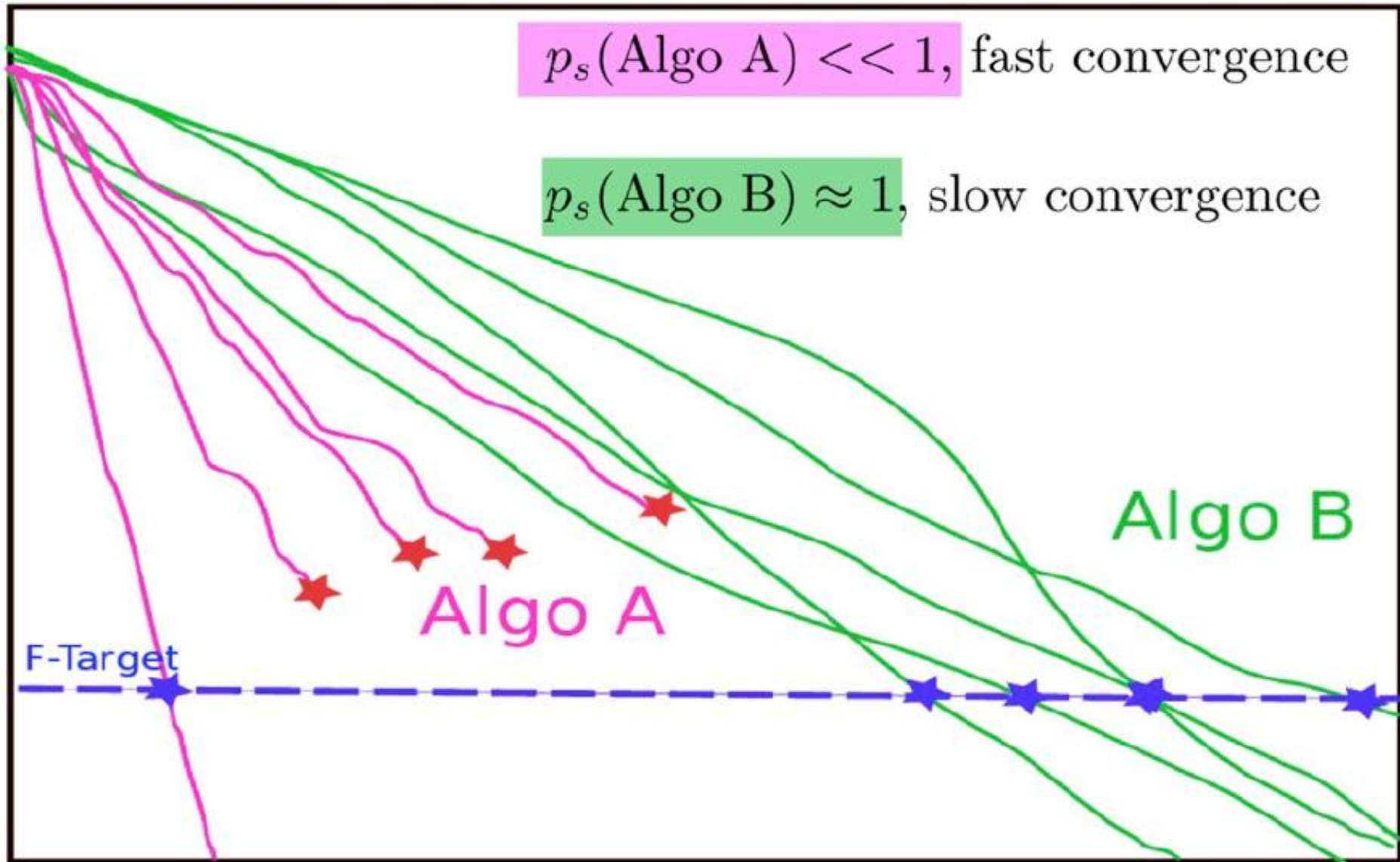
area over the  
ECDF curve

=

average log  
runtime

(or geometric avg.  
runtime) over all  
targets (difficult and  
easy) and all runs

# Fixed-target: Measuring Runtime

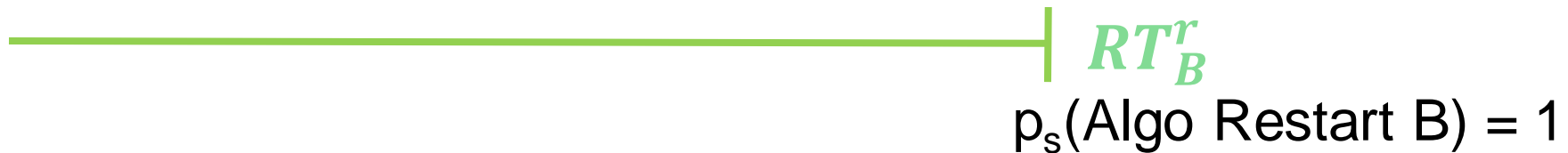


# Fixed-target: Measuring Runtime

- Algo Restart A:



- Algo Restart B:





# Fixed-target: Measuring Runtime

- Expected running time of the restarted algorithm:

$$E[RT^r] = \frac{1 - p_s}{p_s} E[RT_{unsuccessful}] + E[RT_{successful}]$$

- Estimator average running time (aRT):

$$\hat{p}_s = \frac{\#successes}{\#runs}$$

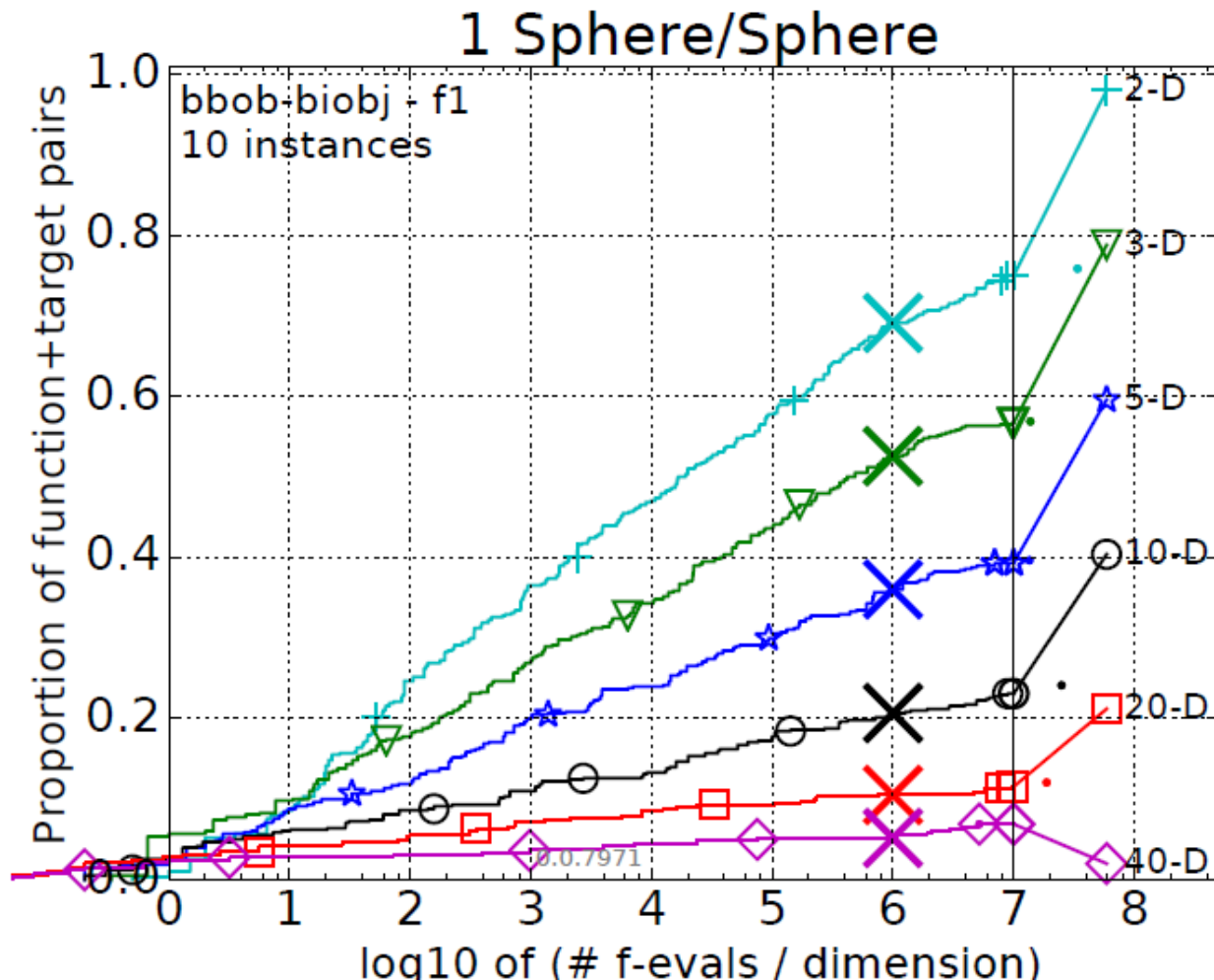
$\widehat{RT}_{unsucc}$  = Average evals of unsuccessful runs

$\widehat{RT}_{succ}$  = Average evals of successful runs

$$aRT = \frac{\text{total \#evals}}{\#successes}$$

# ECDFs with Simulated Restarts

What we typically plot are ECDFs of the simulated restarted algorithms:

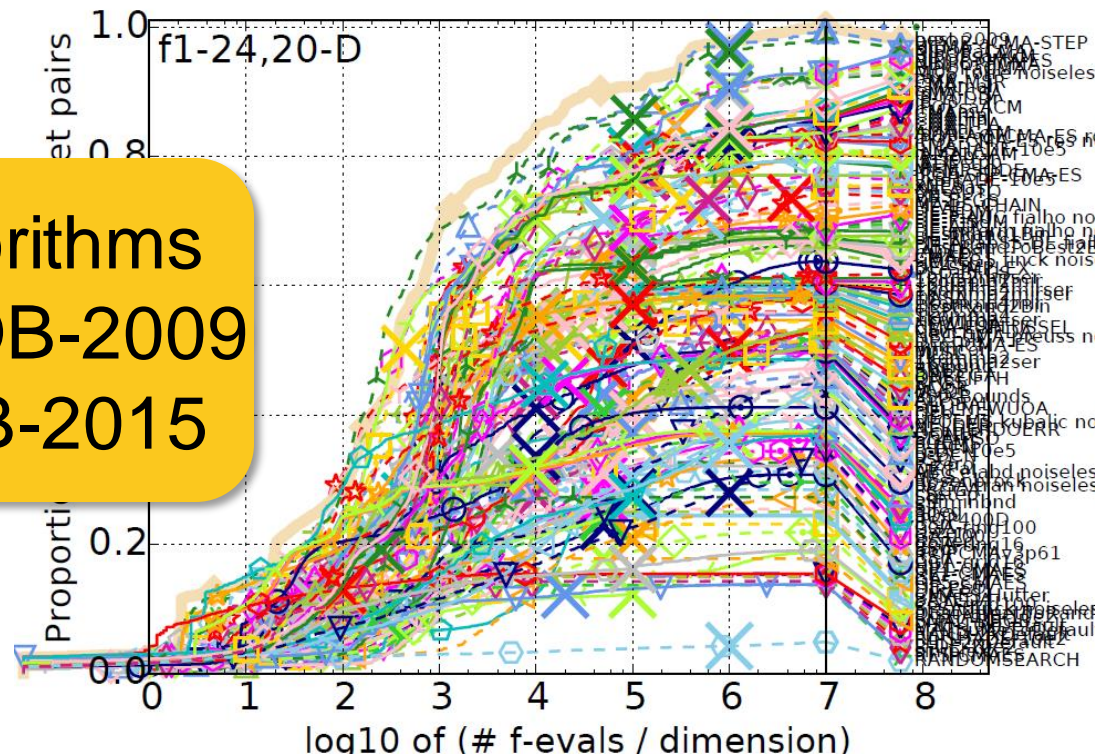


# Worth to Note: ECDFs in COCO

In COCO, ECDF graphs

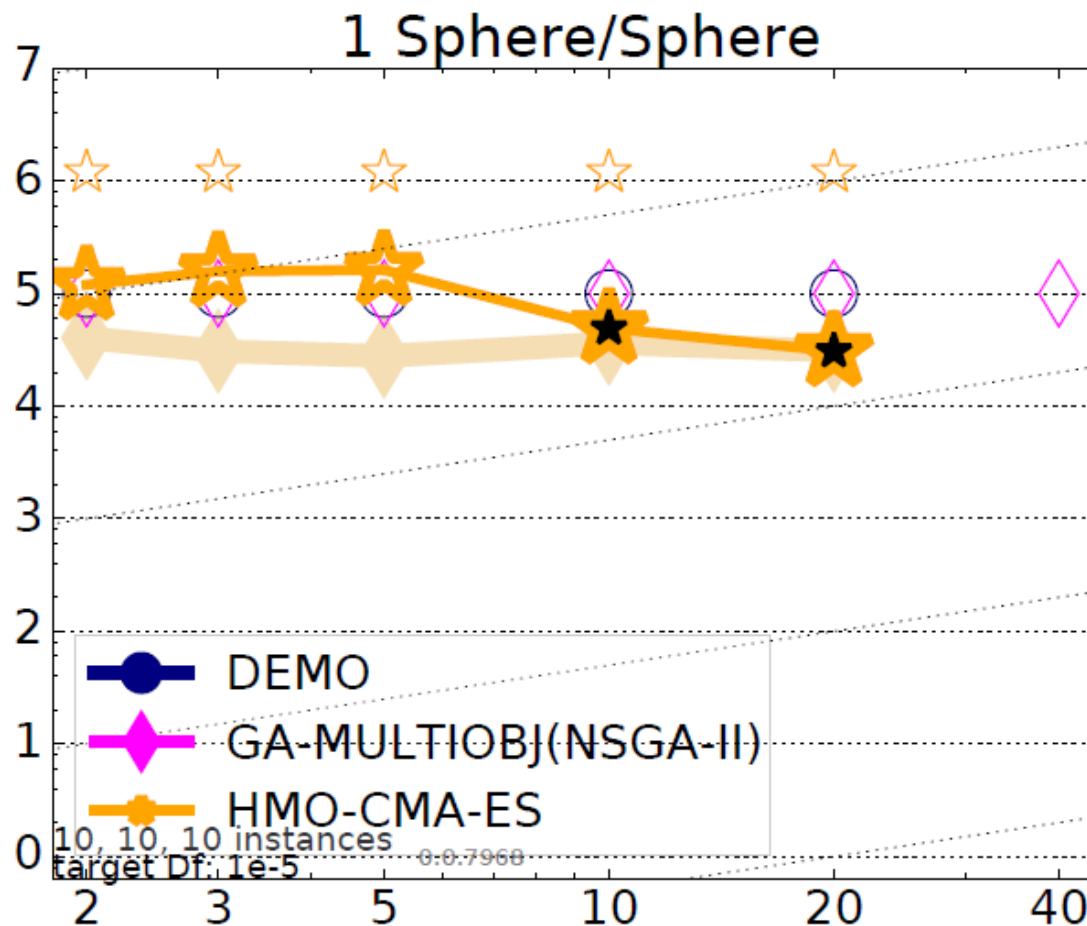
- never aggregate over dimension
  - but often over targets and functions
- can show data of more than 1 algorithm at a time

150 algorithms  
from BBOB-2009  
till BBOB-2015



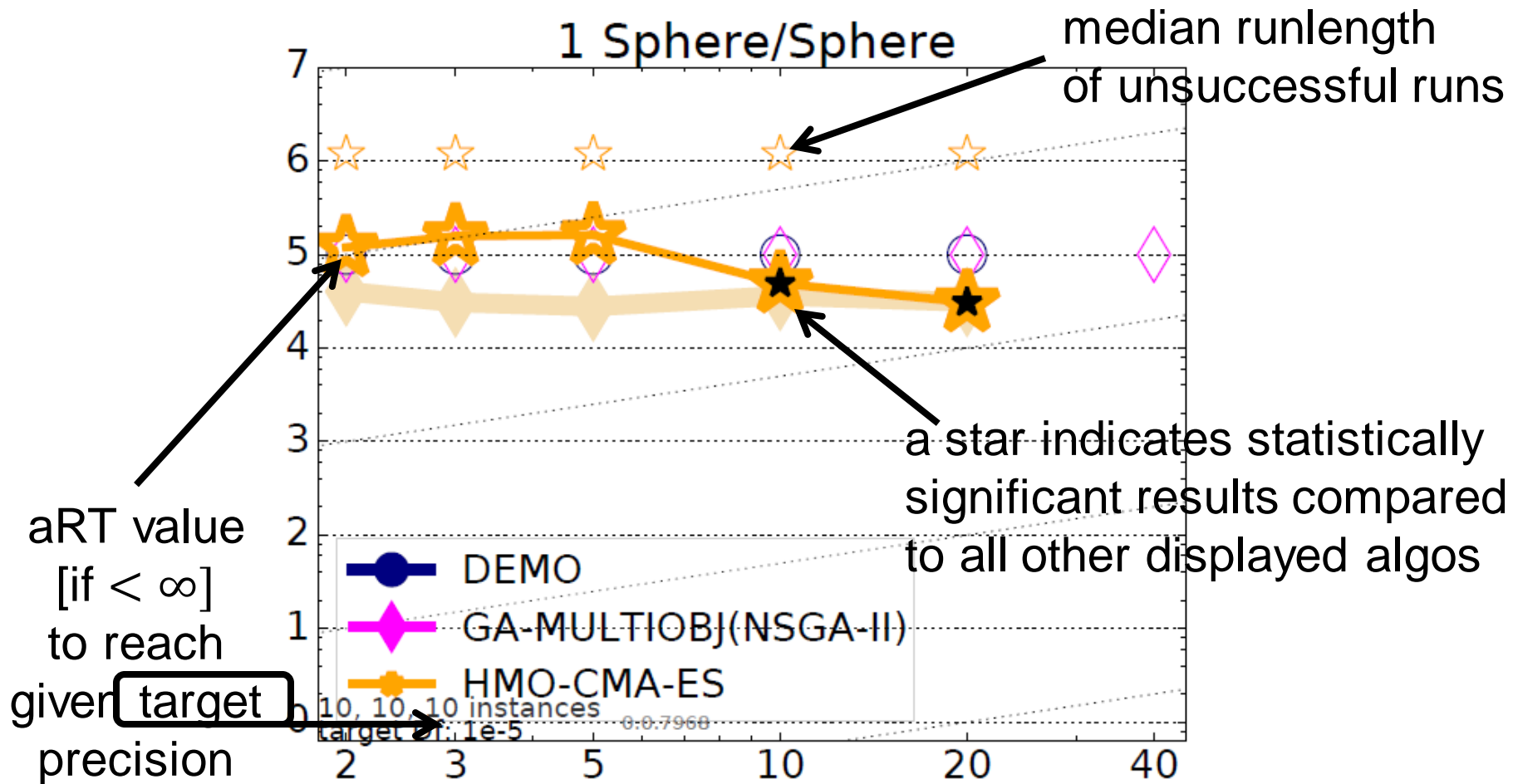
# Another Interesting Plot...

...comparing aRT values over several algorithms



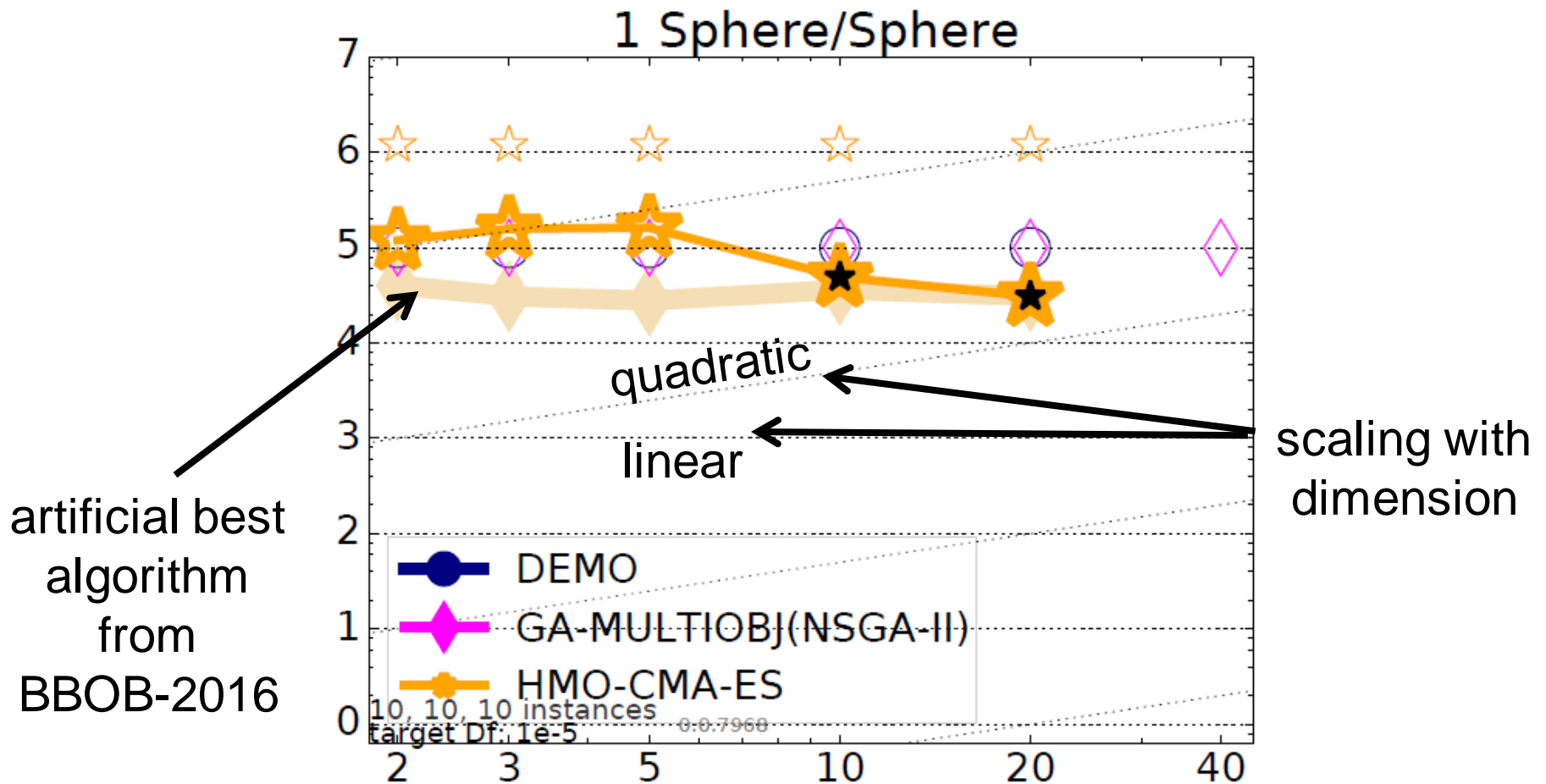
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# Another Interesting Plot...

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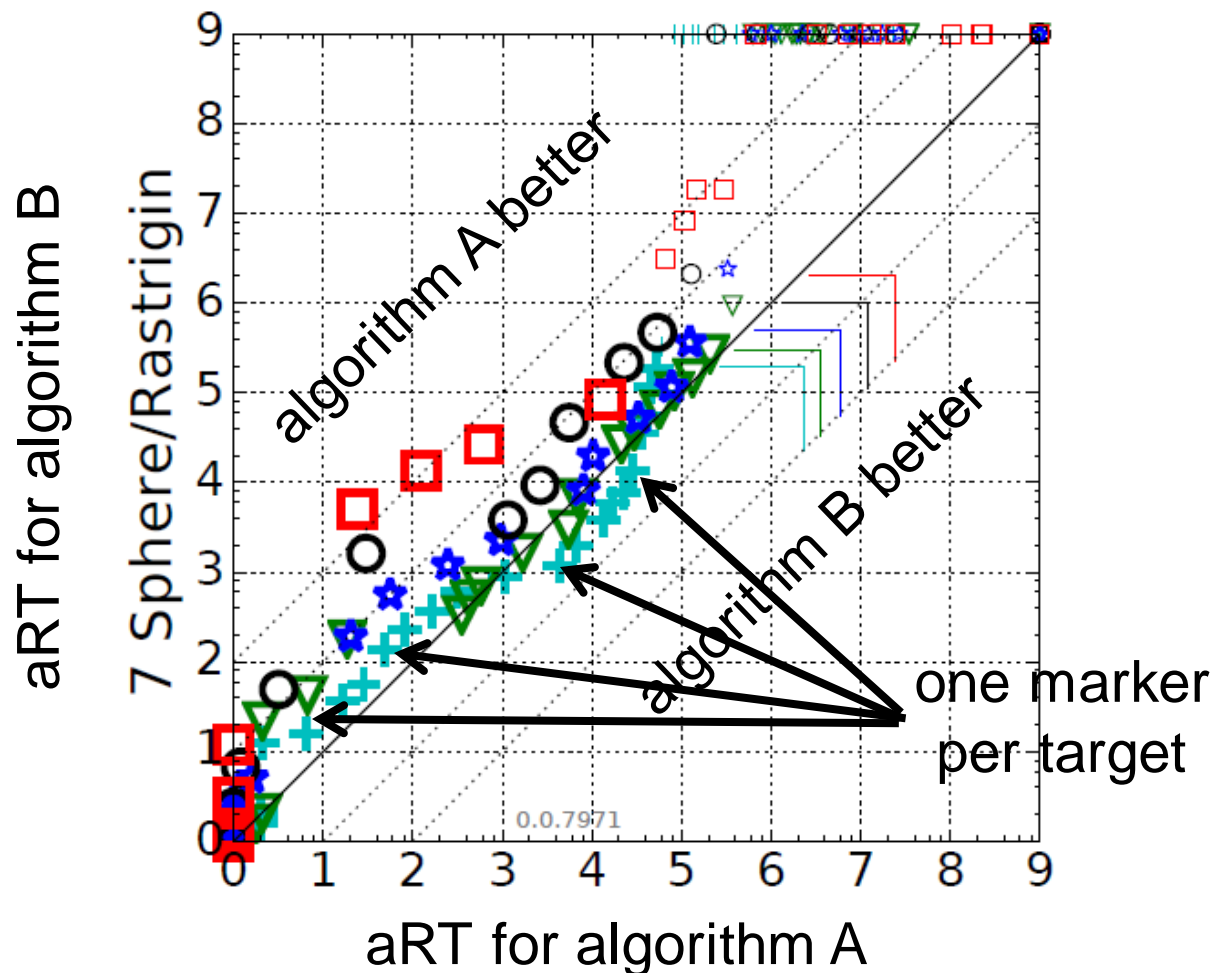


# Interesting for 2 Algorithms...

...are scatter plots

dimensions:

2:+, 3:▽, 5:\*, 10:○, 20:□, 40:◇.



# There are more Plots...















...but they are probably less interesting for us here













# **The single-objective BBOB functions**

# bbob Testbed

- 24 functions in 5 groups:

1 Separable Functions	
f1	 Sphere Function
f2	 Ellipsoidal Function
f3	 Rastrigin Function
f4	 Büche-Rastrigin Function
f5	 Linear Slope
2 Functions with low or moderate conditioning	
f6	 Attractive Sector Function
f7	 Step Ellipsoidal Function
f8	 Rosenbrock Function, original
f9	 Rosenbrock Function, rotated
3 Functions with high conditioning and unimodal	
f10	 Ellipsoidal Function
f11	 Discus Function
f12	 Bent Cigar Function
f13	 Sharp Ridge Function
f14	 Different Powers Function

4 Multi-modal functions with adequate global structure	
f15	 Rastrigin Function
f16	 Weierstrass Function
f17	 Schaffers F7 Function
f18	 Schaffers F7 Functions, moderately ill-conditioned
f19	 Composite Griewank-Rosenbrock Function F8F2
5 Multi-modal functions with weak global structure	
f20	 Schwefel Function
f21	 Gallagher's Gaussian 101-me Peaks Function
f22	 Gallagher's Gaussian 21-hi Peaks Function
f23	 Katsuura Function
f24	 Lunacek bi-Rastrigin Function

- 6 dimensions: 2, 3, 5, 10, 20, (40 optional)

# Notion of Instances

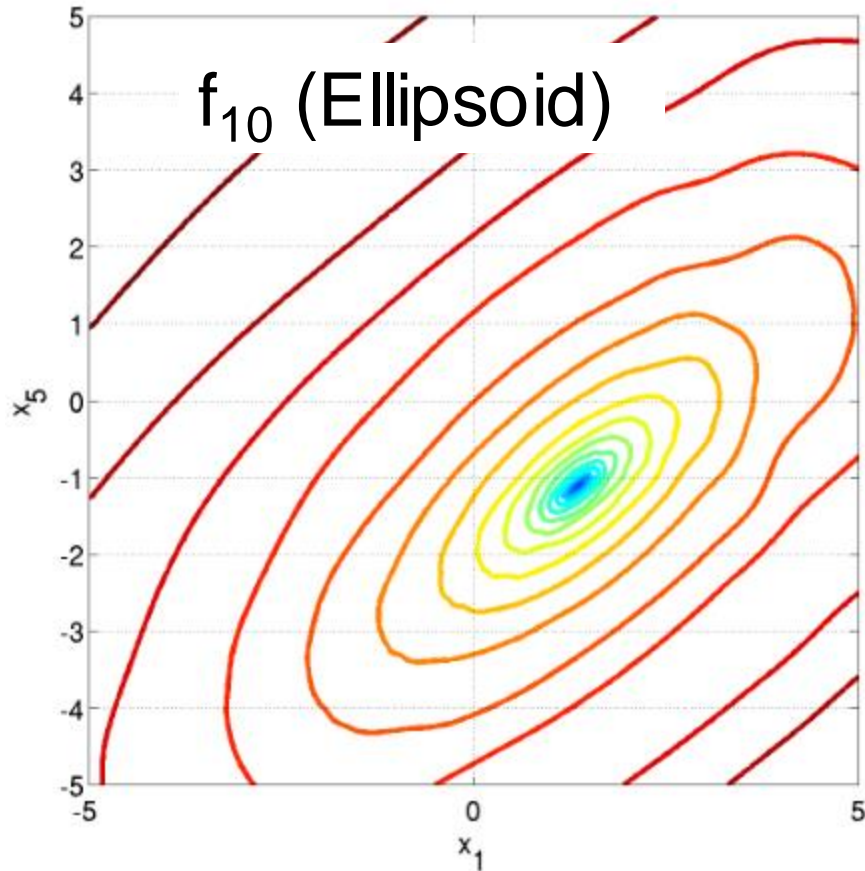
- All COCO problems come in form of instances
  - e.g. as translated/rotated versions of the same function
- Prescribed instances typically change from year to year
  - avoid overfitting
  - 5 instances are always kept the same

Plus:

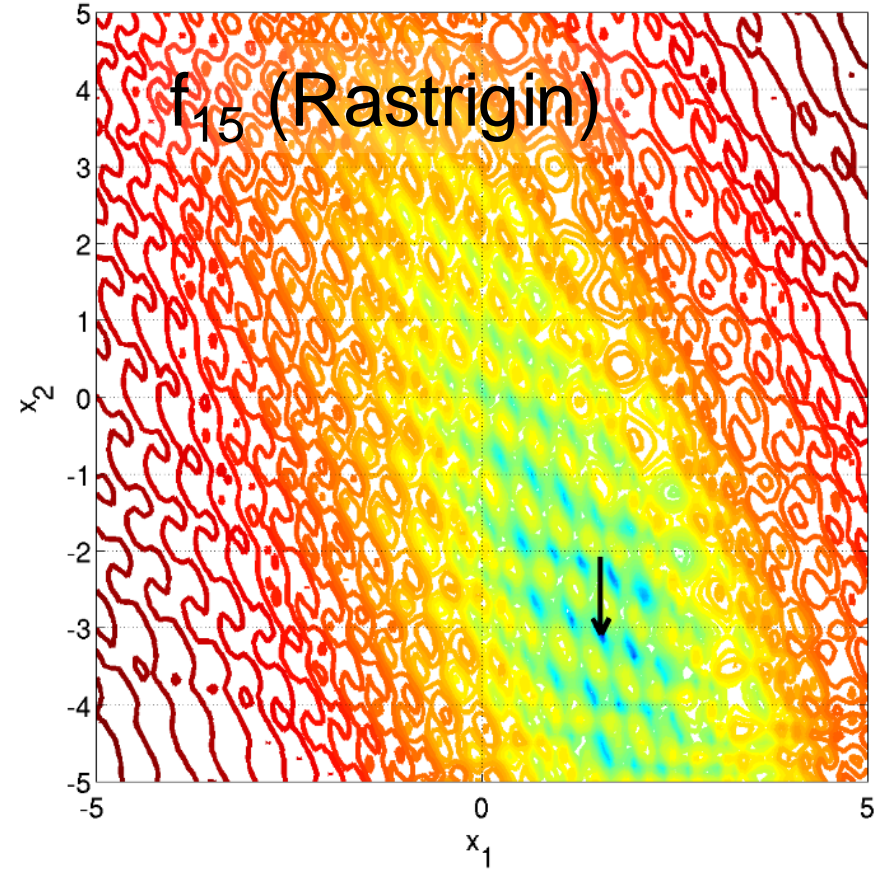
- the bbob functions are locally perturbed by non-linear transformations

# Notion of Instances

All COCO problems come in form of instances



linear transformations

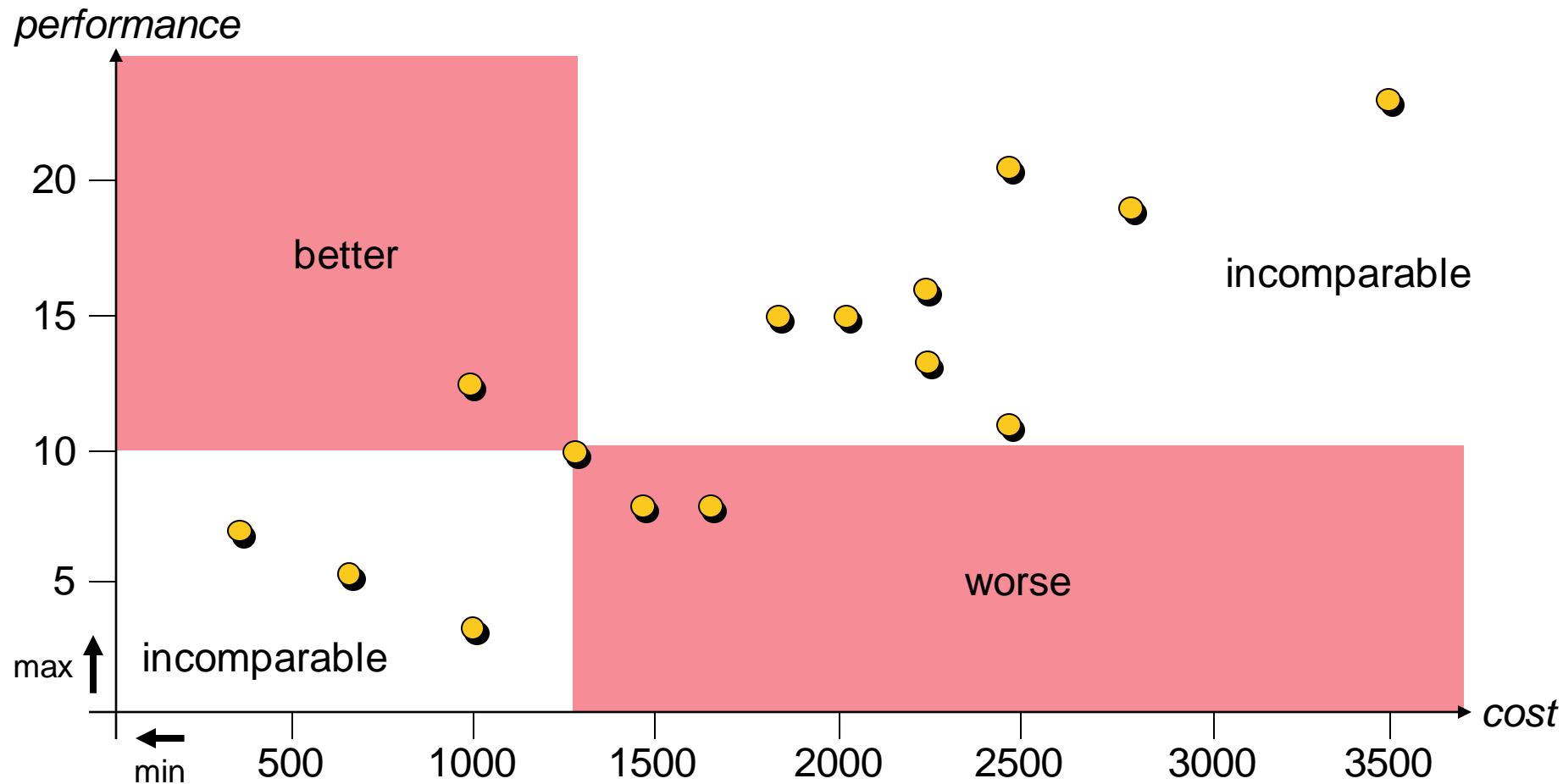


**the recent extension to  
multi-objective optimization**

# A Brief Introduction to Multiobjective Optimization

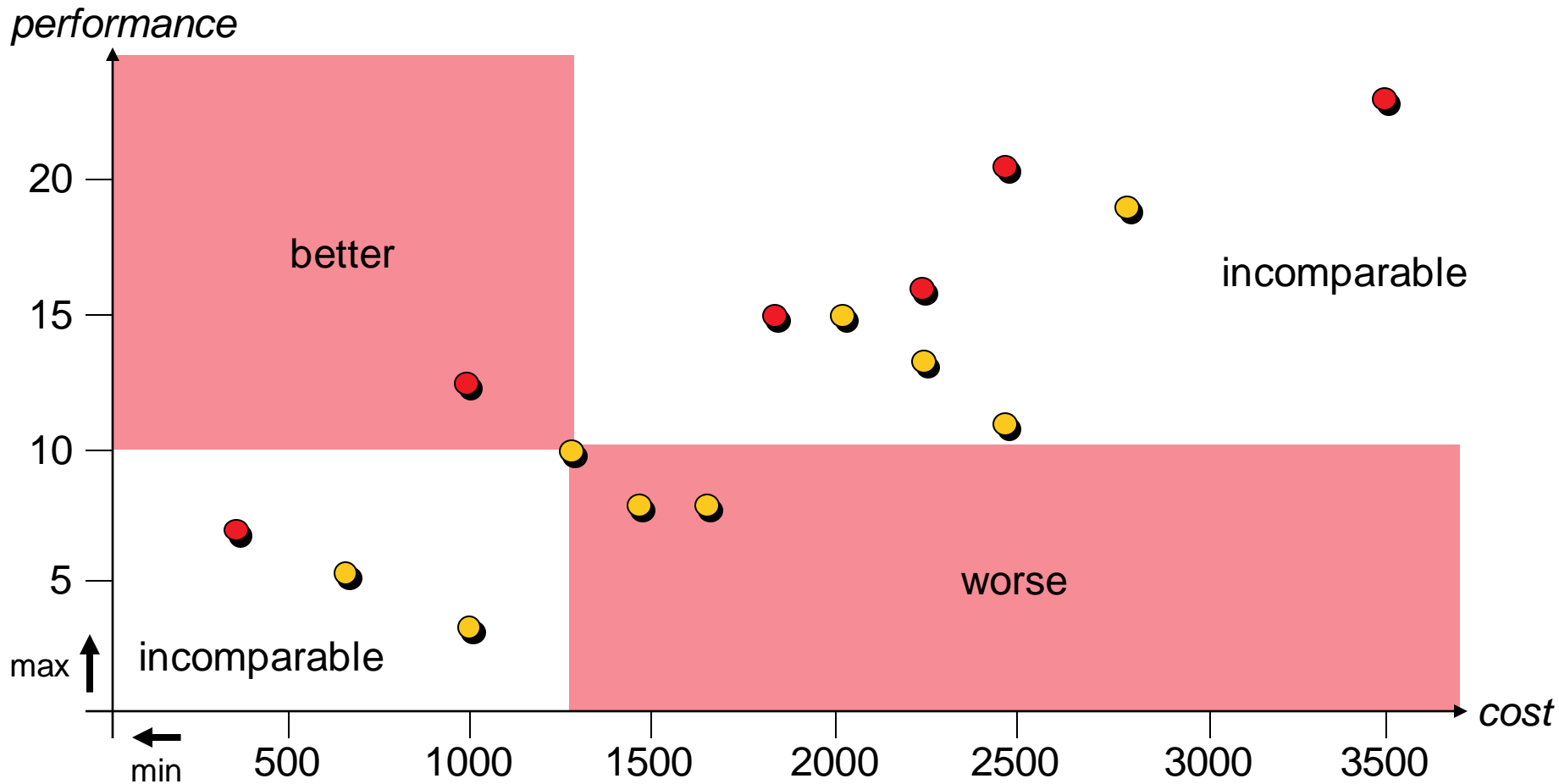
## Multiobjective Optimization (MOO)

Multiple objectives that have to be optimized simultaneously



# A Brief Introduction to Multiobjective Optimization

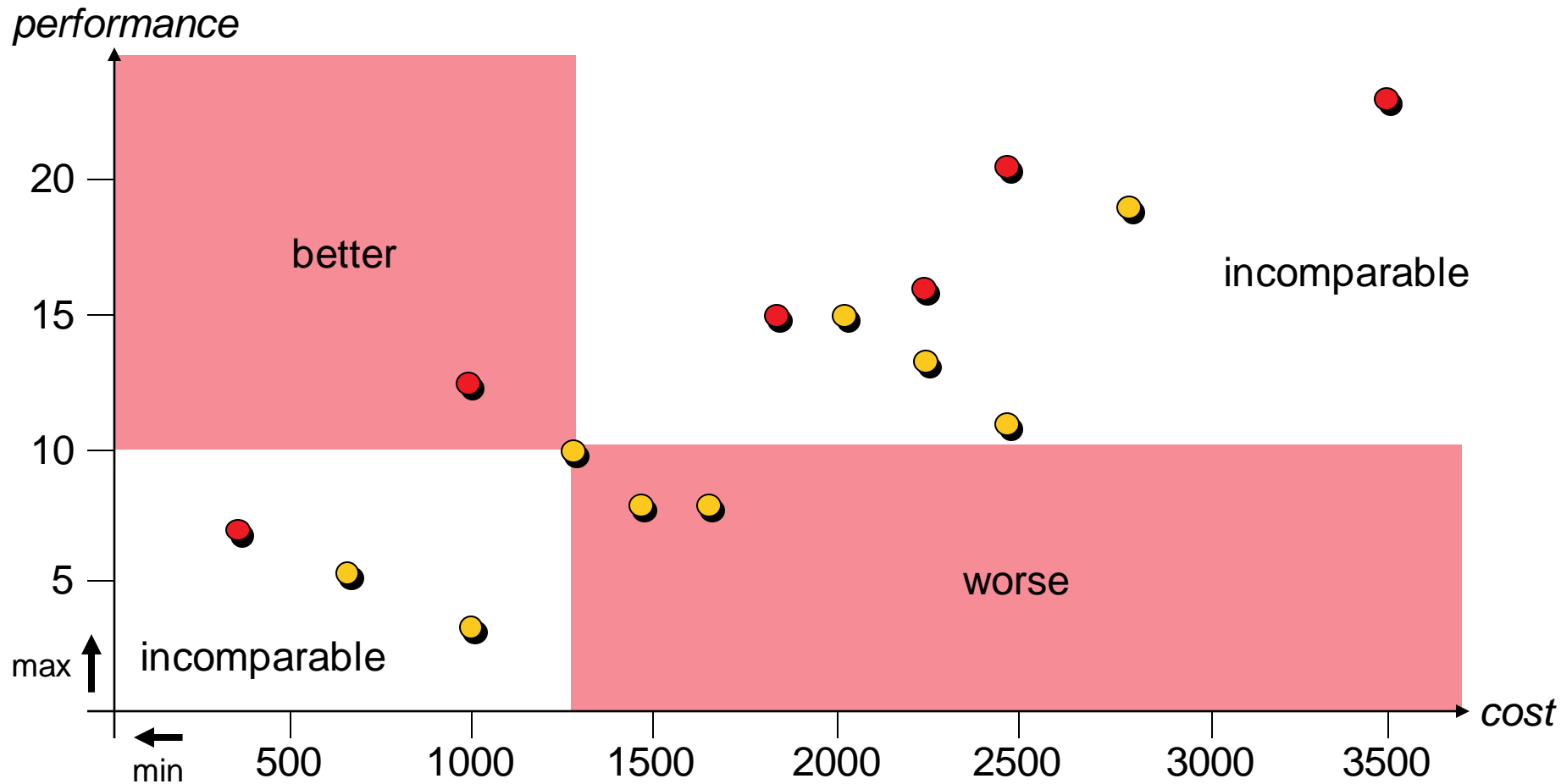
- Observations:**
- 1 there is no single optimal solution, but
  - 2 some solutions (●) are better than others (●)



# A Brief Introduction to Multiobjective Optimization

$u$  weakly Pareto dominates  $v$  ( $u \leq_{par} v$ ):  $\forall 1 \leq i \leq k : f_i(u) \leq f_i(v)$

$u$  Pareto dominates  $v$  ( $u <_{par} v$ ):  $u \leq_{par} v \wedge v \not\leq_{par} u$

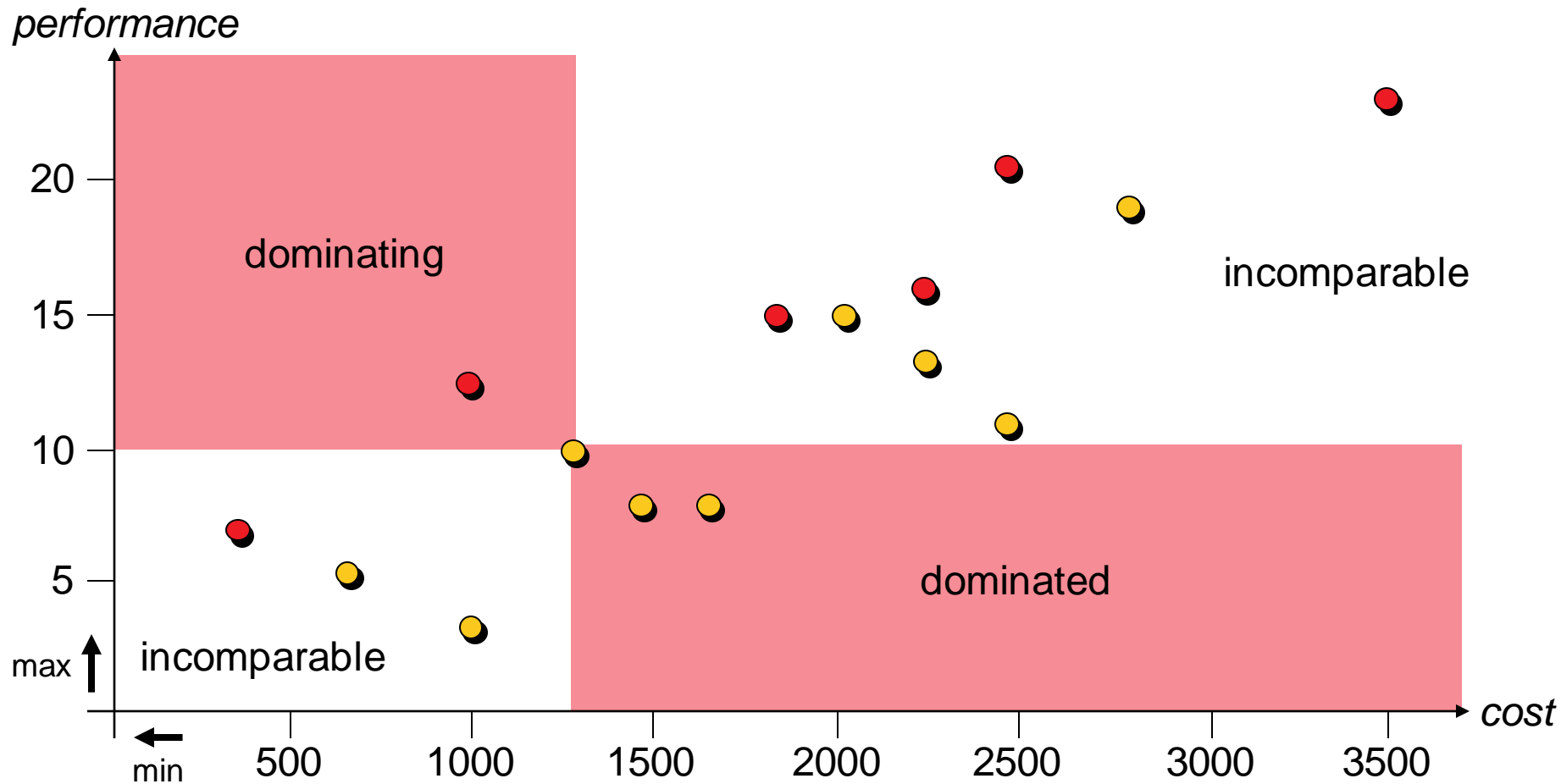




# A Brief Introduction to Multiobjective Optimization

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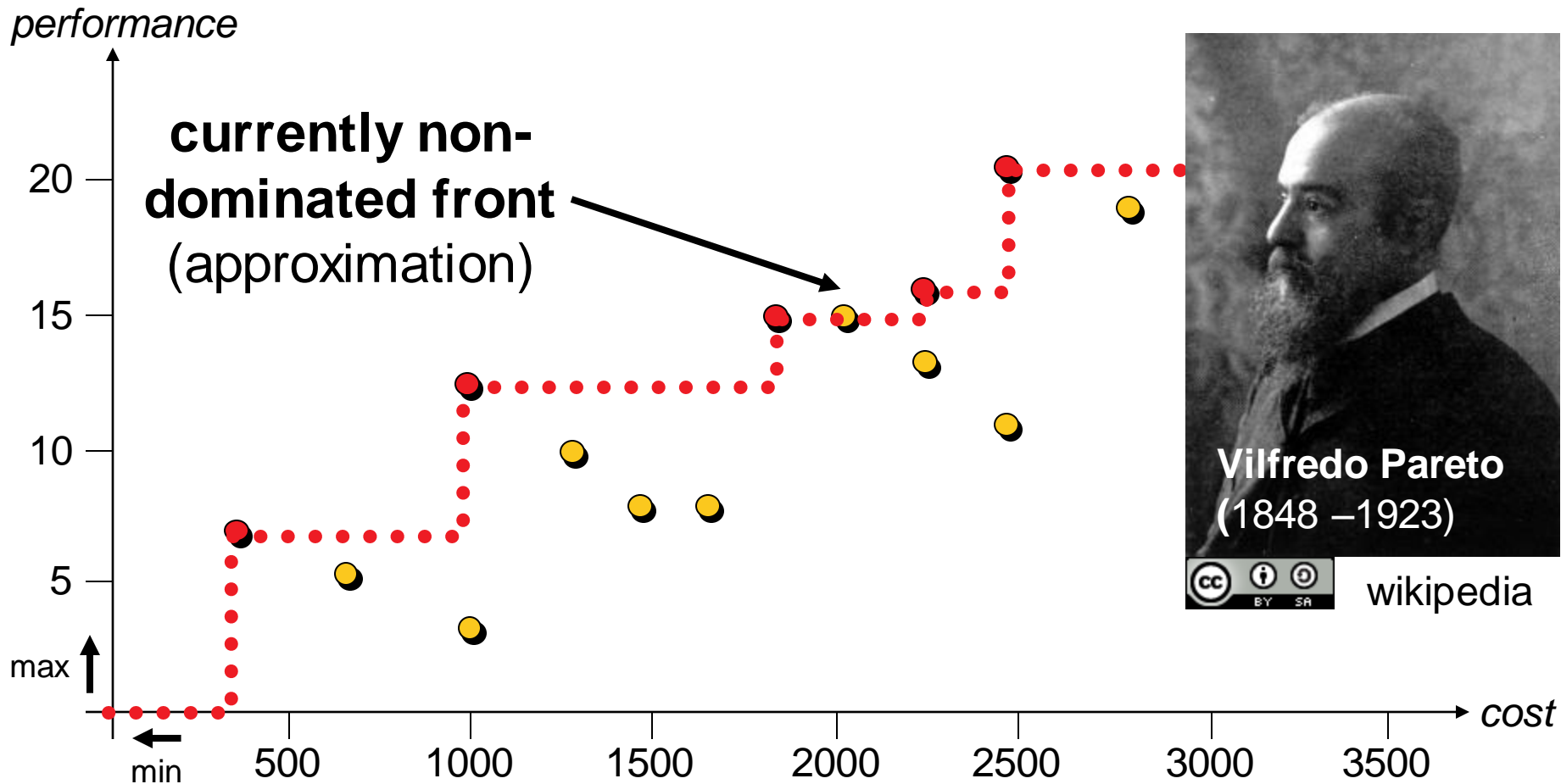
$u$  Pareto dominates  $v$  ( $u <_{par} v$ ):  $u \leq_{par} v \wedge v \not\leq_{par} u$



# A Brief Introduction to Multiobjective Optimization

**Pareto set:** set of all non-dominated solutions (decision space)

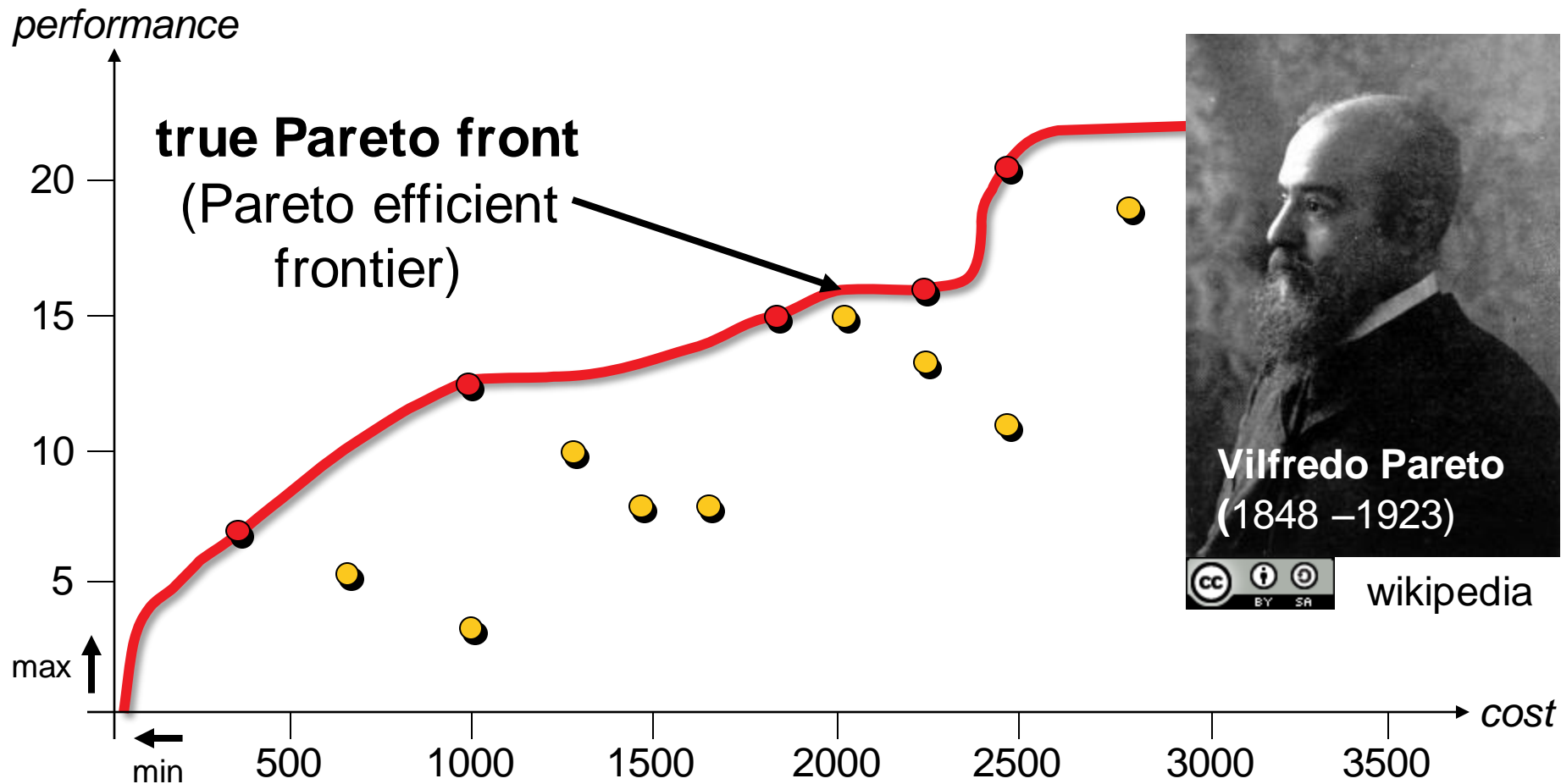
**Pareto front:** its image in the objective space



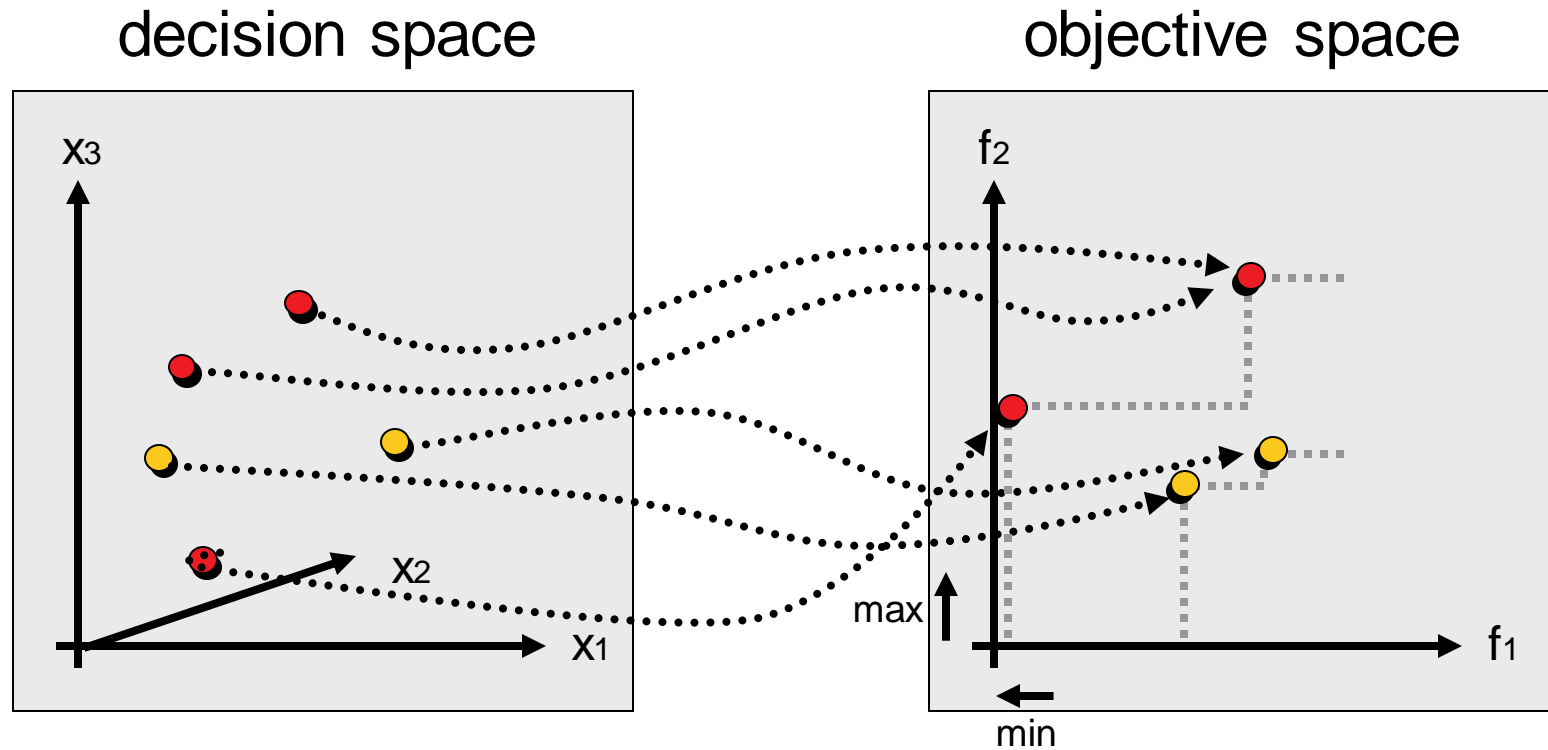
# A Brief Introduction to Multiobjective Optimization

**Pareto set:** set of all non-dominated solutions (decision space)

**Pareto front:** its image in the objective space

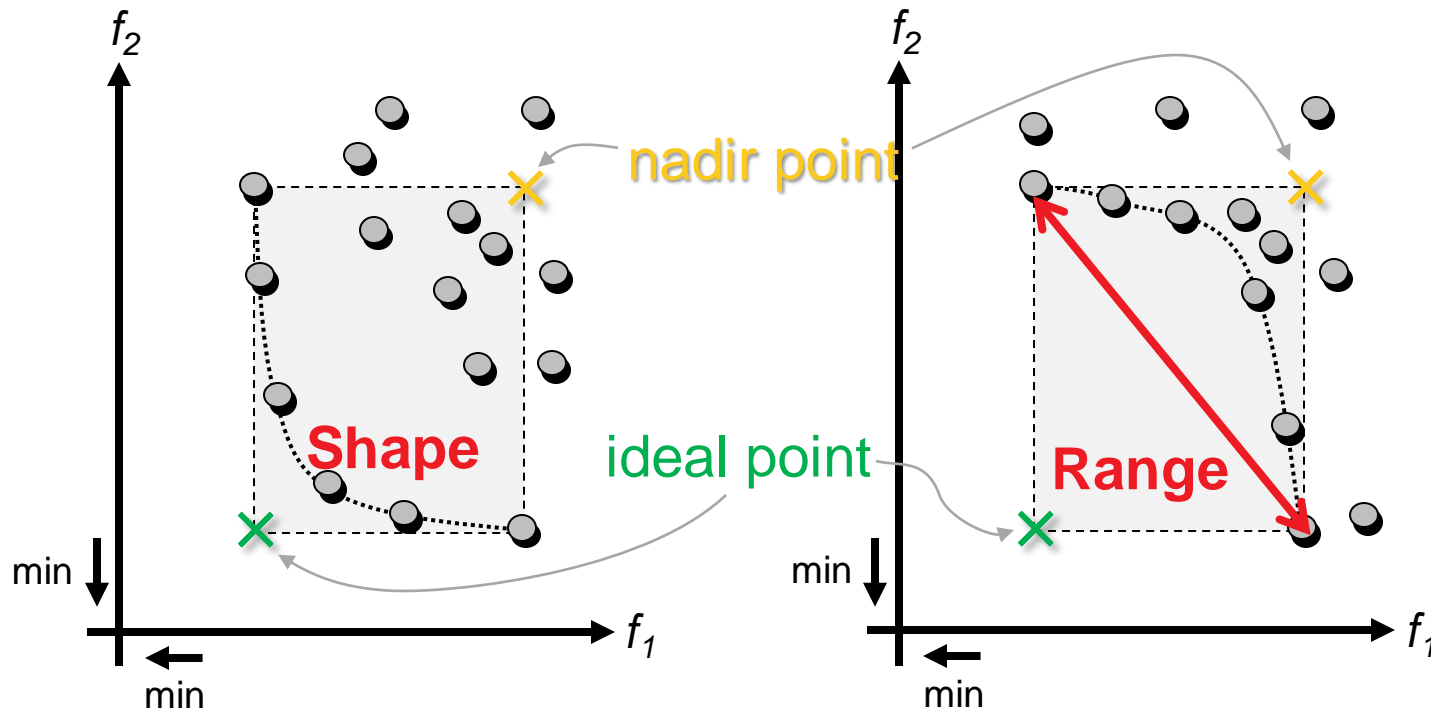


# A Brief Introduction to Multiobjective Optimization



solution of Pareto-optimal set    ● vector of Pareto-optimal front  
non-optimal decision vector    ● non-optimal objective vector

# A Brief Introduction to Multiobjective Optimization



ideal point: best values  
nadir point: worst values } obtained for *Pareto-optimal* points

# Quality Indicator Approach to MOO

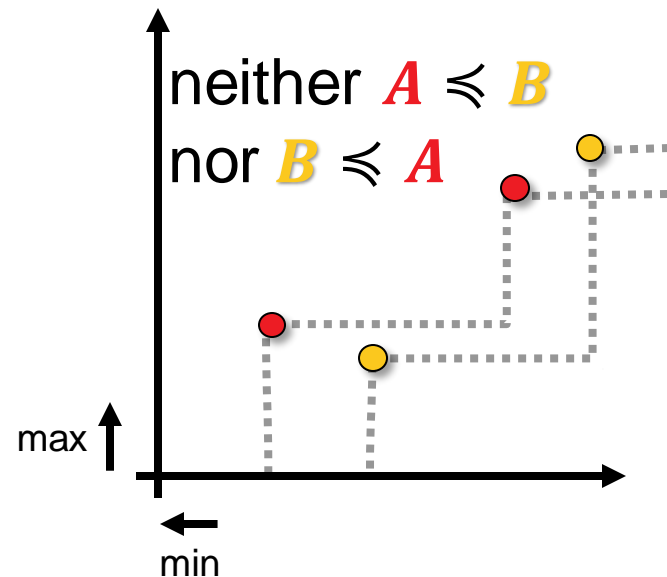
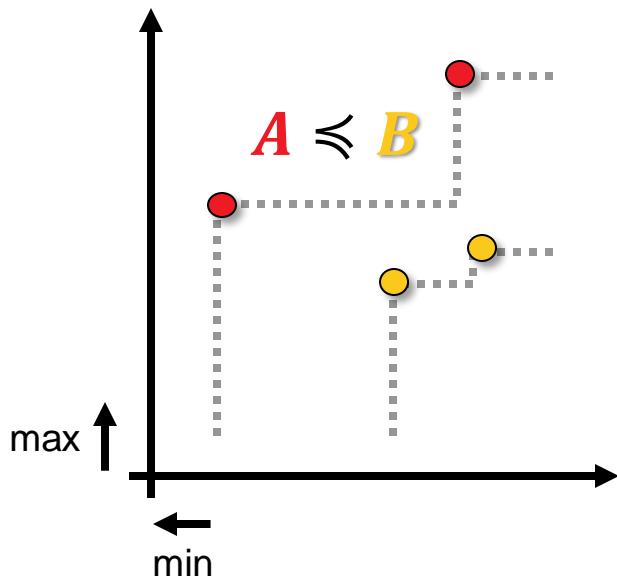
## Idea:

- transfer multiobjective problem into a set problem
- define an objective function (“quality indicator”) on sets

## Important:

⇒ Underlying dominance relation (on sets) should be reflected by the resulting set comparisons!

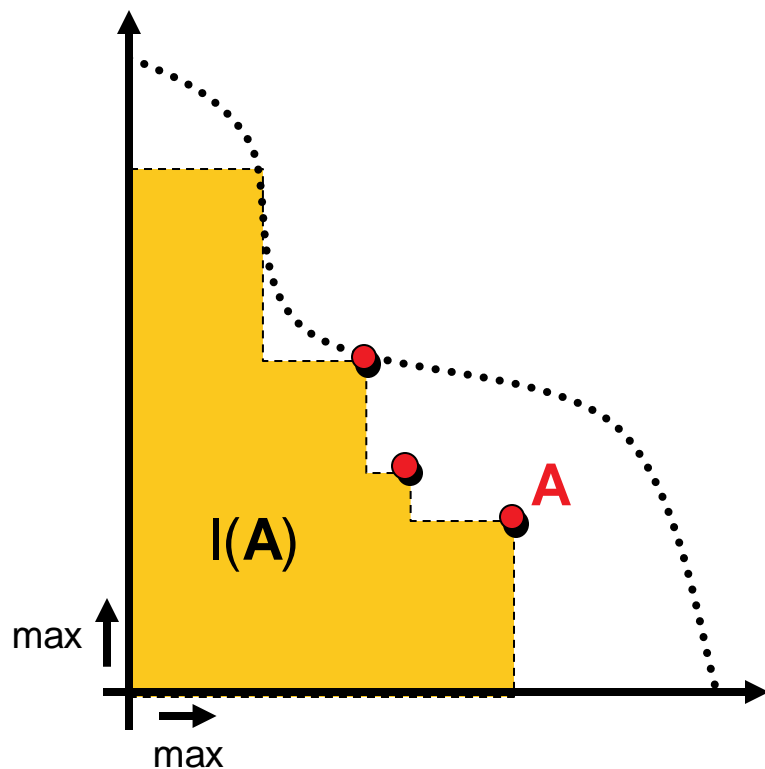
$$A \preceq B \Leftrightarrow \forall y \in B \exists x \in A x \leq_{par} y$$



# Examples of Quality Indicators

$$A \stackrel{\text{ref}}{\preceq} B :\Leftrightarrow I(A) \geq I(B)$$

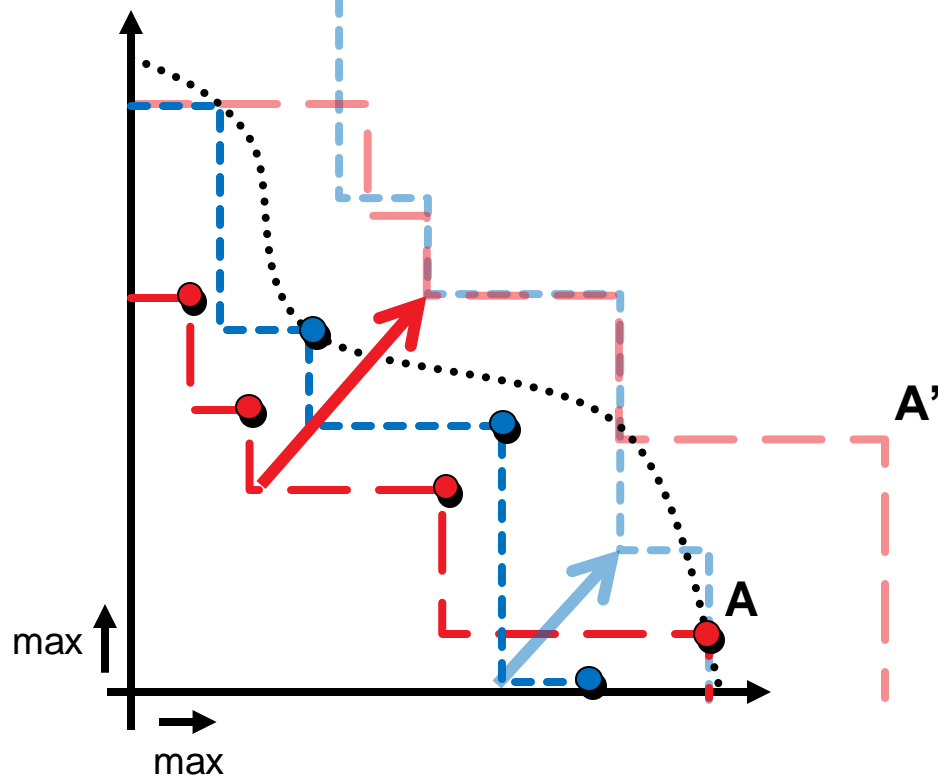
$I(A)$  = volume of the weakly dominated area in objective space



**unary** hypervolume indicator

$$A \stackrel{\text{ref}}{\preceq} B :\Leftrightarrow I(A,B) \leq I(B,A)$$

$I(A,B)$  = how much needs A to be moved to weakly dominate B

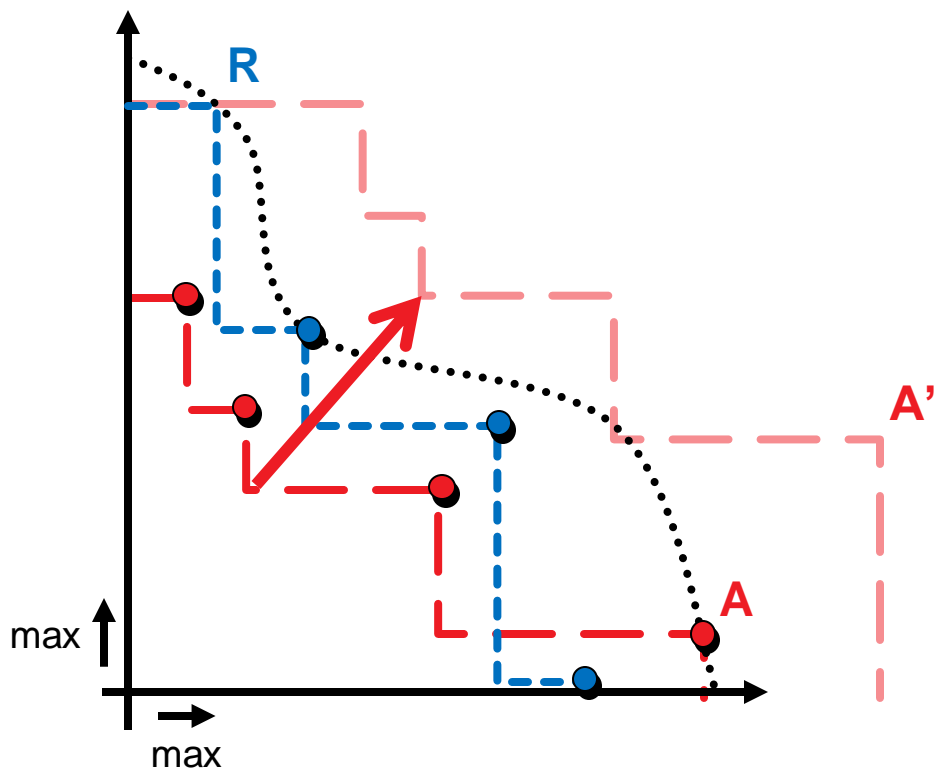


**binary** epsilon indicator

# Examples of Quality Indicators II

$$A \stackrel{\text{ref}}{\preceq} B \Leftrightarrow I(A, R) \leq I(B, R)$$

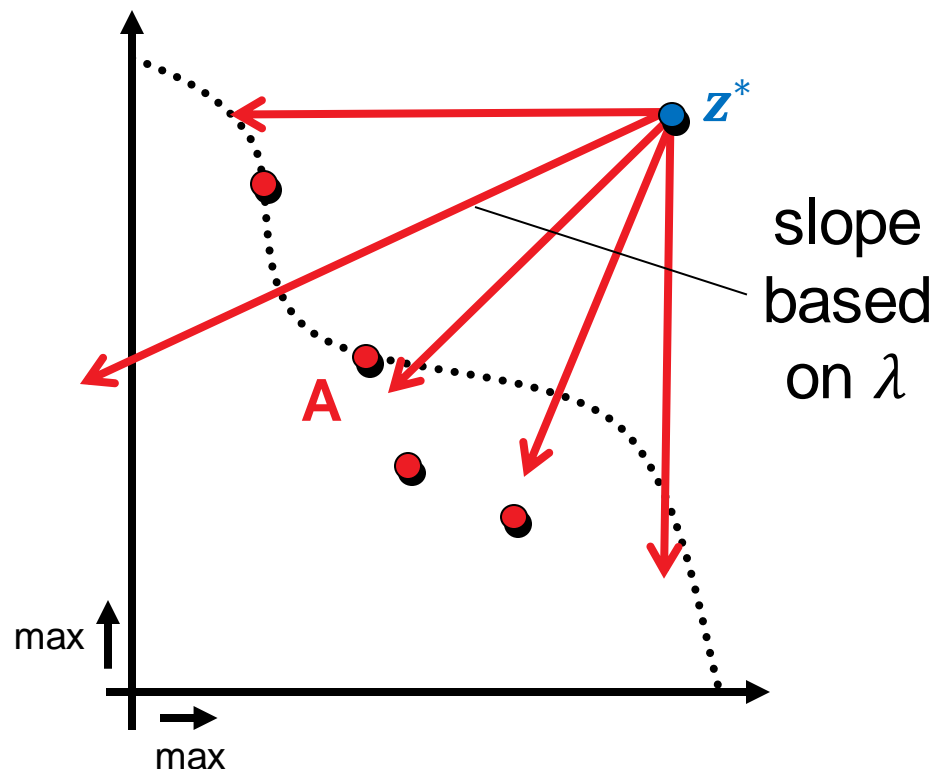
$I(A, R)$  = how much needs A to be moved to weakly dominate R



unary epsilon indicator

$$A \stackrel{\text{ref}}{\preceq} B \Leftrightarrow I(A) \leq I(B)$$

$$I(A) = \frac{1}{|\Lambda|} \sum_{\lambda \in \Lambda} \min_{a \in A} \left( \max_{j=1..m} \lambda_j |z_j^* - a_j| \right)$$



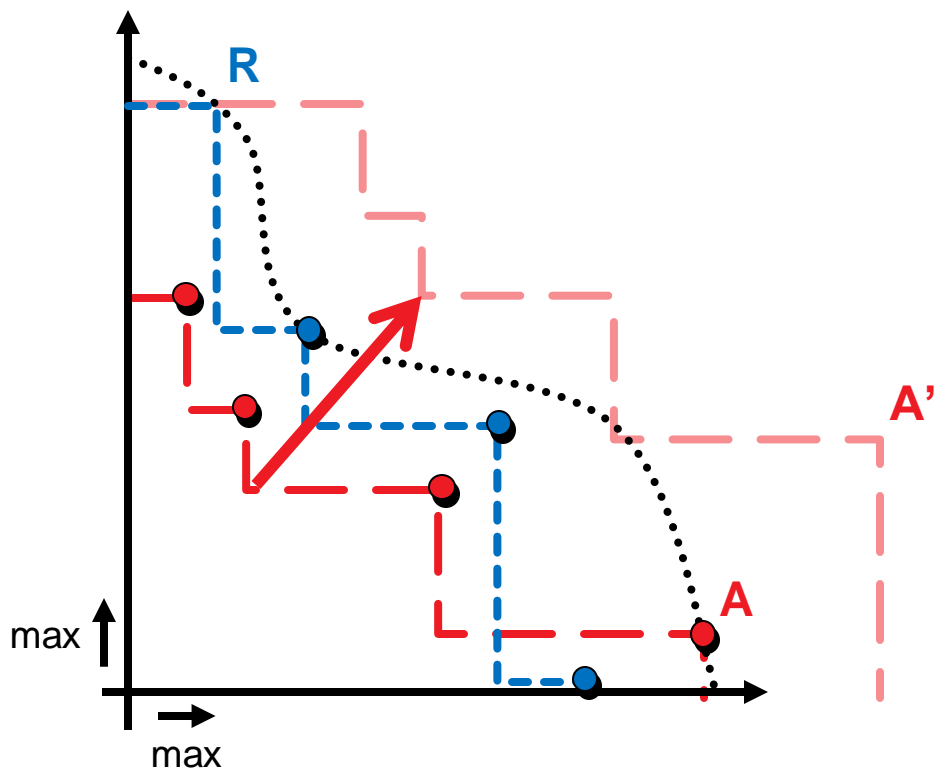
unary R2 indicator



# Examples of Quality Indicators II

$$A \stackrel{\text{ref}}{\preceq} B \Leftrightarrow I(A, R) \leq I(B, R)$$

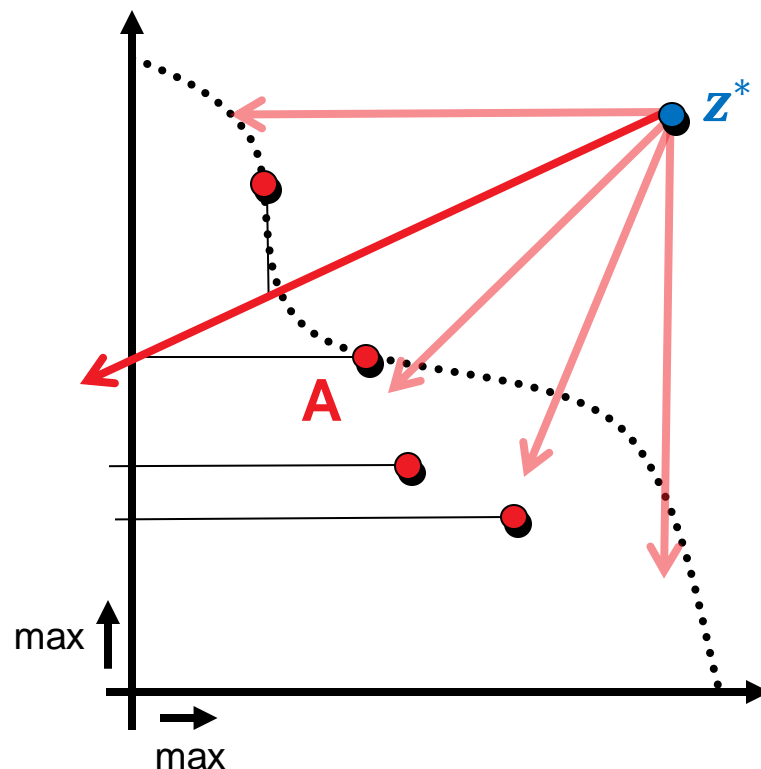
$I(A, R)$  = how much needs A to be moved to weakly dominate R



unary epsilon indicator

$$A \stackrel{\text{ref}}{\preceq} B \Leftrightarrow I(A) \leq I(B)$$

$$I(A) = \frac{1}{|\Lambda|} \sum_{\lambda \in \Lambda} \min_{a \in A} \left( \max_{j=1..m} \lambda_j |z_j^* - a_j| \right)$$



unary R2 indicator

# bbob-biobj Testbed

- 55 functions by combining 2 bbob functions

1 Separable Functions	
f1	<input type="checkbox"/> Sphere Function ✓
f2	<input type="checkbox"/> Ellipsoidal Function ✓
f3	<input type="checkbox"/> Rastrigin Function
f4	<input type="checkbox"/> Büche-Rastrigin Function
f5	<input type="checkbox"/> Linear Slope
2 Functions with low or moderate conditioning	
f6	<input type="checkbox"/> Attractive Sector Function ✓
f7	<input type="checkbox"/> Step Ellipsoidal Function
f8	<input type="checkbox"/> Rosenbrock Function, original ✓
f9	<input type="checkbox"/> Rosenbrock Function, rotated
3 Functions with high conditioning and unimodal	
f10	<input type="checkbox"/> Ellipsoidal Function
f11	<input type="checkbox"/> Discus Function
f12	<input type="checkbox"/> Bent Cigar Function
f13	<input type="checkbox"/> Sharp Ridge Function ✓
f14	<input type="checkbox"/> Different Powers Function ✓

4 Multi-modal functions with adequate global structure	
f15	<input type="checkbox"/> Rastrigin Function ✓
f16	<input type="checkbox"/> Weierstrass Function
f17	<input type="checkbox"/> Schaffers F7 Function ✓
f18	<input type="checkbox"/> Schaffers F7 Functions, moderately ill-conditioned
f19	<input type="checkbox"/> Composite Griewank-Rosenbrock Function F8F2
5 Multi-modal functions with weak global structure	
f20	<input type="checkbox"/> Schwefel Function ✓
f21	<input type="checkbox"/> Gallagher's Gaussian 101-me Peaks Function ✓
f22	<input type="checkbox"/> Gallagher's Gaussian 21-hi Peaks Function
f23	<input type="checkbox"/> Katsuura Function
f24	<input type="checkbox"/> Lunacek bi-Rastrigin Function

# bbob-biobj Testbed

- 55 functions by combining 2 bbob functions

1 Separable Functions		4 Multi-modal functions with adequate global structure									
f1	<input checked="" type="checkbox"/> Sphere Function ✓	f15	<input checked="" type="checkbox"/> Rastrigin Function ✓								
f2	<input checked="" type="checkbox"/> Ellipsoidal Function ✓	f16	<input type="checkbox"/> Weierstrass Function								
f3	<input type="checkbox"/> Rastrigin Function	f17	<input checked="" type="checkbox"/> Schaffers F7 Function ✓								
f4	<input type="checkbox"/> Büche-Rastrigin Function										
f5	<input type="checkbox"/> Linear Slope										
2 Functions with low or moderate conditioning											
f6	<input checked="" type="checkbox"/> Attractive Sector Function ✓										
f7	<input type="checkbox"/> Step Ellipsoidal Function										
f8	<input checked="" type="checkbox"/> Rosenbrock Function, original ✓										
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f11	<input type="checkbox"/> Discus Function										
f12	<input type="checkbox"/> Bent Cigar Function										
f13	<input checked="" type="checkbox"/> Sharp Ridge Function ✓										
f14	<input checked="" type="checkbox"/> Different Powers Function ✓										

	$f_1$	$f_2$	$f_6$	$f_8$	$f_{13}$	$f_{14}$	$f_{15}$	$f_{17}$	$f_{20}$	$f_{21}$
$f_1$	<a href="#">f1</a>	<a href="#">f2</a>	<a href="#">f3</a>	<a href="#">f4</a>	<a href="#">f5</a>	<a href="#">f6</a>	<a href="#">f7</a>	<a href="#">f8</a>	<a href="#">f9</a>	<a href="#">f10</a>
$f_2$		<a href="#">f11</a>	<a href="#">f12</a>	<a href="#">f13</a>	<a href="#">f14</a>	<a href="#">f15</a>	<a href="#">f16</a>	<a href="#">f17</a>	<a href="#">f18</a>	<a href="#">f19</a>
$f_6$			<a href="#">f20</a>	<a href="#">f21</a>	<a href="#">f22</a>	<a href="#">f23</a>	<a href="#">f24</a>	<a href="#">f25</a>	<a href="#">f26</a>	<a href="#">f27</a>
$f_8$				<a href="#">f28</a>	<a href="#">f29</a>	<a href="#">f30</a>	<a href="#">f31</a>	<a href="#">f32</a>	<a href="#">f33</a>	<a href="#">f34</a>
$f_{13}$					<a href="#">f35</a>	<a href="#">f36</a>	<a href="#">f37</a>	<a href="#">f38</a>	<a href="#">f39</a>	<a href="#">f40</a>
$f_{14}$						<a href="#">f41</a>	<a href="#">f42</a>	<a href="#">f43</a>	<a href="#">f44</a>	<a href="#">f45</a>
$f_{15}$							<a href="#">f46</a>	<a href="#">f47</a>	<a href="#">f48</a>	<a href="#">f49</a>
$f_{17}$								<a href="#">f50</a>	<a href="#">f51</a>	<a href="#">f52</a>
$f_{20}$									<a href="#">f53</a>	<a href="#">f54</a>
$f_{21}$										<a href="#">f55</a>

# bbob-biobj Testbed

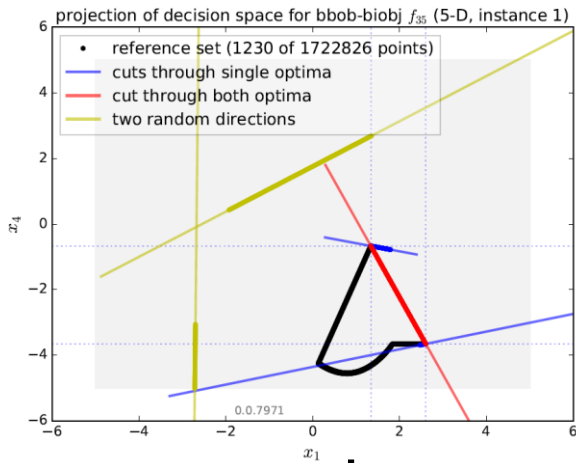
- **55 functions** by combining 2 **bbob** functions
- **15 function groups** with 3-4 functions each
  - separable – separable, separable – moderate, separable - ill-conditioned, ...
- **6 dimensions**: 2, 3, 5, 10, 20, (40 optional)
- instances derived from **bbob** instances:
- **no normalization** (algo has to cope with different orders of magnitude)
- for performance assessment: **ideal/nadir points known**

# bbob-biobj Testbed (cont'd)

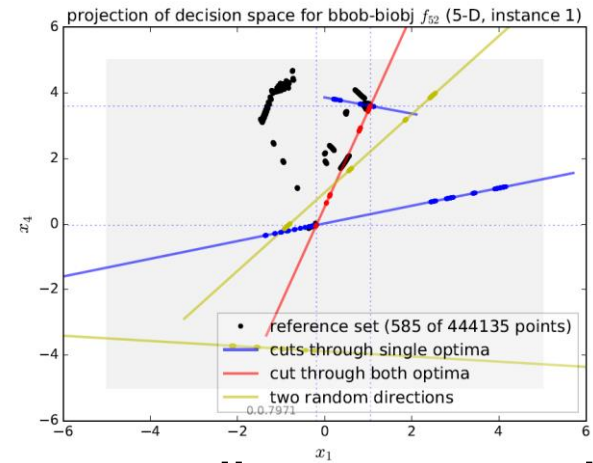
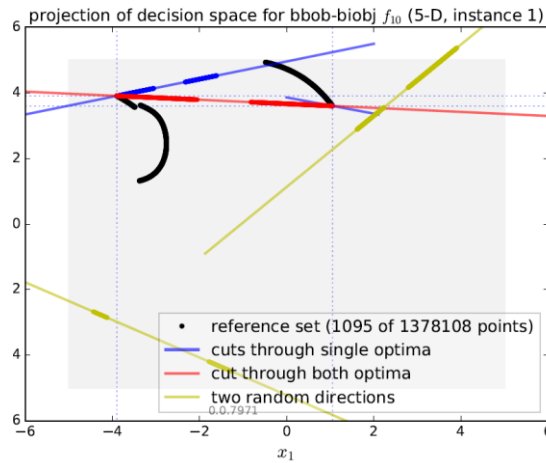
- Pareto set and Pareto front **unknown**
  - but we have a good idea of where they are by running quite some algorithms and keeping track of all non-dominated points found so far
- Various types of shapes

# bbob-biobj Testbed (cont'd)

search space

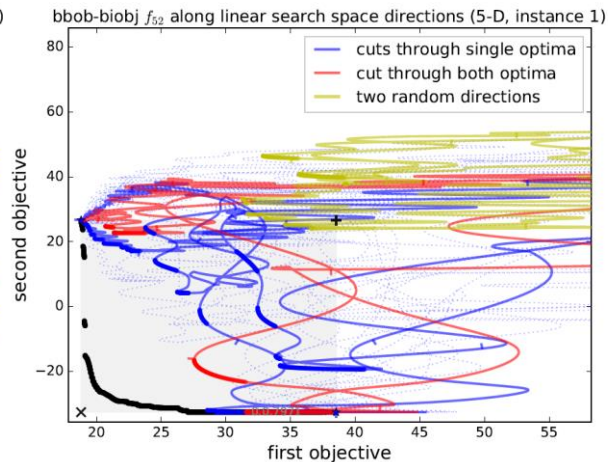
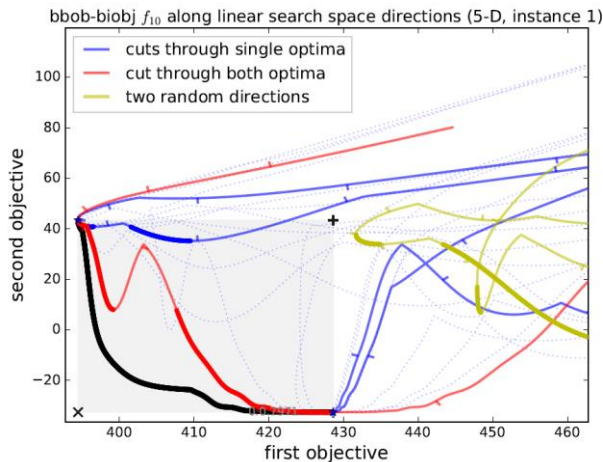
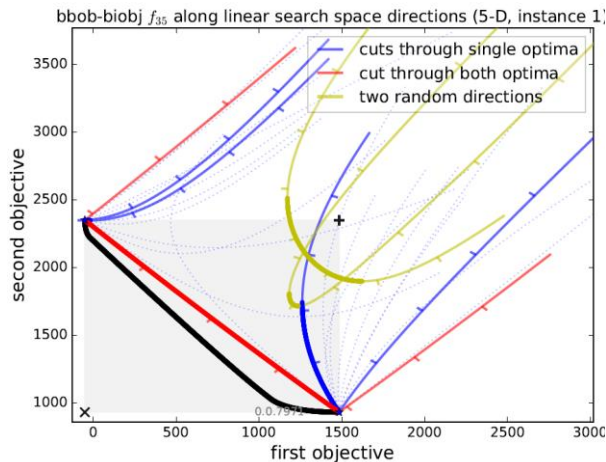


connected  
uni-modal



disconnected  
multi-modal

objective space



# Bi-objective Performance Assessment

algorithm quality =

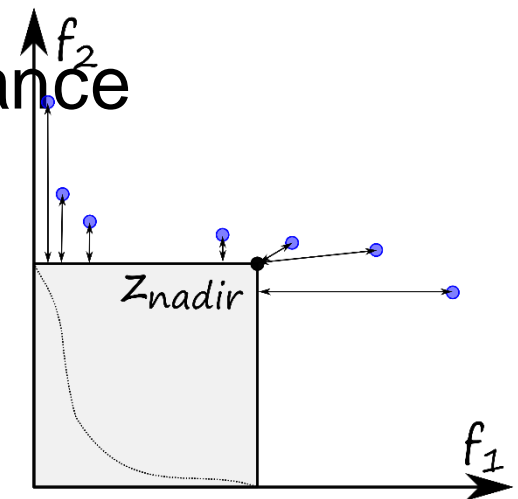
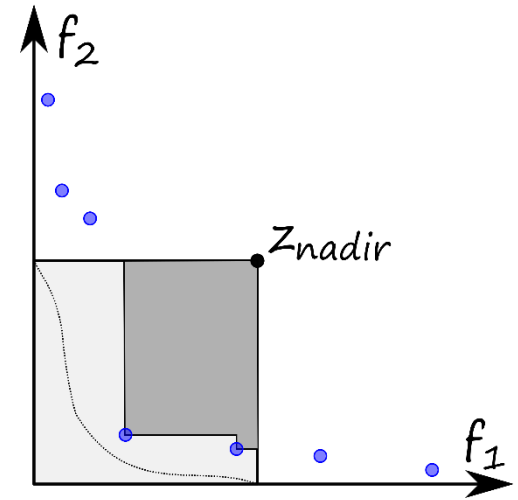
normalized\* hypervolume (HV)  
of all non-dominated solutions

*if a point dominates nadir*

closest normalized\* negative distance  
to region of interest  $[0,1]^2$

*if no point dominates nadir*

\* such that ideal= $[0,0]$  and nadir= $[1,1]$



# Bi-objective Performance Assessment

We measure runtimes to reach (HV indicator) targets:

- relative to a **reference set**, given as the best Pareto front approximation known (since exact Pareto set not known)
- actual **absolute hypervolume targets** used are

$HV(\text{refset}) - \text{targetprecision}$

with 58 **fixed** targetprecisions between +1 and  $-10^{-4}$  (same for all functions, dimensions, and instances) in the displays



# Course Overview

1	Mon, 18.9.2017 Tue, 19.9.2017	first lecture groups defined via wiki everybody went (actively!) through the Getting Started part of <a href="https://github.com/numbbo/coco">github.com/numbbo/coco</a>
2	Wed, 20.9.2017	② today's lecture "Benchmarking", ① final adjustments of groups everybody can run and postprocess the example experiment (③ ~1h for final questions/help during the lecture)
3	Fri, 22.9.2017	lecture "Introduction to Continuous Optimization"
4	Fri, 29.9.2017	lecture "Gradient-Based Algorithms"
5	Fri, 6.10.2017	lecture "Stochastic Algorithms and DFO"
6	Fri, 13.10.2017	lecture "Discrete Optimization I: graphs, greedy algos, dyn. progr." deadline for submitting data sets
	Wed, 18.10.2017	deadline for paper submission
7	Fri, 20.10.2017	final lecture "Discrete Optimization II: dyn. progr., B&B, heuristics"
	Thu, 26.10.2017 / Fri, 27.10.2017	oral presentations (individual time slots)
	after 30.10.2017	vacation aka learning for the exams
	Fri, 10.11.2017	written exam

All deadlines:  
23:59pm Paris time

# Conclusions Benchmarking Continuous Optimizers

I hope it became clear...

...what are the **important issues** in algorithm benchmarking

...which **functionality** is behind the **COCO platform**

...and **how to measure performance** in particular

...what are the basics of **multiobjective optimization**

...and what are the next important steps to do:

**read the assigned paper** and **implement** the algorithm

document everything on the wiki

**run COCO experiment** with your algorithm and **share your data** until Friday 13<sup>th</sup> of October, 2017

And now...

...time for your questions and problems  
around COCO