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Comparison of the MATSuMoTo Library for Expensive Optimization on the Noiseless Black-Box Optimization Benchmarking Testbed

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Abstract-Numerical black-box optimization problems occur frequently in engineering design, medical applications, finance, and many other areas of our society's interest. Often, those problems have expensive-to-calculate objective functions for example if the solution evaluation is based on numerical simulations. Starting with the seminal paper of Jones et al. on Efficient Global Optimization (EGO), several algorithms tailored towards expensive numerical black-box problems have been proposed. The recent MATLAB toolbox MATSuMoTo (short for MATLAB Surrogate Model Toolbox) is the focus of this paper and is benchmarked within the Black-box Optimization Benchmarking framework BBOB. A comparison with other already previously benchmarked algorithms for expensive numerical black-box optimization with the default setting of MATSuMoTo highlights the strengths and weaknesses of MATSuMoTo's cubic radial basis functions surrogate model in combination with a Latin Hypercube initial design in the range of 50 times dimension many function evaluations.

I. INTRODUCTION

Numerical black-box optimization problems, i.e., problems with continuous variables but without the availability of derivatives, have to be solved frequently in many businesses these days. The number of available function evaluations is thereby often restricted to about 10 to 1000 times the search space dimension DIM (*expensive setting*) as a typical evaluation of the objective function can take several minutes or even hours of (already parallelized) computation time.

A state-of-the-art approach to tackle expensive optimization problems is to build a so-called surrogate model of the objective function (based on already evaluated search points) and to use this easier-to-evaluate surrogate model to predict good candidate solutions. Several surrogate-assisted (or modelbased) algorithms for expensive numerical black-box optimization problems exist which mainly differ in the type of the underlying model of the objective function (local vs. global,

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quadratic model, Kriging, radial basis functions, etc.) and the way this model is used for optimization (for example wrt. the criterion for selecting candidate solutions). The criterion for choosing new candidate solutions (to be evaluated on the true, expensive objective function) is known under different names such as "figure of merit" or "infill criterion".

The probably most known approach to expensive numerical black-box optimization is the *Efficient Global Optimization* algorithm (EGO) from the seminal paper by Jones et al. [1]. Here, multivariate *Gaussian processes* are used as surrogate models and the *expected improvement* as infill criterion.

The recently proposed SMAC-BBOB [2] is a similar approach to EGO and uses the same surrogate models and infill criterion as EGO. In comparison to EGO, however, SMAC-BBOB uses the specific "noise-free isotropic Matern kernel and no initial design" [2]. Furthermore, the optimization algorithms DIRECT and CMA-ES are used to optimize the expected improvement criterion instead of the branch-and-bound approach of the original EGO.

A local meta-model based version of the CMA-ES algorithm itself, denoted by lmm-CMA-ES, has been proposed by Kern et al. [3] and was later slightly improved [4]. As its original version CMA-ES, it samples in each iteration λ candidate solutions from a multivariate normal distribution which itself is updated based on the ranking of the candidate solutions' objective function values. In the lmm-CMA-ES, a local quadratic surrogate model is build around each candidate solution to predict a ranking. Iteratively, only a small portion of the candidate solutions is then evaluated on the true objective function until the (updated) ranking does not change anymore.

Another variant of the original CMA-ES algorithm which uses surrogates is the so-called IPOPsaACM algorithm [5]. On top of a variant of CMA-ES that uses a ranking support vector machine as surrogate model, the IPOPsaACM proposes a heuristic that adapts both the number of function evaluations, within which the surrogate model is kept constant, and the surrogate's model parameters itself.

Last, let us mention the algorithm NEWUOA by Powell [6], [7] which is not specifically designed for solving expensive optimization problems but also builds a (global) quadratic model of the objective function in each iteration and, thus, should be considered as a baseline in each comparison of

Erratum: The statement "MATSuMoTo often scales linearly or quadratically with the problem dimension for solved problems while the expected running time for RANDOMSEARCH explodes exponentially." in the original paper was wrong and has now been replaced by "For the solved problems, MATSuMoTo often scales linearly or quadratically relative to the best algorithm of BBOB 2009 while the expected running time for RANDOMSEARCH always explodes exponentially."

optimizers for expensive numerical black-box optimization problems. Instead of using quadratically many solutions to fit the quadratic surrogate model of NEWUOA, typically only linearly many solutions are used to define the surrogate. Minimizing the Frobenius norm of the second derivative matrix of the model changes in each iteration then makes up for the remaining freedom of the quadratic model.

In order to find out which of the many available optimization algorithms performs best on certain classes of functions, benchmarking in terms of numerical experiments is the compulsory path to assess performance of optimizers quantitatively and to understand weaknesses and strengths of each algorithm. To facilitate this tedious task, the Comparing Continuous Optimizers platform (COCO) has been developed and used to create the Black-box Optimization Benchmarking (BBOB) test suite [8]. It provides all necessary code for running the experiments on 24 well-known and -understood noiseless test functions, the collection of data, up to the automated postprocessing of them-including the generation of data profiles, scaling graphs, and tables. In the beginning of 2015, around 120 different algorithms have been benchmarked with the COCO/BBOB framework and the corresponding data sets are available online at http://coco.gforge.inria.fr/. However, the data collection is by far not exhaustive and in particular in the expensive setting (between $10 \cdot \text{DIM}$ and $1000 \cdot \text{DIM}$ function evaluations) does not cover many different algorithm classes.

Our Contributions: This paper will, therefore, benchmark a recently proposed approach to expensive optimization, the MATLAB Surrogate Model Toolbox (MATSuMoTo) [9], [10], and compare its performance on the BBOB noiseless testbed with other above mentioned algorithms. The MATSuMoTo library allows to choose from a variety of different initial designs, surrogate models, and criteria for the choice of new candidate solutions and a previous benchmarking of the available variants has established a default setting which is based on cubic radial basis functions (RBFs) as surrogate models [10]. Since cubic RBFs have not been used as surrogates in any algorithm previously compared on the expensive BBOB testbed, we turn our attention here to the comparison of this default setting of MATSuMoTo with other previously benchmarked algorithms for expensive optimization.

II. THE MATSUMOTO LIBRARY AND THE BENCHMARKED DEFAULT ALGORITHM SETTING

The MATLAB Surrogate Model Toolbox (MATSuMoTo) is an optimization toolbox for "computationally expensive, black-box, global optimization problems that may have continuous, mixed-integer, or pure integer variables" [9]. Various surrogate models, initial experimental design strategies and infill criteria are available. Also mixtures of surrogate models as employed and compared in [10] can be used. We here restrict ourselves to the continuous optimization part of the toolbox.

Several parameters have to be specified by the user when using MATSuMoTo, concretely the optimization problem, the maximum number of allowed expensive function evaluations, the surrogate model type, the sampling strategy, the type of the initial experimental design, the number of points in the initial experimental design, and the number of points to be selected in each iteration for the expensive function evaluations. Optionally, specific points to be included in the initial experimental design can be specified. As the default setting of MATSuMoTo will be chosen by most new users of the toolbox as a starting point, we compare this default setting as a baseline version of MATSuMoTo within the BBOB framework. The default setting has been chosen based on a previous extensive comparison of all of MATSuMoTo's components. The default setting of MATSuMoTo corresponds to using cubic radial basis functions as surrogate model, randomized sampling by local perturbation of the best point found so far together with additional points uniformly selected from the whole variable domain as sampling strategy, a Latin Hypercube sampling as initial experimental design with $2 \cdot (DIM + 1)$ samples, and one new sample per iteration. Only the stopping criterion was set differently than the default, namely to $50 \cdot \text{DIM}$ instead of $20 \cdot \text{DIM}.$

Slight modifications had to be done to the original MAT-SuMoTo code to be able to connect it to the BBOB framework. The main change is that no parallel evaluations are performed anymore via MATLAB's Parallel Computing toolbox but instead the natural parallel evaluations of BBOB are used. As basis for our experiments, the online available MATSuMoTo version of April, 8, 2014 has been used. The source code for the BBOB experiments will be available via http://coco.gforge. inria.fr/doku.php?id=cec-bbob-2015-results.

III. EXPERIMENTAL SETTING

A. Compared Algorithms

Besides the above described default setting of MAT-SuMoTo, several algorithm data sets from the COCO/BBOB web page have been included in the comparison: NEWUOA [7], SMAC-BBOB [2], lmm-CMA-ES [4], IPOPsaACM [5] and pure random search [11]. The default MATSuMoTo optimizer has been run for $50 \cdot \text{DIM}$ function evaluations.

B. CPU Timing of the Default MATSuMoTo

In order to evaluate the CPU timing of the MATSuMoTo library, we have run the algorithm with default settings on the function f_8 with restarts for at least 30 seconds and until a maximum budget equal to $50 \cdot \text{DIM}$ is reached. The code was run on an Intel(R) Core(TM)2 Quad Q6600 CPU @ 2.40GHz with 1 processor and 4 cores. The time per function evaluation for dimensions 2, 3, 5, 10, and 20 equals 0.058, 0.12, 0.26, 0.89, and 2.9 seconds respectively.

C. BBOB-related Settings

Results from experiments according to [8] on the functions given in [12] are presented in Figures 1, 2 and 3 and in Tables I and II. The **expected running time (ERT)** therein depends on a given target function value, $f_t = f_{opt} + \Delta f$, and is computed over all relevant trials as the number of function evaluations executed during each trial while the best function value did not

reach f_t , summed over all trials and divided by the number of trials that actually reached f_t [8], [13]. **Statistical significance** is tested with the rank-sum test for a given target Δf_t using, for each trial, either the number of needed function evaluations to reach Δf_t (inverted and multiplied by -1), or, if the target was not reached, the best Δf -value achieved, measured only up to the smallest number of overall function evaluations for any unsuccessful trial under consideration.

IV. DISCUSSION OF THE RESULTS

When looking at the benchmarking results in Figs. 1, 2, and 3 and in Tables I and II, four main observations can be made:

Scaling with Dimension: Over all problems, MATSuMoTo ranges in performance between RANDOMSEARCH and the other surrogate model based algorithms when looking at the expensive scenario of $10 \cdot$ DIM function evaluations (Fig. 1). For the solved problems, MATSuMoTo often scales linearly or quadratically relative to the best algorithm of BBOB 2009 while the expected running time for RANDOMSEARCH always explodes exponentially.

Solvable Instances: In 20-D (5-D), MATSuMoTo does not solve nine (three) of the 24 noiseless BBOB functions to the precision of the BBOB-2009 reference algorithm after 10·DIM function evaluations. Surprisingly, the sphere function cannot be solved to a precision of 10^{-8} within $50 \cdot$ DIM evaluations—not even in 2-D. The only algorithms in the comparison for which this is also the case in 5-D and 20-D, are RANDOMSEARCH and SMAC-BBOB. Preliminary experiments with other MATSuMoTo settings show similar results but a thorough investigation remains future work.

Strong Performances of MATSuMoTo: The best relative performances of MATSuMoTo can be observed on the functions f_{15} (Rastrigin) and f_{21} (Gallagher's 101 Peaks) in 5-D and on f_{21} and f_{22} (Gallagher's 21 Peaks) in 20-D—providing the best performances among the compared algorithms. For the 20-D functions f_{21} and f_{22} and the largest expensive budget of 50 · DIM, MATSuMoTo is even outperforming the best algorithm of BBOB-2009. For smaller budgets than 50 · DIM and in 5-D, also the results on f_2 , f_6 , and f_{16} are competitive and MATSuMoTo sometimes outperforms the best BBOB-2009 algorithm. None of the results is statistically significant.

Overall Comparison with Other Surrogate-Assisted Optimizers: When compared on the data profiles of Fig. 2 and 3, it appears that the default MATSuMoTo optimizer is always dominated by some other algorithm. Moreover, the combination of the three algorithms SMAC-BBOB (for very low budgets below $\approx 3 \cdot$ DIM function evaluations), NEWUOA (for medium budgets), and lmm-CMA-ES (for relatively large budgets of $\geq 30 \cdot$ DIM evaluations) build a good portfolio that constructs the upper envelope over all compared algorithms for almost all problem groups. Adding IPOPsaACM to the portfolio further improves performance slightly on the moderate function group for the most difficult targets.

V. CONCLUSIONS

The MATLAB Surrogate Model Toolbox (MATSuMoTo) has been taken out-of-the-box in its default setting and was compared with other model-building algorithms of the available BBOB algorithm data collection on the 24 noiseless test functions of the BBOB suite. It turns out that MATSuMoTo shows comparable results over most functions: though in dimension 20, nine functions cannot be solved to comparatively high precision, on the two Gallagher functions (f_{21} and f_{22}), the best BBOB-2009 algorithm is outperformed for the largest expensive budgets (all results not statistically significant).

Overall, MATSuMoTo is a practically interesting optimization toolbox due to its flexibility and availability in MATLAB. However, other available algorithms that outperform its default setting exist and it remains open to investigate more carefully the impact of the other options offered by the framework on the BBOB test suite, similar to the comparison in [10]. In particular, the influence of the initial design, the used surrogate model and the employed infill criterion in surrogate-assisted optimization algorithms should be investigated further.

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Fig. 1. Expected running time (ERT in number of f-evaluations as \log_{10} value) divided by dimension versus dimension. The target function value is chosen such that the bestGECCO2009 artificial algorithm just failed to achieve an ERT of $10 \times \text{DIM}$. Different symbols correspond to different algorithms given in the legend of f_1 and f_{24} . Light symbols give the maximum number of function evaluations from the longest trial divided by dimension. Black stars indicate a statistically better result compared to all other algorithms with p < 0.01 and Bonferroni correction number of dimensions (six). Legend: o:MATSuMoToDefault-50D, \diamond :RANDOMSEARCH, \star :NEWUOA, \bigtriangledown :Imm-CMA, \bigcirc :SMAC, \triangle :IPOPsaACM



Fig. 2. Bootstrapped empirical cumulative distribution of the number of objective function evaluations divided by dimension (FEvals/DIM) for all functions and subgroups in 5-D. The targets are chosen from $10^{[-8..2]}$ such that the bestGECCO2009 artificial algorithm just not reached them within a given budget of $k \times \text{DIM}$, with $k \in \{0.5, 1.2, 3, 10, 50\}$. The "best 2009" line corresponds to the best ERT observed during BBOB 2009 for each selected target.



Fig. 3. Bootstrapped empirical cumulative distribution of the number of objective function evaluations divided by dimension (FEvals/DIM) for all functions and subgroups in 20-D. The targets are chosen from $10^{[-8..2]}$ such that the bestGECCO2009 artificial algorithm just not reached them within a given budget of $k \times \text{DIM}$, with $k \in \{0.5, 1.2, 3, 10, 50\}$. The "best 2009" line corresponds to the best ERT observed during BBOB 2009 for each selected target.

| #FES/D | 0.5 | 1.2 | 3 | 10 | 50 | #succ | #FEs/D | 0.5 | 1.2 | 3 | 10 | 50 | #succ |
|--|---|--|---|--|--|--|---|--|---|--|--|--|--|
| f1 | 2.5e+1:4.8 | 1.6e+1:7.6 | 1.0e-8:12 | 1.0e-8:12 | 1.0e-8:12 | 15/15 | f13 | 1.0e+3:2.8 | 6.3e+2:8.4 | 4.0e+2:17 | 6.3e+1:52 | 6.3e-2:264 | 15/15 |
| RANDOM | 1.8(1) | 2.5(3) | ~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~ | 80 | ∞ 5e6 | 0/15 | RANDOM | 2.0(2) | 1.8(0.9) | 1.5(0.7) | 1.7(0.5) | ∞ 250 ∞ 5¢6 | 0/15 |
| NEWLIOA | 1.9(1) | 13(07) | 1(0.1)*4 | 100*4 | 1(0.1)*4 | 15/15 | NEWUOA | 2.6(2) | 4.5(0.2) | 1(0.3) | 3.3(8) | 43(30) | 15/15 |
| lmm-CMA | 1.2(2) | 1.5(1) | 9.1(0.7) | 9,1(0,5) | 9.1(0.5) | 15/15 | lmm-CMA | 1.4(2) | 1.6(2) | 1.7(0.9) | 1.8(0.3) | 1.6(0.4) | 15/15 |
| SMAC | 0.79(0.5) | 0.84(0.3) | ~ | ~ | ∞ 500 [°] | 0/15 | SMAC | 1 (1) | 1.1(1) | 0.96 (0.5) | 1.1 (0.4) | ∞ 500 | 0/15 |
| IPOPsaACM | 3.1(3) | 2.9(1) | 19(1) | 19(1) | 19(1) | 15/15 | IPOPsaACM | 5.1(5) | 4.1(4) | 3.2(2) | 2.2(0.5) | 1.2(0.3) | 15/15 |
| #FEs/D | 0.5 | 1.2 | 3 | 10 | 50 | #succ | #FEs/D | 0.5 | 1.2 | 3 | 10 | 50 | #succ |
| 12 MATSuMo | 1.6e+6:2.9 | 4.0e+5:11 | 4.0e+4:15 | 6.3e+2:58 | 1.0e-8:95 | 0/15 | 114 MATSuMo | 21(0.9) | 1.0e+1:10 1.4(0.6) | 0.3e+0:15 1 3(0 4) | 2.5e-1:55 | 1.0e-5:251 | 0/15 |
| RANDOM | 1.0(1) 1.0(0.5) | 1(1) | 13(6) | 3591(5042) | ∞ 5e6 | 0/15 | RANDOM | 2.2(2) | 1.2(2) | 1.6(2) | 6945(8521) | ∞ 5e6 | 0/15 |
| NEWUOA | 3.2(2) | 1.0(0.5) | 1(0.2) | $1(0.3)^{*2}$ | 276(232) | 15/15 | NEWUOA | 3.3(3) | 1.7(0.7) | 1.3(0.4) | $1(0.2)^{*2}$ | 5.5(2) | 15/15 |
| lmm-CMA | 1.6(3) | 0.83(0.9) | 2.4(2) | 2.5(0.6) | 5.5(1) | 15/15 | lmm-CMA | 1.1(1) | 0.62(0.7) | 0.81(0.8) | 1.6(0.2) | 1.8(0.2) | 15/15 |
| SMAC | 1.0(0.9) | 0.74(0.5) | 1.7(1) | 8.0(10) | ∞ <i>500</i> | 0/15 | SMAC | 1.2(1) | 0.62 (0.7) | 0.76 (0.7) | 4.9(2) | ∞ 500 | 0/15 |
| IPOPsaACM | 2.7(2) | 1.8(3) | 4.8(4) | 3.5(0.5) | 5.5(0.9) | 15/15 | IPOPsaACM | 4.4(3) | 2.8(2) | 2.4(2) | 2.5(0.3) | 1.8(0.2) | 15/15 |
| #FEs/D | 0.5 | 1.2 | 3 | 10 | 50 | #succ | #FES/D | 0.5 | 1.2 | 6 3 1 1 24 | 10 | 50 1.6a + 1-280 | #succ |
| 13 MATSuMo | 1.00+2:4.1 | 1.0e+2:15 | 0.3e+1:23 | 2.50+1:15 | 1.0e+1:/16 | 4/15 | MATSuMo | 2.4(2) | 1.3(0.3) | 1.6(0.6) | 1.7(0.7) | 0.97(0.5) | 10/15 |
| RANDOM | 1(1) | 2.1(2) | 17(15) | 416(462) | 6763(8580) | 10/15 | RANDOM | 3.4(11) | 1.7(2) | 10(9) | 49(35) | 1083(902) | 15/15 |
| NEWUOA | 3.0(2) | 1.5(1) | 4.1(4) | 16(13) | 6.1(8) | 15/15 | NEWUOA | 10(1) | 7.8(12) | 7.3(10) | 5.3(7) | 5.9(2) | 15/15 |
| lmm-CMA | 1.4(1) | 0.92(0.7) | 1.4 (1) | 2.4 (2) | 0.45 (0.0) | 15/15 | lmm-CMA | 1.3(2) | 1.3(0.9) | 1.5(0.7) | 1.6(1.0) | 1.4(2) | 15/15 |
| SMAC | 0.73(1) | 0.74(0.7) | 2.6(4) | 4.4(4) | 5.1(4) | 2/15 | SMAC IDOD ACM | 1.1 (0.8) | 0.83(0.6) | 1.6(1) | 2.2(1) | 8.1(8) | 3/15 |
| #FEs/D | 2.4(2) | 1.8(2) | 2.2(1) | 3.5(2) | 1.1(0.9) | 15/15 #succ | #FEs/D | 4.2(4) | 1.8(2) | 1.7(1) | 1.8(0.8) | 1.9(2) 50 | 15/15 #succ |
| f4 | 2.5e+2:2.6 | 1.6e+2:10 | 1.0e+2:19 | 4.0e+1:65 | 1.6e+1:434 | 115/15 | f16 | 4.0e+1:4.8 | 2.5e+1:16 | 1.6e+1:46 | 1.0e+1:120 | 4.0e+0:334 | 15/15 |
| MATSuMo | 2.6(2) | 1.1(1) | 2.9(2) | 3.0(3) | 9.0(11) | 1/15 | MATSuMo | 1.4(2) | 0.86(0.8) | 1.2(1) | 1.2(0.8) | 3.9(5) | 3/15 |
| RANDOM | 2.3(4) | 1.8(2) | 3.4(2) | 148(122) | 4682(2688) | 13/15 | RANDOM | 1.6(0.9) | 1.5(0.6) | 1.9(2) | 3.5(5) | 19(17) | 15/15 |
| NEWUOA | 19(2) | 20(36) | 27(28) | 52(48) | 21(28) | 15/15 | NEWUOA | 2.2(2) | 1.3(1) | 3.8(8) | 2.1(5) | 7.1(10) | 15/15 |
| Imm-CMA | 0.51(0.4) | 0.79(1) | 0.93(1) | 2.2(0.7) | 1.3(1) | 15/15 | Imm-CMA | 1.7(0.8) | 1.8(2) | 2.7(2) | 2.0(1) | 1.3(2) | 15/15 |
| IPOPsaACM | 4.1(3) | 2.1(2) | 2.5(1) | 4.3(5) | 1.3(1) | 15/15 | IPOPsaACM | 1.6(4) | 1.7(1) | 2.7(2) | 3.1(2) | 1.9(3) | 15/15 |
| #FEs/D | 0.5 | 1.2 | 3 | 10 | 50 | #succ | #FEs/D | 0.5 | 1.2 | 3 | 10 | 50 | #succ |
| f5 | 6.3e+1:4.0 | 4.0e+1:10 | 1.0e-8:10 | 1.0e-8:10 | 1.0e-8:10 | 15/15 | f17 | 1.0e+1:5.2 | 6.3e+0:26 | 4.0e+0:57 | 2.5e+0:110 | 6.3e-1:412 | 15/15 |
| MATSuMo | 1.6(0.8) | 1.2(0.3) | 1.9(0.3) | 1.9(0.6) | 1.9(0.5) | 15/15 | MATSuMo | 3.1(3) | 1.2(1) | 1.1(1.0) | 1.9(0.8) | 9.2(10) | 1/15 |
| KANDOM | 2.1(3) | 3.8(5) | ∞ 1.5(0.2) | ∞ 1.5(0.4) | ∞ 5e6 1.5(0.4) | 0/15 | KANDOM NEWUOA | P.0(10) | 3.3(3) 1.6(0.5) | 7 2(8) | 32(33) 8 8(15) | ∠514(947) 30(57) | 13/15 |
| Imm_CMA | 2.5(0.1) | 1.1(0.1) | 5.0(2) | 5.0(0.9) | 5.0(2) | 15/15 | lmm-CMA | 1.7(1) | 0.91(0.7) | 0.70(0.3) | 0.55(0.2) | 0.62(1) | 15/15 |
| SMAC | 13(02) | 0.63(0.1)* | 095(01)*4 | 095(01)*4 | 095(01)*4 | 15/15 | SMAC | 2.5(2) | 1.6(2) | 1.9(2) | 2.1(3) | 2.5(3) | 6/15 |
| IPOPsaACM | 2.4(2) | 1.8(2) | 6.3(3) | 6.3(3) | 6.3(2) | 15/15 | IPOPsaACM | 4.9(4) | 1.9(1.0) | 1.4(0.6) | 1.0(0.3) | 1.1(0.3) | 15/15 |
| #FEs/D | 0.5 | 1.2 | 3 | 10 | 50 | #succ | #FEs/D | 0.5 | 1.2 | 3 | 10 | 50 | #succ |
| f6 | 1.0e+5:3.0 | 2.5e+4:8.4 | 1.0e+2:16 | 2.5e+1:54 | 2.5e-1:254 | 15/15 | 118 MATSuMo | 0.3e+1:3.4 | 4.0e+1:7.2 | 2.5e+1:20 | 1.6e+1:58 0.85(0.5) | 1.6e+0:318 | 0/15 |
| MATSuMo | 1.3(1) | 0.90 (0.7) | 1.7(2) | 12(14) | ∞ 250 5 | 0/15 | RANDOM | 1(2) | 3.3(4) | 1.7(3) | 6.3(6) | 1.7e4(2e4) | 9/15 |
| NEWLIOA | 5.5(2) 2.9(2) | 5.1(9) | 4/5(1582) | 203(610) | ∞ <i>320</i> | 15/15 | NEWUOA | 3.3(2) | 4.6(10) | 10(19) | 10(9) | 376(659) | 11/15 |
| lmm-CMA | 1.6(2) | 1.4(1) | 4.7(2) | 3.8(4) | 4.5(3) | 15/15 | lmm-CMA | 1.3(1) | 1.6(1) | 0.92 (0.9) | 0.73 (0.4) | 0.52(0.1)* ² | 15/15 |
| SMAC | 1.4(2) | 1.1(0.9) | 1.5(1) | 1.9(2) | ∞ 500 | 0/15 | SMAC | 1.1(0.4) | 0.85 (0.6) | 0.97(0.4) | 1.1(2) | 11(4) | 2/15 |
| IPOPsaACM | 3.6(4) | 2.2(2) | 58(4) | 3 5(2) | 26(0.0) | 1 | IDOD ACM | (A 2(A) | 2.0(4) | 3 5(7) | 4 2(22) | 1.5(0.4) | 115/15 |
| 11 F F F F | | | 5.0(1) | 515(2) | 2.0(0.9) | 15/15 | IFOFSAACM | H.3(H) | 3.9(4) | 5.5(7) | 4.2(25) | 1.5(0.4) | " |
| #FEs/D | 0.5 | 1.2 | 3 | 10 | 50 | #succ | #FEs/D | 0.5 | 1.2 | 3 | 4.2(23) | 50 2 5 a 2:4046 | #succ |
| #FEs/D f7 MATSuMo | 0.5 1.6e+2:4.2 | 1.2 1.0e+2:6.2 | 3 2.5e+1:20 | 10 4.0e+0:54 7.6(14) | 50 1.0e+0:324 5.4(4) | 15/15 #succ 15/15 2/15 | #FEs/D f19 MATSuMo | 0.5 1.6e-1:172 | 1.2 1.0e-1:242 | 6.3e-2:67: | 4.2(23) 10 5 4.0e-2:307 ∞ | 50 8 2.5e-2:4946 \$\infty 250 | #succ 15/15 |
| #FEs/D f7 MATSuMo RANDOM | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) | 1.2 1.0e+2:6.2 1.8(1) 2.9(0.8) | 3 2.5e+1:20 1.5(0.6) 8.8(6) | 10 4.0e+0:54 7.6(14) 151(135) | 50 1.0e+0:324 5.4(4) 1207(1290) | 15/15 #succ 15/15 2/15 15/15 | #FEs/D f19 MATSuMo RANDOM | 0.5 1.6e-1:172 ∞ 4.2e5(4e5) | 1.2 1.0e-1:242 ∞ | <u>3</u> <u>6.3e-2:67</u> <u>∞</u> ∞ | 4.2(2.5) 10 5 4.0e-2:307 ∞ ∞ | | #succ 15/15 0/15 0/15 |
| #FEs/D f7 MATSuMo RANDOM NEWUOA | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) 2.6(2) | 1.2 1.0e+2:6.2 1.8(1) 2.9(0.8) 2.2(0.2) | 3 2.5e+1:20 1.5(0.6) 8.8(6) 2.2(3) | 10 4.0e+0:54 7.6(14) 151(135) 7.6(13) | <u>50</u> <u>1.0e+0:324</u> 5.4(4) 1207(1290) 13(15) | 15/15 #succ 2/15 15/15 15/15 | #FEs/D #FEs/D f19 MATSuMo RANDOM NEWUOA | $\begin{array}{r} 0.5 \\ \hline 1.6e-1:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \end{array}$ | 1.2 1.0e-1:242 ∞ 1415(1586) | 3.3(7) 3 6.3e-2:67: ∞ 1164(1255) | 4.2(23) 10 5 4.0e-2:307 ∞ 398(447) | $ \frac{50}{50} \frac{50}{8 2.5e-2:4946} $ | #succ 15/15 0/15 0/15 0/15 |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) 2.6(2) 1.2(1) | 1.2 1.0e+2:6.2 1.8(1) 2.9(0.8) 2.2(0.2) 1.3(0.8) | 3 2.5e+1:20 1.5(0.6) 8.8(6) 2.2(3) 1.5 (1) | 10 4.0e+0:54 7.6(14) 151(135) 7.6(13) 2.3(3) | 50 1.0e+0:324 5.4(4) 1207(1290) 13(15) 0.92(2) | 15/15 #succ 15/15 2/15 15/15 15/15 15/15 | #FEs/D f19 MATSuMo RANDOM NEWUOA Imm-CMA | $\begin{array}{r} 0.5 \\ \hline 1.6e-1:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \end{array}$ | 1.2 1.0e-1:242 1415(1586) 56(58) | 3.3(7) 3 6.3e-2:67: ∞ 1164(1255) 30(35) | 4.2(23) 5 $4.0e-2:307\infty398(447)14(13)$ | 50 50 8 2.5e-2:4946 ∞ 250 ∞ 5e6 ∞ 5e5 ∞ 2805 ∞ 60 | #succ 15/15 0/15 0/15 0/15 0/15 |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC ImODec ACM | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) 2.6(2) 1.2(1) 1.3(2) 2.2(2) | 1.2 1.0e+2:6.2 1.8(1) 2.9(0.8) 2.2(0.2) 1.3(0.8) 1.1(0.8) 2.0(2) | 3 2.5e+1:20 1.5(0.6) 8.8(6) 2.2(3) 1.5 (1) 1.5(0.9) 2.4(2) | 10 4.0e+0:54 7.6(14) 151(135) 7.6(13) 2.3(3) 1.6(0.7) 2.2(0.5) | 2.3(0.3) 50 1.0e+0:324 5.4(4) 1207(1290) 13(15) 0.92(2) 0.88(0.4) 1.2(2.2) | 15/15 #succ 2/15 15/15 15/15 15/15 15/15 13/15 | #FEs/D #FEs/D f19 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM | 0.5 1.6e-1:172 ∞ 4.2e5(4e5) 1308(2380) 55(56) ∞ 280(359) | 1.2 1.0e-1:242 1415(1586) 56(58) 250(295) | 3.5.(7) 3 6.3e-2:67: ∞ 1164(1255) 30(35) ∞ 98(104) | $\begin{array}{c} 4.2(23) \\ 10 \\ 5 \\ \infty \\ 398(447) \\ 14(13) \\ \infty \\ 25(21) \end{array}$ | 50 = 50 $50 = 50$ $50 = 50$ $50 = 50$ $50 = 50$ $50 = 50$ $50 = 50$ | #succ 15/15 0/15 0/15 0/15 0/15 0/15 15/15 |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) 2.6(2) 1.2(1) 1.3(2) 3.2(2) 0.5 | 1.2 1.0e+2:6.2 1.8(1) 2.9(0.8) 2.2(0.2) 1.3(0.8) 1.1(0.8) 2.9(2) 1.2 | 3 2.5e+1:20 1.5(0.6) 8.8(6) 2.2(3) 1.5(1) 1.5(0.9) 2.4(2) 3 | 10 4.0e+0:54 7.6(14) 151(135) 7.6(13) 2.3(3) 1.6(0.7) 2.2(0.5) 10 | 50 1.0e+0:324 5.4(4) 1207(1290) 13(15) 0.92(2) 0.88(0.4) 1.2(0.2) 50 | 15/15 #succ 2/15 15/15 15/15 15/15 13/15 15/15 | #Fes/D #Fes/D f19 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D | 0.5 1.6e-1:172 ∞ 4.2e5(4e5) 1308(2380) 55(56) ∞ (280(359) 0.5 | 1.2 1.0e-1:242 1.2 1.2 1.0e-1:242 1415(1586) 56(58) 250(295) 1.2 | 3 6.3e-2:67: | $4.2(25)$ 10 5 4.0e-2:307 ∞ 3998(447) 14(13) ∞ 25(21) 10 | $50 = 50$ $8 = 2.5e \cdot 2:4946$ $\infty = 250$ $\infty = 5e6$ $\infty = 5e5$ $\infty = 2805$ $\infty = 500$ $16(13)$ 50 | #succ 15/15 0/15 0/15 0/15 0/15 0/15 15/15 #succ |
| #FEs/D f7 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f8 | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) 2.6(2) 1.2(1) 1.3(2) 3.2(2) 0.5 1.0e+4:4.6 | 1.2 1.0e+2:6.2 1.8(1) 2.9(0.8) 2.2(0.2) 1.3(0.8) 1.1(0.8) 2.9(2) 1.2 6.3e+3:6.8 | 3 2.5e+1:20 1.5(0.6) 8.8(6) 2.2(3) 1.5(1) 1.5(0.9) 2.4(2) 3 1.0e+3:18 | 10 4.0e+0:54 7.6(14) 151(135) 7.6(13) 2.3(3) 1.6(0.7) 2.2(0.5) 10 6.3e+1:54 | 50 1.0e+0:324 5.4(4) 1207(1290) 13(15) 0.92(2) 0.88(0.4) 1.2(0.2) 50 1.6e+0:258 | 15/15 #succ 15/15 2/15 15/15 15/15 15/15 13/15 15/15 #succ 15/15 | #FEs/D #FEs/D f19 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f20 | $\begin{array}{c} 0.5 \\ \hline 0.6e-l:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 1280(359) \\ 0.5 \\ \hline 6.3e+3:5.1 \end{array}$ | $\begin{array}{c} 1.2 \\ 1.0e{-}1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e{+}3:8.4 \end{array}$ | $3 = \frac{3}{6.3e \cdot 2:67:} \\ \infty \\ 1164(1255) \\ 30(35) \\ \infty \\ 98(104) \\ 3 \\ 4.0e + l:15$ | $\begin{array}{r} 10 \\ 5 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ $ | $50 = 50$ $8 = 2.5e-2:4946$ $\infty 250$ $\infty 5e6$ $\infty 5e5$ $\infty 2805$ $\infty 500$ $16(13)$ 50 $1.0e+0:851$ | #succ #succ 15/15 0/15 0/15 0/15 0/15 0/15 15/15 #succ 15/15 |
| #FEs/D f7 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f8 MATSUMO | $\begin{array}{c} 0.5\\ \hline 1.6e+2:4.2\\ 1.3(1)\\ 2.0(2)\\ 2.6(2)\\ 1.2(1)\\ 1.3(2)\\ 3.2(2)\\ 0.5\\ \hline 1.0e+4:4.6\\ 1.7(2)\\ \end{array}$ | $\begin{array}{c} 1.2\\ 1.0e+2:6.2\\ 1.8(1)\\ 2.9(0.8)\\ 2.2(0.2)\\ 1.3(0.8)\\ 1.1(0.8)\\ 2.9(2)\\ 1.2\\ 6.3e+3:6.8\\ 1.9(1)\\ \end{array}$ | 3 2.5e+1:20 1.5(0.6) 8.8(6) 2.2(3) 1.5(1) 1.5(0.9) 2.4(2) 3 1.0e+3:18 1.4(0.3) | 10 4.0e+0:54 7.6(14) 151(135) 7.6(13) 2.3(3) 1.6(0.7) 2.2(0.5) 10 6.3e+1:54 2.6(1) | $\begin{array}{c} 50\\ \hline 50\\ 1.0e+0:324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.88(0.4)\\ 1.2(0.2)\\ \hline 50\\ \hline 1.6e+0:258\\ \infty 250 \end{array}$ | 15/15 #succ 15/15 15/15 15/15 15/15 13/15 15/15 15/15 #succ 15/15 0/15 | #FEs/D #FEs/D f19 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f20 MATSuMo | $\begin{array}{c} 1.5(4) \\ 0.5 \\ \hline 1.6e-1:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 1280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \end{array}$ | 1.2 1.0e-1:242 | 3 6.3e-2:67: ∞ 1164(1255) 30(35) ∞ 98(104) 3 4.0e+1:15 1.9(0.7) | $\begin{array}{c} 10 \\ \hline 10 \\ 5 \\ 4.0e-2:307 \\ \infty \\ 398(447) \\ 14(13) \\ \infty \\ 25(21) \\ 10 \\ 2.5e+0:69 \\ 4.1(3) \end{array}$ | $50 = 50$ $8 = 2.5e \cdot 2:4946$ $\infty \cdot 250$ $\infty \cdot 5e6$ $\infty \cdot 5e5$ $\infty \cdot 2805$ $\infty \cdot 500$ $16(13) = 50$ $1.0e + 0:851$ $\infty \cdot 250$ | #succ #succ 15/15 0/15 0/15 0/15 0/15 0/15 15/15 #succ 15/15 0/15 |
| #FEs/D f7 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D B MATSUMO RANDOM | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) 2.6(2) 1.2(1) 1.3(2) 3.2(2) 0.5 1.0e+4:4.6 1.7(2) 3.0(3) | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 2.9(2) \\ 1.2 \\ \hline 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \end{array}$ | 3 2.5e+1:20 1.5(0.6) 8.8(6) 2.2(3) 1.5(1) 1.5(0.9) 2.4(2) 3 <i>1.0e+3</i> :18 1.4(0.3) 10(8) | 10 10 4.0e+0.54 7.6(14) 151(135) 7.6(13) 2.3(3) 1.6(0.7) 2.2(0.5) 10 6.3e+1:54 2.6(1) 482(412) | $\begin{array}{r} 50\\ \hline 1.0e+0:324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.88(0.4)\\ 1.2(0.2)\\ \hline 50\\ 1.6e+0.258\\ \infty \ 5e6\end{array}$ | 15/15 #succ 15/15 15/15 15/15 15/15 15/15 15/15 15/15 #succ 15/15 0/15 0/15 | #FEs/D #FEs/D f19 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f20 MATSuMo RANDOM | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-1:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ \hline 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.8(2) \\ \hline 0.5 \\ \hline 0.$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \infty \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ \infty \end{array}$ | 3 6.3e-2:67: ∞ 1164(1255) 30(35) ∞ 98(104) 3 4.0e+1:15 1.9(0.7) 24(10) ±(0.5) | 4.2(23) 10 5 4.0e-2:307 ∞ 398(447) 14(13) ∞ 25(21) 10 2.5e+0:69 4.1(3) 251(328) | $50 = 50$ $8 = 2.5e \cdot 2:4946$ $\infty 250$ $\infty 5e6$ $\infty 5e5$ $\infty 2805$ $\infty 500$ $16(13)$ $1.0e + 0:851$ $\infty 250$ $9234(851)$ | #succ #succ 15/15 0/15 0/15 0/15 0/15 15/15 #succ 15/15 0/15 8/15 |
| #FEs/D f7 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f8 MATSUMO RANDOM NEWUOA | $\begin{array}{c} 0.5 \\ \hline 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.2(1) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ \hline 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ \end{array}$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ \hline 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1,0) \\ 0.96(1,0) \\ \end{array}$ | 3 2.5e+1:20 1.5(0.6) 8.8(6) 2.2(3) 1.5(1) 1.5(0.9) 2.4(2) 3 1.0e+3:18 1.4(0.3) 10(8) 10(0.6) 1.6(0.6) | 10 10 4.0e+0:54 7.6(14) 151(135) 7.6(13) 2.3(3) 1.6(0.7) 2.2(0.5) 10 6.3e+1:54 2.6(1) 482(412) 1(0.8) 1.6(0.4) | $\begin{array}{r} 50\\ \hline 50\\ \hline 1.0e+0.324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.88(0.4)\\ 1.2(0.2)\\ \hline 50\\ \hline 1.6e+0.258\\ \infty \ 250\\ \infty \ 5e6\\ 1.1(2)\\ 1.7(2)\end{array}$ | 15/15 #succ 15/15 2/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 0/15 0 | #FEs/D #FEs/D f19 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f20 MATSuMo RANDOM NEWUOA | $\begin{array}{c} 1.5(4)\\ \hline 0.5\\ \hline 1.6e-1:172\\ \infty\\ 4.2e5(4e5)\\ 1308(2380)\\ 55(56)\\ \infty\\ 0.5\\ \hline 0.5\\ \hline 6.3e+3:5.1\\ 1.7(2)\\ 1.6(2)\\ 2.3(0.7)\\ 1.2(0)\\ $ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \infty \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.83(0.4) \end{array}$ | $\begin{array}{c} 3\\6.3e-2:67:\\\infty\\ \infty\\1164(1255)\\30(35)\\\infty\\98(104)\\3\\4.0e+1:15\\1.9(0.7)\\24(10)\\1(0.3)\\18(1)\end{array}$ | $\begin{array}{r} 10\\ \hline 10\\ 5\\ \hline 4.0e-2:307\\ \infty\\ 398(447)\\ 14(13)\\ \infty\\ 25(21)\\ 10\\ \hline 2.5e+0:69\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ \end{array}$ | $50 = 50$ $2.5e-2:4946$ $\infty 250$ $\infty 5e6$ $\infty 5e5$ $\infty 2005$ $\infty 500$ $1.6e+0:851$ $\infty 250$ $9234(831)$ $3.3(3)$ $15(11)$ | #succ 15/15 0/15 0/15 0/15 0/15 0/15 15/15 #succ 15/15 8/15 15/15 3/15 |
| #FEs/D f7 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f8 MATSUMO RANDOM NEWUOA Imm-CMA MATSUMO RANDOM NEWUOA Imm-CMA SMAC | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) 2.6(2) 1.2(1) 1.3(2) 3.2(2) 0.5 1.0e+4:4.6 1.7(2) 3.0(3) 2.5(0.6) 1.0(1.0) 0.99(0.7) | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.9(1) \\ \end{array}$ | 3 2.5e+1:20 1.5(0.6) 8.8(6) 2.2(3) 1.5(1) 1.5(1) 1.5(0.9) 2.4(2) 3 1.0e+3:18 1.4(0.3) 1.0(0.6) 1.6(0.6) 1.2(0.8) | $\begin{array}{r} 10\\ \hline 10\\ \hline 3.0e+0.54\\ 7.6(14)\\ 151(135)\\ 7.6(13)\\ 2.3(3)\\ 1.6(0.7)\\ 2.2(0.5)\\ 10\\ \hline 6.3e+1.54\\ 2.6(1)\\ 482(412)\\ 1(0.8)\\ 1.5(0.4)\\ 3.3(3)\\ \end{array}$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 1.0e+0.324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.988(0.4)\\ 1.2(0.2)\\ \hline 50\\ \hline 1.6e+0.258\\ \infty \ 250\\ \infty \ 5e6\\ 1.1(2)\\ 1.7(2)\\ \infty \ 500\end{array}$ | 15/15 #succ 15/15 2/15 15/15 15/15 15/15 15/15 15/15 15/15 0/15 0 | HOPSAACM #FEs/D f19 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f20 MATSUMO RANDOM NEWUOA Imm-CMA SMAC | (4.)(4) 0.5 1.6e-1:172 (4.2e5(4e5) 1308(2380) 55(56) ∞ 280(359) 0.5 6.3e+3:5.1 1.7(2) 1.6(2) 2.3(0.7) 1.2(0.1) 0.57(0.2) | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \infty \\ \infty \\ 56(58) \\ \infty \\ 55(58) \\ 0 \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.83(0.4) \\ 0.44(0.2) \end{array}$ | 3 6.3e-2:67: ∞ 1164(1255) 30(35) ∞ 98(104) 3 4.0e+1:15 1.9(0.7) 24(10) 1(0.3) 1.8(1) 0,73(0.3) | $\begin{array}{c} 10\\ \hline 10\\ \hline \\ 5 & 4.0e{-}2:307\\ \infty\\ 398(447)\\ 14(13)\\ \infty\\ 255(21)\\ 10\\ 2.5e{+}0:69\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ \end{array}$ | $\begin{array}{c} 50\\ 8 & 2.5e{-}2.4946\\ \infty & 250\\ \infty & 5e6\\ \infty & 5e5\\ \infty & 2805\\ \infty & 500\\ 16(13)\\ 50\\ 1.0e{+}0.851\\ \infty & 250\\ 3.3(3)\\ 15(11)\\ \infty & 500\\ \end{array}$ | #succ 15/15 0/15 0/15 0/15 0/15 0/15 15/15 15/15 8/15 15/15 3/15 0/15 |
| #FEs/D f7 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f8 MATSUMO RANDOM NEWUOA imm-CMA SMAC IPOPsaACM MATSUMO NEWUOA Imm-CMA SMAC IPOPsaACM | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) 2.6(2) 1.2(1) 1.3(2) 1.0e+4:4.6 1.7(2) 3.0(3) 2.5(0.6) 1.0(1.0) 0.90(0.7) 2.4(2) | 1.2 1.0e+2:6.2 1.8(1) 2.9(0.8) 2.2(0.2) 1.3(0.8) 1.1(0.8) 2.9(2) 1.2 6.3e+3:6.8 1.9(1) 3.1(3) 1.8(0.1) 0.96(1.0) 0.96(| 3 2.5e+1:20 1.5(0.6) 8.8(6) 2.2(3) 1.5(1) 1.5(0.9) 2.4(2) 3 1.0e+3:18 1.4(0.3) 10(8) 1.0(0.6) 1.5(0.6) 1.2(0.8) 2.1(2) | 10 10 4.0e+0.54 7.6(14) 151(135) 7.6(13) 2.3(3) 1.6(0.7) 2.2(0.5) 10 6.3e+1:54 2.6(1) 482(412) 10.8) 1.5(0.4) 3.3(3) 2.0(1) | $\begin{array}{r} 50 \\ \hline 50 \\ \hline 1.0e+0:324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.88(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline 1.6e+0.258 \\ \infty \ 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty \ 500 \\ 1.8(2) \end{array}$ | 15/15 #succ 2/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 0/15 0 | HPOPSAACM #FEs/D f19 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f20 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM | 1.6-1:172 ∞ 4.2e5(4e5) 1308(2380) 55(56) ∞ 280(359) 0.5 6.3e+3:5.1 1.7(2) 1.6(2) 2.3(0.7) 1.2(0.1) 057(0.2) 1.8(2) | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.83(0.4) \\ 0.44(0.2) \\ 1.7(2) \end{array}$ | $\begin{array}{c} 3\\ 6.3e\text{-}2:67;\\ \infty\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ 4.0e\text{+}1:15\\ 1.9(0.7)\\ 24(10)\\ 1(0.3)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2) \end{array}$ | $\begin{array}{r} 10 \\ \hline 10 \\ 5 \\ 4.0e-2;307 \\ \infty \\ 398(447) \\ 14(13) \\ \infty \\ 25(21) \\ 10 \\ 2.5e+0.69 \\ 4.1(3) \\ 251(328) \\ 1.1(1) \\ 4.0(6) \\ 4.3(2) \\ 3.2(2) \end{array}$ | $\begin{array}{c} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \infty & 250\\ \infty & 5e6\\ \infty & 5e5\\ \infty & 2805\\ \infty & 500\\ \hline 1.0e{+}0{\cdot}851\\ \hline & 0.250\\ 9234(8531)\\ \hline & 3.3(3)\\ 15(11)\\ \infty & 500\\ 3.5(3)\\ \end{array}$ | #succ #succ 15/15 0/15 0/15 0/15 0/15 15/15 #succ 15/15 8/15 15/15 3/15 0/15 15/15 15/15 |
| #FEs/D f7 mATSuMo RANDOM NEWUOA lmm-CMA SMAC IPOPsaACM #FEs/D MATSuMo RANDOM NEWUOA IPOPsaACM #FEs/D | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) 2.6(2) 1.2(1) 1.3(2) 3.2(2) 0.5 1.0e+4:4.6 1.7(2) 3.0(3) 2.5(0.6) 1.0(1.0) 0.99(0,7) 2.4(2) 0.5 | $\begin{array}{c} 12\\ 1.0e+2:6.2\\ 1.8(1)\\ 2.9(0.8)\\ 2.2(0.2)\\ 1.3(0.8)\\ 1.1(0.8)\\ 2.9(2)\\ \hline 6.3e+3:6.8\\ 1.9(1)\\ 3.1(3)\\ 1.8(0.1)\\ 0.96(1.0)\\ 0.91(1)\\ 2.2(3)\\ 1.2\end{array}$ | $\begin{array}{c} 3\\ \hline 2.5e+1:20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(1)\\ 1.5(0.9)\\ 2.4(2)\\ \hline \\ 3\\ 1.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.5(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ \hline \\ 3\end{array}$ | $\begin{array}{r} 10\\ \hline 10\\ \hline 4.0e+0.54\\ 7.6(14)\\ 151(135)\\ 7.6(13)\\ 2.3(3)\\ 1.6(0.7)\\ 2.2(0.5)\\ \hline 0\\ 6.3e+1.54\\ 2.6(1)\\ 482(412)\\ 1(0.8)\\ 1.5(0.4)\\ 3.3(3)\\ 2.0(1)\\ 10\end{array}$ | $\begin{array}{r} 50\\ \hline \\ 1.0e+0:324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.88(0,4)\\ 1.2(0,2)\\ \hline \\ 50\\ \hline \\ 1.6e+0.258\\ \infty \ 5e6\\ 1.1(2)\\ 1.7(2)\\ \infty \ 500\\ 1.8(2)\\ \hline \\ 50\\ \end{array}$ | 15/15 #succ 2/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 #succ | HPOPSAACM #FEs/D f19 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM #FEs/D IPOPSAACM #FEs/D | $\begin{array}{c} 0.5 \\ \hline 1.6e-1:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 1280(359) \\ 0.5 \\ \hline 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.5 \\ \end{array}$ | $\begin{array}{c} 1.2 \\ 1.0e{-}1.242 \\ \infty \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e{+}3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.83(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \end{array}$ | $\begin{array}{c} 3\\ 6.3e\text{-}2:67:\\ \infty\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ 4.0e\text{+}1:15\\ 1.9(0.7)\\ 24(10)\\ 1(0.3)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\end{array}$ | $\begin{array}{r} 10\\ \hline 10\\ 5\\ 4.0e{-}2:307\\ \infty\\ 398(447)\\ 114(13)\\ \infty\\ 25(21)\\ 10\\ 2.5e{+}0:69\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 10\\ \end{array}$ | $\begin{array}{c} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2:4946\\ \hline \infty & 250\\ \hline \infty & 5e6\\ \hline \infty & 5e5\\ \hline \infty & 2805\\ \hline \infty & 500\\ 16(13)\\ \hline & 50\\ \hline & 1.0e{+}0:851\\ \hline & \infty & 550\\ 15(11)\\ \hline & \infty & 500\\ \hline & 3.5(3)\\ \hline \end{array}$ | #succ #succ 15/15 0/15 0/15 0/15 0/15 15/15 #succ 15/15 3/15 0/15 15/15 #succ |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) 2.6(2) 1.2(1) 1.3(2) 3.2(2) 0.5 1.0e+4:4.6 1.7(2) 3.0(3) 2.5(0.6) 1.0(1.0) 0.99(0,7) 2.4(2) 0.5 2.5e+1:20 | 1.2 1.0e+2:6.2 1.8(1) 2.9(0.8) 2.2(0.2) 1.3(0.8) 1.1(0.8) 2.9(2) 6.3e+3:6.8 1.9(1) 3.1(3) 1.8(0.1) 0.96(1.0) 0.91(1) 2.2(3) 1.2 1.2 1.2 1.2 1.2 1.2 | 3 2.5e+1:20 1.5(0.6) 8.8(6) 2.2(3) 1.5(1) 1.5(1) 1.5(1) 1.5(0.9) 2.4(2) 3 1.0e+3:18 1.4(0.3) 10(8) 1.0(0.6) 1.2(0.8) 2.1(2) 3 1.0e+1:35 1.0e+1:35 | $\begin{array}{r} 10\\ \hline 10\\ \hline 3.0e+0.54\\ 7.6(14)\\ 151(135)\\ 7.6(13)\\ 2.3(3)\\ 1.6(0.7)\\ 2.2(0.5)\\ 10\\ \hline 6.3e+1.54\\ 2.6(1)\\ 1482(412)\\ 1(0.8)\\ 1.5(0.4)\\ 1.5(0.4)\\ 3.3(3)\\ 2.0(1)\\ 10\\ \hline 4.0e+0.62\end{array}$ | $\begin{array}{r} 50\\ \hline 50\\ 1.0e+0.324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.98(0.4)\\ 1.2(0.2)\\ \hline 50\\ 7.6e+0.288\\ \infty 250\\ \infty 5e6\\ 1.1(2)\\ 1.7(2)\\ \infty 500\\ 1.8(2)\\ 50\\ 1.6e-2.256\end{array}$ | 15/15 #succ 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 0/15 15/15 0/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 | HPOPSACKM #FEs/D f19 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D IPOPsaACM IPOPsaACM IPOPsaACM IPOPsaACM #FEs/D f21 | $\begin{array}{c} 0.5 \\ \hline 1.6e-l:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.5 \\ 4.0e+l:3.9 \\ 1.3(2) \\ 1.8(2) \\ 0.5 \\ 1.6(2) \\ 1.6$ | $\begin{array}{c} 1.2 \\ 1.0e{-}1.242 \\ \hline 0.0e{-}1.242 \\ \infty \\ 56(58) \\ \infty \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e{+}3.8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.03(0.4) \\ 0.044(0.2) \\ 1.7(2) \\ 1.7(2) \\ 1.2 \\ 2.5e{+}1:11 \\ 1.12 \\ 1.2 $ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \\ \infty\\ 1164(1255)\\ 30(35)\\ \\ \\ \\ \\ \\ 30(35)\\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ $ | $\begin{array}{c} 10\\ \hline 10\\ 5\\ \hline 4.0e{-}2:307\\ \infty\\ 398(447)\\ 14(13)\\ \infty\\ 25(21)\\ 10\\ 2.5e{+}0:69\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 3.2(2)\\ 3.2(2)\\ 10\\ \hline 6.3e{+}0:73\\ 10 \end{array}$ | $\begin{array}{r} 50\\ 8 & 2.5e{-}2.4946\\ \infty & 250\\ \infty & 5e6\\ \infty & 5e5\\ \infty & 2805\\ \infty & 500\\ 16(13)\\ 50\\ 1.0e{+}0.851\\ 50\\ 234(8531)\\ 3.3(3)\\ 15(11)\\ 500\\ 3.5(3)\\ 500\\ \mathbf{1.6e{+}0.347} \end{array}$ | #succ #succ 15/15 0/15 0/15 0/15 0/15 0/15 15/15 #succ 15/15 3/15 0/15 15/15 3/15 0/15 15/15 3/15 0/15 0/15 15/15 0/15 15/15 0/ |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D p AATSUMo AATSUMO PATSUMO PATSUMO | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) 2.6(2) 1.2(1) 1.3(2) 1.2(2) 1.2(2) 1.2(2) 1.2(2) 1.2(2) 1.2(2) 1.2(2) 1.2(2) 1.2(2) 1.2(2) 1.2(2) 1.2(1) 1.2(2) 1.2(2) 1.2(1) 1.2(2 | 12 1.0e+2:6.2 1.8(1) 2.9(0.8) 2.2(0.2) 1.3(0.8) 1.1(0.8) 2.9(2) 1.2 6.3e+3:6.8 1.9(1) 3.1(3) 1.8(0.1) 0.96(1.0) 0.91(1) 2.2(3) 1.2 1.6e+1:26 34(51) 2.3(4e+1) 3.3(4e+1) 3.3(4e+1) 3.3(4e+1) 3.3(4e+1) 3.3(4e+1) 3.3(4e+1) 3.3(4e+1) 3.3(4e+1) 3.4(4e+1) | $\begin{array}{c} 3\\ \hline 2.5e+1:20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(1)\\ 1.5(1)\\ 1.5(0.9)\\ 2.4(2)\\ 3\\ \hline 1.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1:35\\ 355(26)\\ 4.14(2-1)\\ \end{array}$ | 10 10 $4.0e+0.54$ $7.6(14)$ $151(135)$ $7.6(13)$ $2.3(3)$ $1.6(0.7)$ $2.2(0.5)$ 10 $6.3e+1.54$ $2.6(1)$ $482(412)$ $1(0.8)$ $1.5(0.4)$ $3.3(3)$ $2.0(1)$ 10 $4.0e+0.62$ $64(75)$ $12.6(5)$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 1.0e+0.324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.88(0.4)\\ 1.2(0.2)\\ \hline 50\\ \hline 1.6e+0.258\\ \infty 250\\ \infty 5e6\\ 1.1(2)\\ 1.7(2)\\ \infty 500\\ 1.8(2)\\ \hline 50\\ \hline 1.6e-2.256\\ \infty 250\\ \hline 0.5e-6\\ \hline \end{array}$ | 15/15 #succ 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 0/15 | HOTSAACM HESD HIP MATSUMO RANDOM NEWUOA Imm-CMA SMAC HOPSAACM HESD RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HDPSAACM HES/D 21 MATSUMO PANDOM | $\begin{array}{c} 0.5 \\ \hline 1.6e-l:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.5 \\ 4.0e+l:3.9 \\ 1.3(0.9) \\ 1.4(2) \\ $ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.38(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.7(2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1.0(2) \end{array}$ | $\begin{array}{c} 3\\ 6.3e\text{-}2:67:\\ \infty\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ 4.0e\text{+}1:15\\ 1.9(0.7)\\ 24(10)\\ 1(0.3)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ 1.6e\text{+}1:31\\ 0.73(0.3)\\ 1.3(2)\\ \end{array}$ | $\begin{array}{r} 10\\ 10\\ 5\\ 4.0e{-}2:307\\ \infty\\ 398(447)\\ 14(13)\\ \infty\\ 25(21)\\ 10\\ 2.5e{+}0:69\\ 4.1(3)\\ 25(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 10\\ 6.3e{+}0:73\\ 1.2(1)\\ 7.7(7)\end{array}$ | $\begin{array}{c} 50\\ 8 & 2.5e{-}2.4946\\ \infty & 250\\ \infty & 5e6\\ \infty & 5e5\\ \infty & 2805\\ \infty & 500\\ 16(13)\\ 50\\ 9234(8531)\\ 3.3(3)\\ 15(11)\\ \infty & 500\\ 3.5(3)\\ 50\\ 1.6e{+}0.347\\ 1.5(1.0)\\ 15(11)\\ \end{array}$ | #succ 15/15 0/15 0/15 0/15 0/15 0/15 15/15 8/15 15/15 3/15 0/15 15/15 5/15 15/15 #succ 5/5 7/15 15/15 |
| #FE3/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FE3/D r8 MATSuMo MATSuMo NATSUMO NEWUOA Imm-CMA SMAC IPOPsaACM #FE3/D j0 MATSUMO AATSUMO NEWUOA MATSUMO WEOSAMCM POPsaACMO NEWUOA NATSUMO NEWUOA NATSUMO NEWUOA NATSUMO NEWUOA NATSUMO NEWUOA | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) 2.6(2) 1.2(1) 1.3(2) 3.2(2) 0.5 1.0e+4:4.6 1.7(2) 0.5 2.5(e+1:20) 0.99(0,7) 2.4(2) 0.5 2.5(e+1:20) 18(10) 7845(7036) 2.30(6)* | 1.2 1.0e+2:6.2 1.8(1) 2.9(0.8) 2.2(0.2) 1.3(0.8) 1.1(0.8) 2.9(2) 1.2 6.3e+3:6.8 1.9(1) 3.1(3) 1.8(0.1) 0.96(1.0) 0.96(1.0) 0.96(1.0) 0.96(1.0) 1.2 1.2 1.6e+1:26 3.4(51) 2.3e(4(64) 2.100 * | $\begin{array}{c} 3\\ \hline 2.5e+1:20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(1)\\ 1.5(0.9)\\ 2.4(2)\\ 3\\ \hline 1.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1:35\\ 3.5(26)\\ 4.1e4(3e4)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star} \end{array}$ | 10 10 $4.0e+0.54$ $7.6(14)$ $151(135)$ $7.6(13)$ $2.3(3)$ $1.6(0.7)$ $2.2(0.5)$ 10 $6.3e+1.54$ $2.6(1)$ $4.82(412)$ $1(0.8)$ $1.5(0.4)$ $3.3(3)$ $2.0(1)$ 10 $4.0e+0.62$ $64(75)$ $1.2e6(2e6)$ $2.2(1)$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 1.0e+0:324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.88(0.4)\\ 1.2(0.2)\\ \hline 50\\ \hline 1.6e+0.258\\ \infty \ 250\\ \hline 5.66\\ 1.1(2)\\ 1.7(2)\\ \infty \ 500\\ 1.8(2)\\ \hline 50\\ \hline 1.6e-2:256\\ \infty \ 250\\ \infty \ 5e6\\ \hline 2.2(1)\\ \hline \end{array}$ | IS/15 #succ 15/15 15/15 15/15 15/15 15/15 15/15 15/15 0/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 0/15 15/15 0/15 0 | HOFSAACM HEESD HID MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM HOPsaACM MATSUMO RANDOM NEWUOA MATSUMO HOPsaACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPsAACM HIPOPSAAC | $\begin{array}{c} 0.5 \\ \hline 0.6e-l:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.5 \\ 4.0e+l:3.9 \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \end{array}$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.63(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \end{array}$ | $\begin{array}{c} 3\\ 6.3e\text{-}2:67:\\ \infty\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ \mathbf{4.0e+1:15}\\ 1.9(0.7)\\ 24(10)\\ 1(0.3)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ \mathbf{1.6e+1:31}\\ 0.73(0.8)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ \end{array}$ | $\begin{array}{r} 10 \\ \hline 10 \\ 5 \\ 4.0e-2;307 \\ \infty \\ 398(447) \\ 14(13) \\ \infty \\ 25(21) \\ 10 \\ 2.5e+0.69 \\ 4.1(3) \\ 251(328) \\ 1.1(1) \\ 4.0(6) \\ 4.3(2) \\ 3.2(2) \\ 1.3(1) \\ 6.3e+0.73 \\ 1.2(1) \\ 7.7(7) \\ 1.3(1) \end{array}$ | $\begin{array}{c} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \infty & 250\\ \hline \infty & 5e6\\ \infty & 5e5\\ \infty & 2805\\ \infty & 500\\ \hline 1.6e{+}0.851\\ \hline 0.250\\ 9234(8531)\\ \hline 3.3(3)\\ 15(11)\\ \hline \infty & 500\\ 3.5(3)\\ \hline 1.6e{+}0.347\\ \hline 1.5(1.0)\\ 15(11)\\ 5.4(6)\\ \hline \end{array}$ | #succ 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 0/15 3/15 0/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #ES/D Ø MATSUMo RANDOM NEWUOA Imm-CMA SMAC | 0.5 1.6e+2:4.2 1.3(1) 2.0(2) 2.6(2) 1.2(1) 1.3(2) 3.2(2) 0.5 1.0e+4:4.6 1.7(2) 0.5 1.0e+4:4.6 1.7(2) 0.5 2.5(e+1:20) 18(10) 7845(7036) 2.3(0.6)* 3.7(1) | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.18(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^* \\ 3.3(1) \end{array}$ | $\begin{array}{c} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(0.9)\\ 2.4(2)\\ 3\\ 1.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 2.7(0.5)\\ \end{array}$ | $\begin{array}{r} 10 \\ \hline 10 \\ \hline 2.0e+0.54 \\ 7.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 1.6(0.7) \\ 2.2(0.5) \\ 10 \\ \hline 6.3e+1.54 \\ 2.6(1) \\ 482(412) \\ 1(0.8) \\ 1.5(0.4) \\ 3.3(3) \\ 2.0(1) \\ 10 \\ \hline 4.0e+0.62 \\ 64(75) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \end{array}$ | $\begin{array}{r} 50\\ \hline 50\\ 1.0e+6.324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.88(0.4)\\ 1.2(0.2)\\ \hline 50\\ 1.6e+0.258\\ \infty \ 5e6\\ 1.1(2)\\ 1.7(2)\\ \infty \ 500\\ 1.8(2)\\ \hline 50\\ 1.6e-2.256\\ \infty \ 250\\ \infty \ 5e6\\ 2.2(1)\\ 2.4(2)\\ \hline \end{array}$ | IS/15 #succ 15/15 15/15 15/15 15/15 15/15 15/15 15/15 0/15 15/15 15/15 15/15 15/15 15/15 15/15 0/15 15/15 0/15 15/15 15/15 15/15 15/15 | HOFSACM HFE3D HFSD KANDOM NEWUOA Imm-CMA SMAC IPOPsaACM HFE3D HTSD NATSUMO RANDOM NEWUOA Imm-CMA MATSUMO RANDOM NEWUOA Imm-CMA | $\begin{array}{c} 0.5 \\ \hline 0.6e-l:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 228(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.9(2) \\ 1.9(2) \end{array}$ | $\begin{array}{c} 1.2 \\ 1.0e{-}1.242 \\ \hline 0.0e{-}1.242 \\ \infty \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e{+}3.8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.33(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e{+}1.11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \end{array}$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \\ \infty\\ 1164(1255)\\ 30(35)\\ \\ 98(104)\\ 3\\ 4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ 1.6e+1:31\\ 0.73(0.8)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 0.93(0.8)\\ \end{array}$ | $\begin{array}{r} 10\\ \hline 10\\ \hline & 4.0e{-}2:307\\ \infty\\ 398(447)\\ 14(13)\\ \infty\\ 25(21)\\ 10\\ 2.5e{+}0.69\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 10\\ \hline & 6.3e{+}0{\cdot}73\\ 1.2(1)\\ 7.7(7)\\ 1.3(1)\\ 1.6(0.5)\\ \end{array}$ | $\begin{array}{r} 50\\ \hline & 2.5e{-}2.4946\\ \hline \infty \ 250\\ \hline \infty \ 5e6\\ \hline \infty \ 5e5\\ \hline \infty \ 2805\\ \hline \infty \ 500\\ \hline 16(13)\\ \hline 0234(851)\\ \hline 3.3(3)\\ 15(11)\\ \hline 3.5(3)\\ \hline 1.6e{+}0.851\\ \hline 0.50\\ \hline 1.6e{+}0.347\\ \hline 1.5(1.0)\\ \hline 15(11)\\ \hline 5.4(6)\\ 2.7(4)\end{array}$ | IS/IS 45/IS 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 15/15 15/15 15/15 15/15 15/15 13/15 |
| #FEx/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEx/D B MATSuMo NEWUOA Imm-CMA SMAC IPOPsaACM #FEx/D g MATSuMo #KEX/D g MATSuMo RANDOM NEWUOA Imm-CMA SMAC SMAC IPO-saACM #G MATSuMo ANDOM | $\begin{array}{c} 0.5\\ 1.6e+2:4.2\\ 1.3(1)\\ 2.0(2)\\ 2.6(2)\\ 1.2(1)\\ 1.3(2)\\ 3.2(2)\\ 0.5\\ 1.0e+4:4.6\\ 1.7(2)\\ 3.0(3)\\ 2.5(0.6)\\ 1.0(1.0)\\ 0.99(0.7)\\ 2.4(2)\\ 0.5\\ 2.5e+1:20\\ 1.8(10)\\ 7845(7036)\\ 2.3(0.6)^*\\ 3.7(1)\\ 14(9)\\ \end{array}$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^* \\ 3.3(1) \\ 12(3) \end{array}$ | $\begin{array}{c} 3\\ \hline 2.5e+1:20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(1)\\ 1.5(0.9)\\ 2.4(2)\\ 3\\ 1.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{*}\\ 2.7(0.5)\\ 12(3)\\ \end{array}$ | $\begin{array}{r} 10\\ \hline 10\\ \hline 4.0e+0.54\\ 7.6(14)\\ 151(135)\\ 7.6(13)\\ 2.3(3)\\ 1.6(0.7)\\ 2.2(0.5)\\ 10\\ \hline 6.3e+1.54\\ 2.6(1)\\ 482(412)\\ 1(0.8)\\ 1.5(0.4)\\ 3.3(3)\\ 2.0(1)\\ \hline 1.2e6(2e6)\\ 6.4(75)\\ 1.2e6(2e6)\\ 2.2(1)\\ 2.7(0.9)\\ 120(95)\\ \end{array}$ | $\begin{array}{r} 50 \\ \hline 50 \\ \hline 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.988(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline 1.6e+0.258 \\ \infty \ 250 \\ \infty \ 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty \ 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e-2.256 \\ \infty \ 250 \\ \infty \ 5e6 \\ 2.2(1) \\ 2.4(2) \\ \infty \ 500 \\ \end{array}$ | 15/15 #suecc 15/15 15/15 15/15 15/15 15/15 15/15 13/15 15/15 15/15 15/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 0/15 15/15 0/15 0/15 0/15 | HOFSIACM #FEs/D TI9 MTSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsiaACM #FEs/D T20 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsiaACM | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-I:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 2.80(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.5 \\ 4.0e+I:3.9 \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.9(2) \\ 1.8(2) \\ 1.9(2) \\ 1.8(2$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 56(58) \\ \infty \\ 55(58) \\ \infty \\ 55(58) \\ 0.250(295) \\ 1.2 \\ 1.2 \\ 0.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.3(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \end{array}$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ 4.0e+l:15\\ 1.9(0.7)\\ 24(10)\\ 1(0.3)\\ 1.8(1)\\ 0.73(0.8)\\ 2.3(2)\\ 3\\ 1.6e+l:31\\ 0.73(0.8)\\ 1.3(2)\\ 1$ | $\begin{array}{r} 10\\ 10\\ 5\\ 4.0e{-}2:307\\ \infty\\ 398(447)\\ 14(13)\\ \infty\\ 255(21)\\ 10\\ 2.5e{+}0:69\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 10\\ 6.3e{+}0:73\\ 1.2(1)\\ 7.7(7)\\ 1.3(1)\\ 1.6(0.5)\\ 1.0(0.9)\\ \end{array}$ | $\begin{array}{r} 50\\ \hline & 2.5e{-}2.4946\\ \hline \infty 250\\ \hline \infty 5c6\\ \hline \infty 5c6\\ \hline \infty 5c5\\ \hline \infty 2805\\ \hline \infty 500\\ \hline 16(13)\\ \hline 0\\ 9234(8531)\\ \hline \infty 250\\ 9234(8531)\\ \hline 3.3(3)\\ \hline 15(11)\\ \hline \infty 500\\ \hline 3.5(3)\\ \hline 50\\ \hline 1.6e{+}0.347\\ \hline 1.5(1.0)\\ \hline 15(11)\\ \hline 5.4(6)\\ 2.7(4)\\ \hline 1.0(0.6)\\ \hline \end{array}$ | 45/15 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 115/15 115/15 115/15 115/15 115/15 115/15 115/15 115/15 |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D 100 RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D 10 MATSUMO ASMAC IPOPsaACM MATSUMO ASMAC IPOPsaACA IPOPsaACA IPOPsaCA IPOPsaCA IPOPsaCA IPOPsaCA | $\begin{array}{c} 0.5\\ 1.6e+2:4.2\\ 1.3(1)\\ 2.0(2)\\ 2.6(2)\\ 1.2(1)\\ 1.3(2)\\ 3.2(2)\\ 0.5\\ 1.0e+4:4.6\\ 1.7(2)\\ 3.0(3)\\ 2.5(0.6)\\ 1.0(1.0)\\ 0.99(0.7)\\ 2.4(2)\\ 0.5\\ 2.5e+1:20\\ 185(10)\\ 7845(7036)\\ 2.30(.6)*\\ 3.7(1)\\ 14(9)\\ 6.8(1)\\ \end{array}$ | 1.2 1.0e+2:6.2 1.8(1) 2.9(0.8) 2.2(0.2) 1.3(0.8) 1.1(0.8) 2.9(2) 1.2 6.3e+3:6.8 1.9(1) 3.1(3) 1.8(0.1) 0.96(1.0) 0.91(1) 2.2(3) 1.2 1.6e+1:26 3.4(51) 2.3e4(4e4) 2.1(0.9)* 3.3(1) 12(3) 5.7(2) | $\begin{array}{c} 3\\ \hline 2.5e+1:20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(1)\\ 1.5(0.9)\\ 2.4(2)\\ 3\\ \hline 1.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ 35(26)\\ 4.1e4(3e4)\\ 4.1e4(3e4)\\ 4.1e4(3e4)\\ 1.8(0.7)\\ 2.7(0.5)\\ 12(3)\\ 5.0(2)\\ \end{array}$ | 10 10 $4.0e+0.54$ $7.6(14)$ $151(135)$ $7.6(13)$ $2.3(3)$ $1.6(0.7)$ $2.2(0.5)$ 10 $6.3e+1.54$ $2.6(1)$ $482(412)$ $1(0.8)$ $1.5(0.4)$ $3.3(3)$ $2.0(1)$ 10 $4.0e+0.62$ $64(75)$ $1.2e6(2e6)$ $2.2(1)$ $2.7(0.9)$ $120(95)$ $3.7(2)$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 1.0e+0.324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.88(0.4)\\ 1.2(0.2)\\ \hline 50\\ \hline 1.6e+0.258\\ \infty 250\\ \hline 5.66\\ 1.1(2)\\ 1.7(2)\\ \infty 500\\ 1.8(2)\\ \hline 50\\ \hline 1.6e+2.256\\ \infty 250\\ \hline 0.500\\ 2.2(1)\\ 2.4(2)\\ \infty 500\\ 2.3(0.8)\\ \hline \end{array}$ | [15/15] #succ #succ [15/15] [15 | HOFSAACM HFEs/D HATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM HFEs/D T00 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM HES/D CI DOPsaACM Imm-CMA SMAC IPOPsaACM | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-1:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.5 \\ 4.0e+1:3.9 \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.9(2) \\ 1$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.38(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(1) \\ 1.8(1) \\ 1.8(1) \\ 1.2 \\ $ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ 4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1(0.3)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ 1.6e+1:31\\ 0.73(0.8)\\ 1.3(2)$ | $\begin{array}{c} 10 \\ \hline 10 \\ 5 \\ 4.0e-2:307 \\ \infty \\ 398(447) \\ 14(13) \\ \infty \\ 25(21) \\ 10 \\ 2.5e+0:69 \\ 4.1(3) \\ 251(328) \\ 1.1(1) \\ 4.0(6) \\ 4.3(2) \\ 3.2(2) \\ 1.2(1) \\ 7.7(7) \\ 1.2(1) \\ 7.7(7) \\ 1.3(1) \\ 1.6(0.5) \\ 1.0(0.9) \\ 3.8(4) \\ 10 \end{array}$ | $\begin{array}{c} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \hline \infty & 250\\ \hline \infty & 5e6\\ \hline \infty & 5e6\\ \hline \infty & 5e6\\ \hline \infty & 5e0\\ \hline \infty & 500\\ \hline 1.0e{+}0.851\\ \hline \infty & 250\\ \hline 9234(8531)\\ \hline 3.3(3)\\ \hline 15(11)\\ \hline \infty & 500\\ \hline 3.5(3)\\ \hline 50\\ \hline 1.6e{+}0.347\\ \hline 1.5(1.0)\\ \hline 15(11)\\ \hline 5.4(6)\\ 2.7(4)\\ \hline 1.0(0.6)\\ \hline 4.8(6)\\ \hline 50\\ \hline \end{array}$ | #succ 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 |
| #FE3/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FE3/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FE3/D MATSUMO AANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FE3/D #FE3/D #FE4D | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 1.0(1.0) \\ 1.0(1.0) \\ 0.99(0.7) \\ 1.0(1.0) \\ 0.99(0.7) \\ 1.0(1.0) \\ 0.99(0.7) \\ 1.0(1.0) \\ 0.5 \\ 1.0(1.0) \\ 1.0(1.0) \\ 0.5 \\ 1.0(1.0) \\$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 2.9(2) \\ 1.2 \\ 1.6e+1:26 \\ 3.1(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^{*} \\ 3.3(1) \\ 12(3) \\ 3.3(1) \\ 12(3) \\ 5.7(2) \\ 1.2 \\ 1$ | $\begin{array}{c} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(0.9)\\ 2.4(2)\\ 3\\ 1.0e+3.18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 1.2(0.5)\\ 1.2(3)\\ 5.0(2)\\ 3\\ 5.0(2)\\ 3\\ 5.0(2)\\ 5.0(2)\\ 3\\ 5.0(2)\\ 5.$ | $\begin{array}{r} 10 \\ \hline 10 \\ \hline 4.0e+0.54 \\ 7.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 1.6(0.7) \\ 2.2(0.5) \\ 1.2e(0.7) \\ 482(412) \\ 1(0.8) \\ 1.5(0.4) \\ 3.3(3) \\ 2.0(1) \\ 10 \\ \hline 4.0e+0.62 \\ 64(75) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 120(95) \\ 3.7(2) \\ 10 \\ \hline \end{array}$ | $\begin{array}{r} 50\\ \hline 50\\ \hline l.0e+0.324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.88(0.4)\\ 1.2(0.2)\\ \hline 50\\ r.6e+0.258\\ \infty 250\\ \infty 5e6\\ 1.1(2)\\ 1.7(2)\\ \infty 500\\ 1.8(2)\\ \hline 50\\ r.6e-2.256\\ \infty 250\\ 0.56\\ 2.2(1)\\ 2.4(2)\\ \infty 500\\ 2.3(0.8)\\ \hline 50\\ 0.56\\ 2.4(2)\\ \infty 500\\ 2.4(2)\\ 0.4(2)$ | 15/15 #succ 15/15 2/15 15/15 | HOFSAACM HFEs/D HFEs/D HOPSAACM HFES/D HOPSAACM HFES/D HOPSAACM HFES/D HTSMMO RANDOM NEWUOA Imm-CMA SMAC HOPSAACM HFES/D HTSMMO RANDOM NEWUOA Imm-CMA SMAC HFES/D HTSMMO KATSMMO KATSMMO KATSMMO HFES/D HOPSAACM HOPSAACM H | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-i:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 2.80(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 2.30(7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 1.5(0.1) \\ 0.33(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(1) \\ 1.8(1) \\ 1.8(1) \\ 1.2 \\ 1.8 \\ 1.2 \\ 1.$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \\ \infty\\ 1164(1255)\\ 30(35)\\ \\ 98(104)\\ 3\\ 4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.0(3)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ 1.6e+1:31\\ 0.73(0.8)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 3\\ 2.5e+1:33\\ 2.5e+1:32\\ 2.5e+1$ | $\begin{array}{r} 10\\ \hline 10\\ \hline$ | $\begin{array}{r} 50\\ \hline & 2.5e{-}2.4946\\ \hline \infty \ 250\\ \hline \infty \ 5e6\\ \hline \infty \ 5e5\\ \hline \infty \ 5e5\\ \hline \infty \ 5e5\\ \hline \infty \ 5e6\\ \hline \infty \ 5e5\\ \hline \infty \ 5e6\\ \hline 0 \ 5e5\\ \hline 0 \ 5e6\\ \hline 16(13)\\ \hline 0 \ 5e6\\ \hline 1.6e{+}0.851\\ \hline \infty \ 500\\ \hline 1.6e{+}0.851\\ \hline 0 \ 50\\ \hline 1.6e{+}0.347\\ \hline 1.5(11)\\ \hline 5.4(6)\\ \hline 2.7(4)\\ \hline 1.0(0.6)\\ \hline 4.8(6)\\ \hline 50\\ \hline 1.6e{+}0.341\\ \hline \end{array}$ | 45/15 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 5/5 5/5 15/15 15/15 15/15 15/15 15/15 5/5 |
| #FEx/D f7 MATSuMo RANDOM NEWUGA Imm-CMA SMAC IPOPsaACM #FEs/D B MATSUMo NEWUGA Imm-CMA SMAC IPOPsaACM #FEs/D 9 MATSUMo RANDOM NEWUGA Imm-CMA SMAC IPOPsaACM #FEs/D F09 MATSUMO NACM IPOPsaACM WEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f10 | $\begin{array}{c} 0.5\\ 1.6e+2:4.2\\ 1.3(1)\\ 2.0(2)\\ 2.6(2)\\ 1.2(1)\\ 1.3(2)\\ 3.2(2)\\ 0.5\\ 1.0e+4:4.6\\ 1.7(2)\\ 3.0(3)\\ 2.5(0.6)\\ 1.0(1.0)\\ 0.99(0,7)\\ 2.4(2)\\ 0.5\\ 2.5e+4:20\\ 18(10)\\ 7845(7036)\\ 2.3(0.6)^*\\ 3.7(1)\\ 14(9)\\ 6.8(1)\\ 0.5\\ 2.5e+6:2.9\\ 15(1)\\ 5.5e+6:2.9\\ 15(1)\\ 15($ | $\begin{array}{c} 12\\ 1.0e+2:6.2\\ 1.8(1)\\ 2.9(0.8)\\ 2.2(0.2)\\ 1.3(0.8)\\ 1.1(0.8)\\ 2.9(2)\\ 2.9(2)\\ 1.2\\ 6.3e+3:6.8\\ 1.9(1)\\ 3.1(3)\\ 1.8(0.1)\\ 0.96(1.0)\\ 0.91(1)\\ 2.2(3)\\ 1.2\\ 1.6e+1:26\\ 34(51)\\ 2.3e4(4e4)\\ 2.1(0.9)^*\\ 3.3(1)\\ 12(3)\\ 5.7(2)\\ 1.2\\ 6.3e+5:7.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.2\\ 1.0\\ 1.0\\ 1.0\\ 1.0\\ 1.0\\ 1.0\\ 1.0\\ 1.0$ | $\begin{array}{c} 3\\ \hline 3\\ 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1.6)\\ 2.4(2)\\ 3\\ 1.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 2.7(0.5)\\ 12(3)\\ 5.0(2)\\ 3\\ 2.5e+5:17\\ 1.4(1.2e+5):17\\ 1.4(1.2e+5):17\\ 1.5(1.2e+5):17\\ 1.5(1.2$ | $\begin{array}{r} 10\\ 10\\ \hline 10\\ \hline 2.6(14)\\ 151(135)\\ 7.6(13)\\ 2.3(3)\\ 1.6(0.7)\\ 2.2(0.5)\\ 10\\ \hline 6.3e+1.54\\ 2.6(1)\\ 482(412)\\ 1(0.8)\\ 1.5(0.4)\\ 3.3(3)\\ 2.0(1)\\ \hline 10\\ \hline 4.0e+0.62\\ 64(75)\\ 1.2e6(2e6)\\ 2.2(1)\\ 2.7(0.9)\\ 120(95)\\ 3.7(2)\\ 10\\ \hline 6.3e+3.54\\ 6.4(5)\\ 10\\ \hline 6.3e+3.54\\ 6.4(5)\\ 10\\ \hline 6.3e+3.54\\ 6.4(5)\\ 10\\ \hline 6.3e+3.54\\ 6.4(5)\\ 10\\ \hline 0.3e+3.54\\ \hline 0.3e+3.$ | $\begin{array}{r} 50 \\ \hline 50 \\ \hline l.0e+0.324 \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.98(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline l.6e+0.258 \\ \infty \ 250 \\ \infty \ 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty \ 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e-2.256 \\ \infty \ 250 \\ \infty \ 5e6 \\ 2.2(1) \\ 2.4(2) \\ \infty \ 500 \\ 2.3(0.8) \\ 50 \\ 2.5e+1:297 \\ \infty \ 50 \\ 2.5e+1:297 \\ \infty \ 50 \\ \hline \end{array}$ | 15/15 #succ 15/15 2/15 15/15 <td>IFOFSIACA) HFEs/D HFEs/D HATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPSIACM HFEs/D P20 MATSuMo RANDOM NEWUOA IPOPSIACM HATSUMO RANDOM NEWUOA IPOPSIACM HATSUMO RANDOM NEWUOA IPOPSIACM HES/D F21 MATSUMO RANDOM NEWUOA</td> <td>$\begin{array}{c} 0.5 \\ \hline 0.6e-l:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.67(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.3(0.9) \\ 1.3(0.9) \\ 1.3(0.9) \\ 1.3(0.9) \\ 1.3(0.9) \\ 1.3(2) \\ 0.5 \\ 0.5e+l:3.6 \\ 1.6(2) \\ 0.5e+l:3.6 \\ 1.6(2)$</td> <td>$\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 56(58) \\ \infty \\ 55(58) \\ \infty \\ 55(58) \\ 0.250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.33(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.1(2)$</td> <td>$\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ 4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1(0.3)\\ 1.8(1)\\ 0.73(0.8)\\ 2.3(2)\\ 3\\ 1.3(2)\\$</td> <td>$\begin{array}{r} 10\\ 10\\ 5\\ 4.0e{-}2:307\\ \infty\\ 399(447)\\ 14(13)\\ \infty\\ 255(21)\\ 10\\ 2.5e{+}0:69\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 1.1(1)\\ 4.0(6)\\ 5.2e{+}0:73\\ 1.2(1)\\ 7.7(7)\\ 1.3(1)\\ 1.6(0.5)\\ 1.0(0.5)\\ 1$</td> <td>$\begin{array}{r} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \hline \infty & 250\\ \hline \infty & 5e6\\ \hline \infty & 5e6\\ \hline \infty & 5e5\\ \hline \infty & 2805\\ \hline \infty & 500\\ \hline 16(13)\\ \hline 0 & 250\\ \hline 9224(8531)\\ \hline 3.3(3)\\ 15(11)\\ \hline 5.4(8531)\\ \hline 1.6e{+}0.347\\ \hline 1.5(1.0)\\ \hline 15(11)\\ \hline 5.4(6)\\ 2.7(4)\\ \hline 1.0(0.6)\\ \hline 4.8(6)\\ \hline 50\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 1.6e{+}0.341\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 1.6e{+}0.341\\ \hline 1.6e{+}0.34$</td> <td>#succ 15/13 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 5/15 5/15</td> | IFOFSIACA) HFEs/D HFEs/D HATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPSIACM HFEs/D P20 MATSuMo RANDOM NEWUOA IPOPSIACM HATSUMO RANDOM NEWUOA IPOPSIACM HATSUMO RANDOM NEWUOA IPOPSIACM HES/D F21 MATSUMO RANDOM NEWUOA | $\begin{array}{c} 0.5 \\ \hline 0.6e-l:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.67(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.3(0.9) \\ 1.3(0.9) \\ 1.3(0.9) \\ 1.3(0.9) \\ 1.3(0.9) \\ 1.3(2) \\ 0.5 \\ 0.5e+l:3.6 \\ 1.6(2) \\ 0.5e+l:3.6 \\ 1.6(2)$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 56(58) \\ \infty \\ 55(58) \\ \infty \\ 55(58) \\ 0.250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.33(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.1(2) $ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ 4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1(0.3)\\ 1.8(1)\\ 0.73(0.8)\\ 2.3(2)\\ 3\\ 1.3(2)\\$ | $\begin{array}{r} 10\\ 10\\ 5\\ 4.0e{-}2:307\\ \infty\\ 399(447)\\ 14(13)\\ \infty\\ 255(21)\\ 10\\ 2.5e{+}0:69\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 1.1(1)\\ 4.0(6)\\ 5.2e{+}0:73\\ 1.2(1)\\ 7.7(7)\\ 1.3(1)\\ 1.6(0.5)\\ 1.0(0.5)\\ 1$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \hline \infty & 250\\ \hline \infty & 5e6\\ \hline \infty & 5e6\\ \hline \infty & 5e5\\ \hline \infty & 2805\\ \hline \infty & 500\\ \hline 16(13)\\ \hline 0 & 250\\ \hline 9224(8531)\\ \hline 3.3(3)\\ 15(11)\\ \hline 5.4(8531)\\ \hline 1.6e{+}0.347\\ \hline 1.5(1.0)\\ \hline 15(11)\\ \hline 5.4(6)\\ 2.7(4)\\ \hline 1.0(0.6)\\ \hline 4.8(6)\\ \hline 50\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 1.6e{+}0.341\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 1.6e{+}0.341\\ \hline 1.6e{+}0.34$ | #succ 15/13 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 5/15 5/15 |
| #FEx/D // // MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM // FEx/D // | $\begin{array}{c} 0.5\\ 1.6e+2:4.2\\ 1.3(1)\\ 2.0(2)\\ 2.6(2)\\ 1.2(1)\\ 1.3(2)\\ 3.2(2)\\ 0.5\\ 1.0e+4:4.6\\ 1.7(2)\\ 3.0(3)\\ 2.5(0.6)\\ 1.0(1.0)\\ 0.99(0.7)\\ 2.4(2)\\ 0.5\\ 2.5e+1:20\\ 18(10)\\ 3.7(1)\\ 14(9)\\ 6.8(1)\\ 0.5\\ 2.5e+6:29\\ 1.5(1)\\ 1.6(1)\\ 1.5(1)\\$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.3(1) \\ 1.2 \\ 3.3(1) \\ 1.2 \\ 3.3(1) \\ 1.2 \\ 5.7(2) \\ 1.2 \\ 6.3e+5.7.0 \\ 1.2 \\ 1.5 \\ $ | $\begin{array}{c} 3\\ \hline 3\\ \hline 2.5e+1:20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(1)\\ 1.5(1)\\ 1.5(1)\\ 1.5(1)\\ 1.5(1)\\ 1.5(1)\\ 1.5(1)\\ 1.5(1)\\ 1.5(1)\\ 1.5(1)\\ 3\\ 1.0e+3:18\\ 1.0e+3:18\\ 1.0(0.6)\\$ | $\begin{array}{r} 10 \\ \hline 10 \\ \hline 4.0e+0.54 \\ 7.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 2.2(0.5) \\ 10 \\ \hline 6.3e+1.54 \\ 2.6(1) \\ 482(412) \\ 10(.8) \\ 1.5(0.4) \\ 3.3(3) \\ 2.0(1) \\ 10 \\ \hline 4.0e+0.62 \\ 6.4(75) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 120(95) \\ 3.7(2) \\ 10 \\ \hline 6.3e+3.54 \\ 6.4(4) \\ 102(54) \end{array}$ | $\begin{array}{r} 50 \\ \hline 50 \\ \hline 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.88(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline 1.6e+0.258 \\ \infty 250 \\ \infty 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e+2.256 \\ \infty 250 \\ \infty 5e6 \\ 2.2(1) \\ 2.4(2) \\ \infty 500 \\ 2.3(0.8) \\ \hline 50 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e+1:297 \\ 2.5e+1.5e+1.5e+1.5e+1.5e+1.5e+1.5e+1.5e+1$ | 15/15 15/15 2/15 15/15 2/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 0/15 | HOFSAACM HFEs/D HTSUMO RATSUMO RANDOM NEWUOA Imm-CMA SMAC HOPSAACM HFES/D F20 MATSUMO RANDOM HES/D POSAACM HFES/D F21 MATSUMO RANDOM HEWUOA Imm-CMA SMAC HOPSAACM HEWDOA RANDOM HEWUOA | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline l.6e-l:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.5 \\ 4.0e+l:3.9 \\ 1.3(0.3) \\ 1.4(3) \\ 2.7(2) \\ 1.9(2) \\ 1.8(2) \\ 2.0(2) \\ 0.5 \\ 6.3e+l:3.6 \\ 1.6(2) \\ 2.4(2) \end{array}$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.38(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.7(2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.2 \\ 4.0e+1:15 \\ 1.1(0.9) \\ 3.0(4) \end{array}$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ 4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1(0.3)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ 1.6e+1:31\\ 0.73(0.8)\\ 1.3(2)\\ 1.3(3)\\ 1.3(2)\\ 1.3(3)\\ 1.3(2)\\ 1.3(3)$ | $\begin{array}{r} 10\\ \hline 10\\ \hline \\ 10\\ \hline \\ 5\\ \hline \\ 4.0e-2:307\\ \hline \\ \\ \infty\\ 398(447)\\ 14(13)\\ \hline \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \infty & 250\\ \hline 50\\ \infty & 5e6\\ \infty & 5e5\\ \infty & 2805\\ \infty & 500\\ \hline 1.0e{+}0.851\\ \hline & 0.250\\ 9234(8531)\\ \hline & 0.250\\ 9234(8531)\\ \hline & 0.250\\ 9234(8531)\\ \hline & 0.33(3)\\ 15(11)\\ \hline & 0.500\\ 3.3(3)\\ \hline & 1.6e{+}0.347\\ 1.5(1.0)\\ 15(11)\\ 5.4(6)\\ 2.7(4)\\ 1.6e{+}0.347\\ 1.5(1.6)\\ \hline & 1.6e{+}0.341\\ 2.3(2)\\ 43(15)\\ \hline \end{array}$ | 15/15 15/13 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 5/15 5/15 5/15 5/15 15/15 |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D F100 ATSSUMO RANDOM WHODA | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.2(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5(e+1:20) \\ 18(10) \\ 7845(7036) \\ 2.3(0.6)^{\star} \\ 3.7(1) \\ 14(9) \\ 6.8(1) \\ 0.5 \\ 2.5e+6:2.9 \\ 1.5(1) \\ 1.6(1) \\ 1.$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 1.2(3) \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^* \\ 3.3(1) \\ 1.2(3) \\ 2.3e4(4e4) \\ 2.1(0.9)^* \\ 3.3(1) \\ 1.2(3) \\ 5.7(2) \\ 1.2 \\ 1.6e+5:7.0 \\ 1.9(1) \\ 1.5(2) \\ 1.4(0.6) \\ 1.4(0.6) \\ 1.4(0.6) \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(2) \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(2) \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(2) \\ 1.5(2) \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(2) \\ 1.5$ | $\begin{array}{r} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(0.9)\\ 2.4(2)\\ 3\\ \hline 1.0e+3.18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 1.2(3)\\ 5.0(2)\\ 3\\ 2.5e+5.17\\ 1.4(1.0)\\ 1.6(2)\\ 1.0(0.6)\\ \end{array}$ | $\begin{array}{r} 10 \\ \hline 10 \\ \hline 4.0e+0.54 \\ 7.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 1.6(0.7) \\ 2.2(0.5) \\ \hline 0 \\ 6.3e+1:54 \\ 2.6(1) \\ 482(412) \\ 1(0.8) \\ 1.5(0.4) \\ 3.3(3) \\ 2.0(1) \\ 10 \\ \hline 4.0e+0.62 \\ 64(75) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 120(95) \\ 3.7(2) \\ 10 \\ \hline 6.3e+3:54 \\ 6.4(4) \\ 102(54) \\ 1.8(0.8) \end{array}$ | $\begin{array}{r} 30\\ 50\\ \hline 1.0e+0.324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.88(0.4)\\ 1.2(0.2)\\ 50\\ \hline 1.6e+0.258\\ \infty 250\\ \infty 5e6\\ 1.1(2)\\ 1.7(2)\\ \infty 500\\ 1.8(2)\\ 50\\ \hline 1.6e-2:256\\ \infty 250\\ 0.5e6\\ 2.2(1)\\ 2.4(2)\\ \infty 500\\ 2.3e5(4e5)\\ 50\\ 2.5e+1:297\\ \infty 250\\ 2.5e5(4e5)\\ 2.6(4)\\ \end{array}$ | 15/15 45/15 2/15 15/15 2/15 15/15 15/15 15/15 15/15< | HOFSAACM HEESD HID MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsAACM HFEx/D 20 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsAACM HESZD 21 MATSUMO RANDOM NEWUOA ImposaACM HESZD 22 MATSUMO RANDOM NEWUOA | $\begin{array}{c} 0.5 \\ \hline 0.6e-i:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.67(0.2) \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 1.4(3) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 1.4($ | $\begin{array}{c} 1.2 \\ 1.0e{-}1:242 \\ \hline 0.0e{-}1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e{+}3:8.4 \\ 1.4(1) \\ 0.83(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.7(2) \\ 1.2 \\ 2.5e{+}1:11 \\ 1.3(1) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(1) \\ 1.4(2) \\ 1.8(1) \\ 1.2 \\ 1.09 \\ 3.0(4) \\ 2.1(4) \end{array}$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \\ \infty\\ 1164(1255)\\ 30(35)\\ \\ 98(104)\\ 3\\ 4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.0(3)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ 1.6e+1:31\\ 0.73(0.8)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(3$ | $\begin{array}{r} 10\\ \hline 10\\ \hline 0\\ 5\\ \hline 4.0e-2:307\\ \infty\\ 398(447)\\ 14(13)\\ \infty\\ 25(21)\\ 10\\ \hline 2.5e+0.69\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 10\\ \hline 6.3e+0.73\\ 1.2(1)\\ 7.7(7)\\ 1.3(1)\\ 1.6(0.5)\\ 1.0(0.9)\\ 3.8(4)\\ \hline 1.0\\ 1.0e+1.71\\ 1.1(1)\\ 7.6(13)\\ 2.1(3)\\ \end{array}$ | $\begin{array}{r} 50\\ \hline & 2.5e{-}2.4946\\ \varpropto 250\\ \eqsim 56\\ \eqsim 56\\ \eqsim 56\\ \eqsim 56\\ \eqsim 56\\ \eqsim 56\\ \eqsim 50\\ 16(13)\\ \hline 50\\ 1.6e{+}0.851\\ \eqsim 50\\ \hline 1.6e{+}0.851\\ \eqsim 50\\ \hline 1.6e{+}0.347\\ 1.5(1.0)\\ 1.5(11)\\ 5.4(6)\\ 2.7(4)\\ 1.6(0.6)\\ 4.8(6)\\ \hline 50\\ \hline 1.6e{+}0.341\\ 2.3(2)\\ 2.4(5)\\ \hline \end{array}$ | #succ 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 |
| #FEx/D f7 MATSuMo RANDOM NEWUOA imm-CMA SMAC IPOPsaACM #FEx/D RANDOM NEWUOA imm-CMA SMAC IPOPsaACM #FEx/D #FEx/D MATSUMO RANDOM NEWUOA imm-CMA SMAC IPOPsaACM #FEx/D MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEx/D MATSUMO RANDOM NEWUOA Imm-CMA MATSUMO ANDOM NEWUOA Imm-CMA Imm-CMA MAC RANDOM NEWUOA Imm-CMA Imm-CMA Imm-CMA Imm-CMA Imm-CMA | $\begin{array}{c} 0.5\\ 1.6e+2:4.2\\ 1.3(1)\\ 2.0(2)\\ 2.6(2)\\ 1.2(1)\\ 1.3(2)\\ 3.2(2)\\ 0.5\\ 1.0e+4:4.6\\ 1.7(2)\\ 3.0(3)\\ 2.5(0.6)\\ 1.0(1.0)\\ 0.99(0.7)\\ 2.4(2)\\ 0.5\\ \hline 2.5e+4:20\\ 1.8(10)\\ 7845(7036)\\ 2.3(0.6)^{\star}\\ 3.7(1)\\ 14(9)\\ 6.8(1)\\ 0.5\\ \hline 2.5e+4:2.9\\ 1.5(1)\\ 1.6(1)\\$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^{*} \\ 3.3(1) \\ 1.2(3) \\ 1.2 \\ 5.7(2) \\ 1.2 \\ 6.3e+5.7.0 \\ 1.9(1) \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(1$ | $\begin{array}{c} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1.6)\\ 2.4(2)\\ 3\\ \hline 1.0e+3.18\\ 1.4(0.3)\\ 10(8)\\ 1.0e(1.6)\\ 1.0e(1.6)\\ 1.0e(1.6)\\ 1.10(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.4e(3e4)\\ 1.4e(3e4)\\ 1.4e(3e4)\\ 1.4e(3e4)\\ 1.4e(3e4)\\ 1.4e(3e4)\\ 1.4e(3e4)\\ 1.2(0.8)\\ 2.5e+5.17\\ 1.4(1.0)\\ 1.6(2)\\ 1.0(0.6)\\ 1.1(0.6)\\ \end{array}$ | $\begin{array}{r} 10 \\ \hline 10 \\ \hline 4.0e+0.54 \\ 7.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 1.6(0.7) \\ 2.2(0.5) \\ 10 \\ \hline 6.3e+1.54 \\ 2.6(1) \\ 10 \\ \hline 4.82(412) \\ 10.8) \\ 1.5(0.4) \\ 1.5(0.4) \\ 1.0(.8) \\ 1.5(0.4) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 120(95) \\ 3.7(2) \\ 10 \\ \hline 6.3e+3.54 \\ 6.4(4) \\ 102(54) \\ 1.8(0.8) \\ 1.5(0.5) \end{array}$ | $\begin{array}{r} 50\\ \hline 50\\ l. loc+0.324\\ J. loc+0.324\\ J. 207(1290)\\ 13(15)\\ 0.92(2)\\ 0.98(0.4)\\ 1.2(0.2)\\ \hline 50\\ l. loc-2.250\\ \infty 5e6\\ 1.1(2)\\ 1.7(2)\\ \infty 500\\ 1.8(2)\\ \hline 50\\ l. loc-2.256\\ \infty 250\\ \infty 5e6\\ 2.2(1)\\ 2.4(2)\\ \infty 500\\ 2.3(0.8)\\ \hline 50\\ 2.5e+1.297\\ \infty 250\\ 2.5e5(4e5)\\ 2.6(4)\\ 0.83(0.3)\\ \hline \end{array}$ | 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 | HOFSIACU HFEs/D HFEs/D MATSuMo RANDOM NEWUOA MIDOPSIACH HOPSIACH HOPSIACH HOPSIACH HOPSIACH HOPSIACH HES/D HOPSIACH HES/D HATSUMO RANDOM NEWUOA IND-SIACH HES/D HOPSIACH HO | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-1:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 0.5 \\ \hline 0.5 \\ 6.3e+1:3.6 \\ 1.6(2) \\ 2.4(2) \\ 1.6(2) \\ 2.4(2) \\ 3.4(2) \\ 1.6(2) \\ 3.4(2) \\ 1.6(2) \\ 3.4(2) \\ 1.6(2$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.83(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(1) \\ 1.2 \\ 4.0e+1:15 \\ 1.1(0.9) \\ 3.0(4) \\ 2.1(4) \\ 1.4(1) \\ 0.$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ -80(10,1)\\ 24(10)\\ 1.8(1)\\ 0.73(0.8)\\ 2.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(3)\\ 1.3(2)\\ 1.3(3)\\ 1.3($ | $\begin{array}{c} 10\\ 10\\ 5\\ 4.0e-2:307\\ \infty\\ 98(447)\\ 14(13)\\ \infty\\ 25(228)\\ 1.1(1)\\ 4.0(6)\\ 4.1(3)\\ 251(228)\\ 1.1(1)\\ 4.0(6)\\ 3.2(2)\\ 3.2(2)\\ 10\\ 6.3e+0.73\\ 1.2(1)\\ 7.7(7)\\ 1.3(1)\\ 1.6(0.5)\\ 1.0(0.5)\\ 1.0(0.5)\\ 1.0(0.5)\\ 1.0(0.5)\\ 1.0(1)\\ 2.1(3)\\ 2.5(10)\\ 0\\ 1.0(1)\\ 1$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 2.5e{-}2.4946\\ \hline \infty 250\\ \hline \infty 5c6\\ \hline \infty 5c6\\ \hline \infty 5c5\\ \hline \infty 2805\\ \hline \infty 500\\ \hline 16(13)\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline \infty 250\\ \hline 2234(8531)\\ \hline 3.3(3)\\ 15(11)\\ \hline 5.3(3)\\ \hline 50\\ \hline 1.6e{+}0.347\\ \hline 1.5(11)\\ \hline 5.4(6)\\ \hline 2.7(4)\\ \hline 1.0(0.6)\\ \hline 4.8(6)\\ \hline 0\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 2.4(5)\\ \hline 4.2(4)\\ \hline 0\\ \hline $ | #succ #succ 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 |
| #FEx/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D B MATSuMo NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D Ø MATSuMo #KES/D Ø MATSuMo RANDOM NEWUOA Imm-CMA SMAC POPsaACM #FES/D Ø MATSuMo RANDOM NEWUOA Imm-CMA SMAC POPsaACM #FES/D Ø MATSUMo RANDOM NEWUOA Imm-CMA SMAC | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.2(1) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5e+4:20 \\ 1.8(10) \\ 7845(7036) \\ 2.3(0.6)^{\star} \\ 3.7(1) \\ 14(9) \\ 6.8(1) \\ 0.5 \\ 2.5e+6:2.9 \\ 1.5(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(1) \\ 1.1(0) \\ 2.3(2) \\ 1.3(0.8) \\ \end{array}$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.10(9.9)^{*} \\ 3.3(1) \\ 1.2(3) \\ 5.7(2) \\ 1.2 \\ 6.3e+5:1.0 \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(1) \\ 1$ | $\begin{array}{c} 3\\ \hline 3\\ \hline 2.5e+I:20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(0.9)\\ 2.4(2)\\ 3\\ \hline I.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.4(0.5)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ \hline 3\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^*\\ 2.7(0.5)\\ 12(3)\\ 5.0(2)\\ 3\\ \hline 2.5e+5:17\\ 1.4(1.0)\\ 1.6(2)\\ 1.0(0.6)\\ 1.1(0.6)\\ 0.58(0.7)\\ \hline \end{array}$ | $\begin{array}{r} 10 \\ \hline 10 \\ \hline 4.0e+0.54 \\ 7.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 2.3(3) \\ 2.2(0.5) \\ \hline 10 \\ \hline 6.3e+1.54 \\ 2.6(1) \\ 482(412) \\ 1(0.8) \\ 1.5(0.4) \\ 3.3(3) \\ 2.0(1) \\ \hline 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2e6(2e6) \\ 2.2(1) \\ 3.7(2) \\ 10 \\ \hline 6.3e+3.54 \\ 6.4(4) \\ 102(54) \\ 1.8(0.8) \\ 1.5(0.5) \\ 2.5(2) \\ \hline \end{array}$ | $\begin{array}{r} 50 \\ \hline 50 \\ \hline 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.98(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline 1.6e+0.258 \\ \infty 250 \\ \infty 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e+2.256 \\ \infty 250 \\ \infty 5e6 \\ 2.2(1) \\ 2.4(2) \\ \infty 500 \\ 2.3(0.8) \\ \hline 50 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e(4e5) \\ 2.5e(4e5) \\ 2.6(4) \\ 0.83(0.3) \\ \infty 500 \\ \hline \end{array}$ | 15/15 #succ 15/15 215 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 0/15 15/15 15/15 15/15 15/15 15/15 | HOPSIACA) HFEs/D HFEs/D HFEs/D HOPSIACA H | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-I:172 \\ \infty \\ 4.2cs(4c5) \\ 1308(2380) \\ \overline{55}(56) \\ \infty \\ 280(359) \\ 0.5 \\ c.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.5 \\ c.3e+J:3.6 \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\ $ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.33(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 14(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.2 \\ 1$ | 3 6.3e-2:67: ∞ 1164(1255) 30(35) ∞ 98(104) 3 4.0e+1:15 1.9(0.7) 2.4(10) 1(0.3) 1.8(1) 0.73(0.3) 2.3(2) 1.3(2) 0.33(0.3) 1.3(2) 0.93(0.8) 1.3(2) 1.3(2) 0.93(0.8) 1.3(2) 1.3(3) 1.3(3) 1.3(3) 1.3(2) 1.3(2) 1.3(3) 1.3(3) 1.3(2) 1.3(3) 1.3(3) 1.3(2) 1.3(3) 1.3(3) 1.3(2) 1.3(3) | $\begin{array}{r} 10\\ \hline 10\\ \hline$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \hline \infty & 250\\ \hline \infty & 5e6\\ \hline \infty & 5e5\\ \hline \infty & 2805\\ \hline \infty & 500\\ \hline 16(13)\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline \infty & 250\\ \hline 9234(8531)\\ \hline 3.3(3)\\ \hline 15(11)\\ \hline \infty & 500\\ \hline 3.5(3)\\ \hline 50\\ \hline 1.6e{+}0.347\\ \hline 1.5(1.0)\\ \hline 5.4(6)\\ 2.7(4)\\ \hline 1.6(0.5)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 4.3(15)\\ 2.4(5)\\ \hline 2.4(5)\\ 2.4(5)\\ \hline 4.2(4)\\ \hline 1.0(0.8)\\ \hline 120(0)\\ \hline 120$ | #succ 15/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FES/D MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FES/D f10 MATSUMO NEWUOA Imm-CMA SMAC IPOPsaACM #EE/D MATSUMO NEWUOA Imm-CMA SMAC IPOPsaACM #FE/D GIO ATSUMO NEWUOA Imm-CMA SMAC IPOPsaACM | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(3) \\ 2.5(0.6) \\ 1.0(0.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5e+4:20 \\ 1.5(1) \\ 1.6(1) \\ 0.5 \\ 1.3(0.8) \\ 2.5(2) \\ 1.5(1) \\ 1.6(1) \\ 1.6(1) \\ 1.3(0.8) \\ 2.0(5) \\ 0.5 \\ $ | $\begin{array}{c} 12 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^* \\ 3.3(1) \\ 1.2(3) \\ 5.7(2) \\ 1.2 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.9(1) \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(1) \\ 0.80(0.4) \\ 2.0(1) \\ 1.2 \\$ | $\begin{array}{c} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(0.9)\\ 2.2(4)\\ 1.5(0.9)\\ 2.2(4)\\ 3\\ 1.0e+3.18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 1.2(3)\\ 5.0(2)\\ 3\\ 2.5e+5.17\\ 1.4(1.0)\\ 1.6(2)\\ 1.0(0.6)\\ 1.1(0.6)\\ 0.58(0.7)\\ 1.5(1)\\ 2\end{array}$ | $\begin{array}{r} 10 \\ \hline 10 \\ \hline 4.0e+0.54 \\ 7.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 1.6(0.7) \\ 2.2(0.5) \\ \hline 0 \\ 6.3e+1.54 \\ 2.6(1) \\ 482(412) \\ 1(0.8) \\ 1.5(0.4) \\ 3.3(3) \\ 2.0(1) \\ \hline 10 \\ \hline 4.0e+0.62 \\ 64(75) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 120(95) \\ 3.7(2) \\ 10 \\ \hline 6.3e+3.54 \\ 6.4(4) \\ 102(54) \\ 1.8(0.8) \\ 1.5(0.5) \\ 2.5(2) \\ 2.4(0.8) \\ 1.5(0.5) \\ 2.5(2) \\ 2.4(0.8) \\ 1.0 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 10 \\ 1$ | $\begin{array}{r} 30 \\ \hline 50 \\ \hline 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.88(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline 1.6e+0.258 \\ \infty 250 \\ \infty 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e-2:256 \\ \infty 250 \\ 0.8500 \\ 2.4(2) \\ \infty 500 \\ 2.4(2) \\ \infty 500 \\ 2.5e+1:297 \\ \infty 250 \\ 0.85(4e5) \\ 2.5(4) \\ 0.83(0.3) \\ \infty 500 \\ 0.85(0.2) \\ 0.85(0.2) \\ 50 \\ \hline \end{array}$ | 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 15/15 | HOPSAACM #FEs/D HIDOPSAACM MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM #FEs/D P20 MATSUMO RANDOM #FEs/D P21 MATSUMO RANDOM #FEs/D POPSAACM #FES/D POPSAACM #FES/D POPSAACM #FES/D | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-1:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.5 \\ 0.5 \\ 4.0e+1:3.9 \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.3(0.2) \\ 1.4(3) \\ 2.7(2) \\ 1.3(0.2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(1) \\ 0.5 \\ 1.4(1) \\ 0.5 \\ 1.4(1) \\ 0.5 \\ 1.4(1) \\ $ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.38(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \\ \infty\\ 1164(1255)\\ 30(35)\\ \\ 98(104)\\ 3\\ 4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.0(.7)\\ 24(10)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ 1.6e+1:15\\ 1.3(2)\\ 1.3(3)\\ 1.3(2)\\ 1.3(5)\\$ | $\begin{array}{r} 10\\ \hline 10\\ \hline$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 8 & 2.5e-2.4946\\ \infty & 250\\ \infty & 5e6\\ \infty & 500\\ \hline 1.0e+0.851\\ \infty & 250\\ 9234(8531)\\ 3.3(3)\\ 15(11)\\ \infty & 500\\ 3.5(3)\\ 50\\ \hline 1.6e+0.347\\ 1.5(1.0)\\ 15(11)\\ 5.4(6)\\ 2.7(4)\\ 1.6(0.6)\\ 4.8(6)\\ 50\\ \hline 1.6e+0.341\\ 2.3(2)\\ 4.3(15)\\ 2.4(5)\\ 4.2(4)\\ 1.6(0.8)\\ 13(4)\\ 50\\ \end{array}$ | #succ 15/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 1 |
| #FEx/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEx/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEx/D Ø MATSUMO RANDOM NEWUOA Inm-CMA SMAC IPOPsaACM #FEx/D MATSUMO RANDOM NEWUOA Inm-CMA SMAC IPOPsaACM #FEx/D f0 MATSUMO RANDOM NEWUOA Inm-CMA SMAC IPOPsaACM #FEx/D f0 | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.2(1) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5e+4:20 \\ 1.5(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(3) \\ 2.3(2) \\ 1.3(0.8) \\ 2.0(5) \\ 0.5 \\ 1.0e+6:30 \\ 0.5 \\ $ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.1(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e(4(4e4) \\ 2.1(0.9)^{*} \\ 3.3(1) \\ 12(3) \\ 5.7(2) \\ 1.2 \\ 6.3e+5.7.0 \\ 1.9(1) \\ 1.5(1) \\ 0.80(0.4) \\ 2.0(1) \\ 1.2 \\ 0.6(1+4:6) \\ $ | $\begin{array}{c} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1.6)\\ 2.4(2)\\ 3\\ \hline 1.0e+3.18\\ 1.4(0.3)\\ 10(8)\\ 1.0e(1.6)\\ 1.0e($ | $\begin{array}{r} 10 \\ \hline 10 \\ \hline 4.0e+0.54 \\ 7.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 1.6(0.7) \\ 2.2(0.5) \\ 10 \\ \hline 6.3e+1.54 \\ 2.6(1) \\ 482(412) \\ 1(0.8) \\ 1.5(0.4) \\ 1.5(0.4) \\ 1.3(3) \\ 2.0(1) \\ 10 \\ \hline 4.0e+0.62 \\ 6.4(75) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2e(2e6) \\ 1.2e(2e$ | $\begin{array}{r} 30 \\ \hline 50 \\ \hline 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.98(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline 1.6e+0.288 \\ \infty 250 \\ \infty 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e-2:256 \\ \infty 250 \\ \infty 5e6 \\ 2.2(1) \\ 2.4(2) \\ \infty 500 \\ 2.3e+1:297 \\ \infty 250 \\ 2.5e+4:297 \\ \infty 250 \\ 2.5e+4:297 \\ \infty 250 \\ 2.5e+4:297 \\ \infty 500 \\ 2.5e+4:297 \\ \infty 500 \\ 2.5e+4:297 \\ \infty 250 \\ 0.83(0.3) \\ \infty 500 \\ 0.83(0.3) \\ \infty 500 \\ 0.85(0.2) \\ 50 \\ \hline 6 \ begin{tabular}{lllllllllllllllllllllllllllllllllll$ | 15/15 15/15 </td <td>HOFSAACM HFEs/D HFEs/D HOPSAACM HOPSAACM HOPSAACM HOPSAACM HES/D H</td> <td>$\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline l.6e-l:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0,7) \\ 1.2(0,1) \\ 0.57(0,2) \\ 1.8(2) \\ 0.57(0,2) \\ 1.8(2) \\ 0.57(0,2) \\ 1.8(2) \\ 0.57(1,2) \\ 1.8(2) \\ 0.57(1,2) \\ 1.8(2) \\ 0.57(1,2) \\ 1.8(2) \\ 0.57(1,2) \\ 1.8(2) \\ 0.57(1,2) \\ 1.8($</td> <td>$\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.33(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(1) \\ 1.2 \\ 4.0e+1:15 \\ 1.1(0.9) \\ 1.2 \\ 1.2 \\ 4.0e+1:15 \\ 1.1(0.9) \\ 1.2 \\ 1.2 \\ 4.0e+1:15 \\ 1.1(0.9) \\ 1.2$</td> <td>$\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ -3\\ -4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1(0.3)\\ 1.8(1)\\ 0.73(0.8)\\ 1.3(2)\\ 0.33(0.8)\\ 1.3(2)\\ 1.3(2)\\ 0.93(0.8)\\ 1.0(0.9)\\ 1.1(0.5)\\ 3\\ 2.5e+1:32\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.9(1)\\ 1.5(2)\\ 3\\ -4.0e+0:33\\ -4.0e+0:33$</td> <td>$\begin{array}{r} 10\\ 10\\ 5\\ 4.0e-2:307\\ \infty\\ 398(447)\\ 14(13)\\ \infty\\ 25(21)\\ 10\\ 2.5e+0.69\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 1.1(1)\\ 4.0(6)\\ 3.2(2)\\ 1.2(1)\\ 7.7(7)\\ 1.3(1)\\ 1.6(0.5)\\ 1.0(0.5)\\ 1$</td> <td>$\begin{array}{r} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \propto 2.50\\ \hline 50\\ \hline 0.5e5\\ \propto 5e6\\ \propto 5e5\\ \propto 2.805\\ \hline 0.5e5\\ \propto 2.805\\ \hline 0.5e{+}0.851\\ \hline 0.5e{+}0.851\\ \hline 0.5e{+}0.851\\ \hline 0.5e{+}0.851\\ \hline 0.5e{+}0.347\\ \hline 1.5(11)\\ \hline 5.4(6)\\ \hline 1.6e{+}0.347\\ \hline 1.5(11)\\ \hline 5.4(6)\\ \hline 1.6e{+}0.347\\ \hline 1.5(11)\\ \hline 5.4(6)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 2.4(5)\\ \hline 2.4(5)\\ \hline 2.4(5)\\ \hline 2.4(5)\\ \hline 1.0e{+}0.518\\ \hline 0\\ \hline 1.0e{+}0.518\\ \hline 0\\ \hline$</td> <td>#succ 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15</td> | HOFSAACM HFEs/D HFEs/D HOPSAACM HOPSAACM HOPSAACM HOPSAACM HES/D H | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline l.6e-l:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0,7) \\ 1.2(0,1) \\ 0.57(0,2) \\ 1.8(2) \\ 0.57(0,2) \\ 1.8(2) \\ 0.57(0,2) \\ 1.8(2) \\ 0.57(1,2) \\ 1.8(2) \\ 0.57(1,2) \\ 1.8(2) \\ 0.57(1,2) \\ 1.8(2) \\ 0.57(1,2) \\ 1.8(2) \\ 0.57(1,2) \\ 1.8($ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.33(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(1) \\ 1.2 \\ 4.0e+1:15 \\ 1.1(0.9) \\ 1.2 \\ 1.2 \\ 4.0e+1:15 \\ 1.1(0.9) \\ 1.2 \\ 1.2 \\ 4.0e+1:15 \\ 1.1(0.9) \\ 1.2$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ -3\\ -4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1(0.3)\\ 1.8(1)\\ 0.73(0.8)\\ 1.3(2)\\ 0.33(0.8)\\ 1.3(2)\\ 1.3(2)\\ 0.93(0.8)\\ 1.0(0.9)\\ 1.1(0.5)\\ 3\\ 2.5e+1:32\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.8(5)\\ 1.3(0.7)\\ 1.9(1)\\ 1.5(2)\\ 3\\ -4.0e+0:33\\ -4.0e+0:33$ | $\begin{array}{r} 10\\ 10\\ 5\\ 4.0e-2:307\\ \infty\\ 398(447)\\ 14(13)\\ \infty\\ 25(21)\\ 10\\ 2.5e+0.69\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 1.1(1)\\ 4.0(6)\\ 3.2(2)\\ 1.2(1)\\ 7.7(7)\\ 1.3(1)\\ 1.6(0.5)\\ 1.0(0.5)\\ 1$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \propto 2.50\\ \hline 50\\ \hline 0.5e5\\ \propto 5e6\\ \propto 5e5\\ \propto 2.805\\ \hline 0.5e5\\ \propto 2.805\\ \hline 0.5e{+}0.851\\ \hline 0.5e{+}0.851\\ \hline 0.5e{+}0.851\\ \hline 0.5e{+}0.851\\ \hline 0.5e{+}0.347\\ \hline 1.5(11)\\ \hline 5.4(6)\\ \hline 1.6e{+}0.347\\ \hline 1.5(11)\\ \hline 5.4(6)\\ \hline 1.6e{+}0.347\\ \hline 1.5(11)\\ \hline 5.4(6)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 2.4(5)\\ \hline 2.4(5)\\ \hline 2.4(5)\\ \hline 2.4(5)\\ \hline 1.0e{+}0.518\\ \hline 0\\ \hline 1.0e{+}0.518\\ \hline 0\\ \hline $ | #succ 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15 |
| #FEx/D f7 MATSuMo RANDOM NEWUGA imm-CMA SMAC IPOPsaACM #EEx/D B MATSUMo NEWUGA imm-CMA SMAC IPOPsaACM #EEx/D Ø MATSUMO RANDOM NEWUGA Imm-CMA SMAC IPOPsaACM #EEx/D MATSUMO RANDOM RANDOM MATSUMO RANDOM MATSUMO RANDOM MATSUMO MACSUMO MARAC IPOPsaACM #FEx/D #T11 | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.2(1) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0,7) \\ 2.4(2) \\ 0.5 \\ 2.5e+4:20 \\ 1.8(10) \\ 7845(7036) \\ 2.3(0.6)^* \\ 3.7(1) \\ 14(9) \\ 6.8(1) \\ 0.5 \\ 2.5e+6:2.9 \\ 1.5(1) \\ 1.6(1$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^* \\ 3.3(1) \\ 12(3) \\ 5.7(2) \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 2.5(2) \\ 1.2 \\ 2.5(2) \\ 1.2 \\ 2.5(2) \\ 1.2 \\ 2.5(2) \\ 1.2 \\ 2.5(2) \\ 1.2 \\ 2.5(2) \\ 1.2 \\ 1.2 \\ 2.5(2) \\ 1.2 \\ 1.2 \\ 2.5(2) \\ 1.2 \\ 1.2 \\ 2.5(2) \\ 1.2 \\ 1.2 \\ 2.5(2) \\ 1.2 \\ 1.2 \\ 1.2 \\ 2.5(2) \\ 1.2 \\ 1.2 \\ 1.2 \\ 2.5(2) \\ 1.2 \\ 1.2 \\ 1.2 \\ 1.2 \\ 2.5(2) \\ 1.2 $ | $\begin{array}{r} 3\\ \hline 3\\ \hline 2.5e+1:20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1.6)\\ 2.4(2)\\ 3\\ \hline 1.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1:35\\ 35(26)\\ 4.1e4(3e4)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 2.7(0.5)\\ 12(3)\\ 5.0(2)\\ 3\\ \hline 2.5e+5:17\\ 1.4(1.0)\\ 1.6(2)\\ 3\\ \hline 2.5e+5:17\\ 1.4(1.0)\\ 1.6(2)\\ 1.0(0.6)\\ 1.1(0.6)\\ 0.58(0.7)\\ 1.5(1)\\ 3\\ \hline 6.3e+2:16\\ 4.7(2) \end{array}$ | $\begin{array}{r} 10\\ \hline 10\\ \hline 4.0e+0.54\\ 7.6(14)\\ 151(135)\\ 7.6(13)\\ 2.3(3)\\ 1.6(0.7)\\ 2.2(0.5)\\ 10\\ \hline 6.3e+1.754\\ 2.6(1)\\ 482(412)\\ 1(0.8)\\ 1.5(0.4)\\ 3.3(3)\\ 2.0(1)\\ \hline 10\\ \hline 4.0e+0.62\\ 64(75)\\ 1.2e6(2e6)\\ 2.2(1)\\ 2.7(0.9)\\ 1.2e6(2e6)\\ 6.3e+3.754\\ 6.4(4)\\ 102(54)\\ 1.8(0.8)\\ 1.5(0.5)\\ 2.5(2)\\ 2.4(0.8)\\ 1.6(0.5)\\ 2.5(2)\\ 2.4(0.8)\\ 10\\ \hline 6.3e+1.74\\ 8.9(12)\\ 10\\ \hline \end{array}$ | $\begin{array}{r} 30 \\ \hline 50 \\ \hline 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.98(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline 1.6e+0.258 \\ \infty \ 250 \\ \infty \ 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty \ 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e+2.256 \\ \infty \ 250 \\ \infty \ 5e6 \\ 2.2(1) \\ 2.4(2) \\ \infty \ 500 \\ 2.3e(4.5) \\ 2.5e(4.5) \\$ | [15] [15] [15] <td>HOFSIACH HFEs/D HT9 MATSuMo RANDOM NEWUOA Imm-CMA SMAC HOPSsAACM HES/D RANDOM NEWUOA Imm-CMA SMAC IPOPssACM HTES/D RANDOM NEWUOA Imm-CMA SMAC IPOPssACM HES/D T21 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPssACM HFEs/D T22 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPssACM HES/D T23 MATSUMO RANDOM NEWUOA Imm-CMA SMAC</td> <td>$\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-I:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.67(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.5 \\ 6.3e+I:3.6 \\ 1.6(2) \\ 2.4(2) \\ 3.4(2) \\ 1.6(2) \\ 1.8(2) \\ 1.8(2) \\ 1.4(1) \\ 0.5 \\ 1.0e+I:3.0 \\ 1.8(1) \\ 1.0e+I:3.0$</td> <td>$\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.33(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\$</td> <td>$\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ -4.0e+l:15\\ 1.9(0.7)\\ 24(10)\\ 1(0.3)\\ 1.8(1)\\ 0.73(0.8)\\ 2.3(2)\\ 3\\ 1.6e+l:31\\ 0.73(0.8)\\ 1.3(2)\\$</td> <td>$\begin{array}{r} 10\\ 10\\ \hline 1$</td> <td>$\begin{array}{r} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \propto 2.50\\ \hline 50\\ \hline 50\\ \hline 50\\ \hline 50\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline 50\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline 50\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline 50\\ \hline 1.6e{+}0.347\\ \hline 1.5(11)\\ \hline 5.4(6)\\ 2.7(4)\\ \hline 1.0(0.6)\\ \hline 1.6e{+}0.341\\ 2.3(2)\\ \hline 2.4(5)\\ 2.4(5)\\ 2.4(5)\\ 2.4(5)\\ 2.4(5)\\ 2.4(5)\\ 1.0(0.8)\\ \hline 1.0e{+}0.518\\ \hline 50\\ \hline 1.0e{+}0.518\\ \hline 50\\ \hline 1.0e{+}0.518\\ \hline 50\\ \hline 50\\ \hline 1.0e{+}0.518\\ \hline 50\\ \hline$</td> <td>#succ 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 </td> | HOFSIACH HFEs/D HT9 MATSuMo RANDOM NEWUOA Imm-CMA SMAC HOPSsAACM HES/D RANDOM NEWUOA Imm-CMA SMAC IPOPssACM HTES/D RANDOM NEWUOA Imm-CMA SMAC IPOPssACM HES/D T21 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPssACM HFEs/D T22 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPssACM HES/D T23 MATSUMO RANDOM NEWUOA Imm-CMA SMAC | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-I:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.67(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.5 \\ 6.3e+I:3.6 \\ 1.6(2) \\ 2.4(2) \\ 3.4(2) \\ 1.6(2) \\ 1.8(2) \\ 1.8(2) \\ 1.4(1) \\ 0.5 \\ 1.0e+I:3.0 \\ 1.8(1) \\ 1.0e+I:3.0 $ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.33(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ $ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ -4.0e+l:15\\ 1.9(0.7)\\ 24(10)\\ 1(0.3)\\ 1.8(1)\\ 0.73(0.8)\\ 2.3(2)\\ 3\\ 1.6e+l:31\\ 0.73(0.8)\\ 1.3(2)\\ $ | $\begin{array}{r} 10\\ 10\\ \hline 1$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \propto 2.50\\ \hline 50\\ \hline 50\\ \hline 50\\ \hline 50\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline 50\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline 50\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline 50\\ \hline 1.6e{+}0.347\\ \hline 1.5(11)\\ \hline 5.4(6)\\ 2.7(4)\\ \hline 1.0(0.6)\\ \hline 1.6e{+}0.341\\ 2.3(2)\\ \hline 2.4(5)\\ 2.4(5)\\ 2.4(5)\\ 2.4(5)\\ 2.4(5)\\ 2.4(5)\\ 1.0(0.8)\\ \hline 1.0e{+}0.518\\ \hline 50\\ \hline 1.0e{+}0.518\\ \hline 50\\ \hline 1.0e{+}0.518\\ \hline 50\\ \hline 50\\ \hline 1.0e{+}0.518\\ \hline 50\\ \hline$ | #succ 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOP-suACM #FEs/D RANDOM NEWUOA Imm-CMA SMAC IPOP-suACM #FEs/D Ø MATSUMO RANDOM NEWUOA Imm-CMA SMAC PIOP-suACM #FEs/D f10 MATSUMO RANDOM NEWUOA Imm-CMA SMAC POP-suACM #FEs/D f10 MATSUMO MATSUMO RANDOM | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.2(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5e+t-120 \\ 18(10) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5e+t-120 \\ 18(10) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5e+t-20 \\ 1.5(1) \\ 1.6(1) \\ 0.5 \\ 2.5e+6:2.9 \\ 1.5(1) \\ 1.6(1) \\ 1.6(1) \\ 1.3(0.8) \\ 2.0(5) \\ 0.5 \\ 1.0e+6:3.0 \\ 1.4(2) \\ 1.8(2) \\ 0.5 \\ 0.5 \\ 1.0e+6:3.0 \\ 1.4(2) \\ 1.8(2) \\ 0.5 \\ 0.5 \\ 1.0e+6:3.0 \\ 1.4(2) \\ 0.5 \\ 0.5 \\ 1.0e+6:3.0 \\ 1.4(2) \\ 0.5 \\ 0.5 \\ 0.5 \\ 1.0e+6:3.0 \\ 1.4(2) \\ 0.5 \\ 0$ | $\begin{array}{c} 12\\ 1.0e+2:6.2\\ 1.8(1)\\ 2.9(0.8)\\ 2.2(0.2)\\ 1.3(0.8)\\ 1.1(0.8)\\ 2.9(2)\\ 1.2\\ 6.3e+3:6.8\\ 1.9(1)\\ 2.2(3)\\ 1.8(0.1)\\ 0.96(1.0)\\ 0.96(1.0)\\ 0.96(1.0)\\ 0.96(1.0)\\ 0.96(1.0)\\ 0.96(1.0)\\ 1.2\\ 1.6e+1:26\\ 3.4(51)\\ 2.3e4(4e4)\\ 2.1(0.9)^*\\ 3.3(1)\\ 12(3)\\ 5.7(2)\\ 1.2\\ 6.3e+5:7.0\\ 1.9(1)\\ 1.5(2)\\ 1.4(0.6)\\ 1.5(1)\\ 0.80(0.4)\\ 2.0(1)\\ 1.2\\ 6.3e+4:6.2\\ 2.5(2)\\ 2.5(1)\\ 1.2\\ 1.2\\ 1.2\\ 1.2\\ 1.2\\ 1.2\\ 1.2\\ 1.2$ | $\begin{array}{c} 3\\ \hline 3\\ \hline 2.5e+1:20\\ 1.5(0.6)\\ \hline 8.8(6)\\ 2.2(3)\\ \hline 1.5(1)\\ 1.5(0.9)\\ 2.4(2)\\ \hline 3\\ \hline 1.0e+3:18\\ \hline 1.4(0.3)\\ 10(8)\\ \hline 1.0(0.6)\\ \hline 1.6(0.6)\\ \hline 1.6(0.6)\\ \hline 1.6(0.6)\\ \hline 1.6(0.8)\\ 2.1(2)\\ \hline 3\\ \hline 5.0(2)\\ \hline 3\\ 2.7(0.5)\\ \hline 1.2(3)\\ \hline 5.0(2)\\ \hline 3\\ \hline 2.5e+5:17\\ \hline 1.4(1.0)\\ \hline 1.6(2)\\ \hline 1.0(0.6)\\ \hline 1.1(0.6)\\ \hline 0.58(0.7)\\ \hline 1.5(1)\\ \hline 3\\ \hline 6.3e+2:16\\ \hline 4.7(2)\\ 6.8(5)\\ \hline \end{array}$ | $\begin{array}{r} 10\\ \hline 10\\ \hline 4.0e+0.54\\ 7.6(14)\\ 151(135)\\ 7.6(13)\\ 2.3(3)\\ 1.6(0.7)\\ 2.2(0.5)\\ \hline 10\\ \hline 6.3e+1.54\\ 2.6(1)\\ 482(412)\\ 1(0.8)\\ 1.5(0.4)\\ 3.3(3)\\ 2.0(1)\\ \hline 1.2e6(2e6)\\ 2.2(1)\\ 2.7(0.9)\\ 1.2e6(2e6)\\ 2.2(1)\\ 2.7(0.9)\\ 1.2e6(2e6)\\ 3.7(2)\\ \hline 10\\ \hline 6.3e+3.54\\ 6.4(4)\\ 102(54)\\ 18(0.8)\\ 1.5(0.5)\\ 2.5(2)\\ 2.4(0.8)\\ 1.5(0.5)\\ 2.5(2)\\ 2.4(0.8)\\ 10\\ \hline 6.3e+1.74\\ 8.9(12)\\ 17(15)\\ \end{array}$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 1.0e+0.324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.98(0.4)\\ 1.2(0.2)\\ \hline 50\\ \hline 1.6e+0.258\\ \infty 250\\ \infty 5e6\\ \hline 1.1(2)\\ 1.7(2)\\ \infty 500\\ 1.1(2)\\ 1.7(2)\\ \infty 500\\ 1.1(2)\\ 1.7(2)\\ \infty 500\\ 1.6e+2.256\\ \infty 250\\ \infty 5e6\\ \hline 2.2(1)\\ 2.4(2)\\ \infty 500\\ 2.3(0.8)\\ \hline 50\\ 2.5e+1:297\\ \infty 250\\ 2.5e+1:298\\ \infty 250\\ 1.2e(2e5)\\ \hline \end{array}$ | [15/15] Mate 15/15 2/15 15/15 </td <td>HOPSIACM HFEs/D HFEs/D HATSuMo RANDOM NEWUOA Imm-CMA SMAC HPOPSIACM HFES/D HOPSIACM HFES/D HOPSIACM HFES/D HOPSIACM HOPSIACM HES/D HOPSIACM HES/D HOPSIACM HES/D HOPSIACM HES/D HOPSIACM HO</td> <td>$\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-I:172 \\ \infty \\ 4.2cs(4c5) \\ 1308(2380) \\ \overline{5}s(56) \\ \infty \\ 280(359) \\ 0.5 \\ c.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 2.0(2) \\ 0.5 \\ c.3e+I:3.6 \\ 1.6(2) \\ 2.0(2) \\ 0.5 \\ c.3e+I:3.6 \\ 1.6(2) \\ 1.8(2) \\ 2.0(2) \\ 0.5 \\ c.3e+I:3.6 \\ 1.6(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.6(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 1.8($</td> <td>$\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.38(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\$</td> <td>$\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \\ \hline \\ 6.3e-2:67:\\ \infty\\ \\ 98(104)\\ 3\\ 0.98(104)\\ 3\\ 3\\ 0.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.0(.3)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ 1.6e+1:31\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ 1.6e+1:31\\ 0.73(0.3)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 1$</td> <td>$\begin{array}{r} 10\\ \hline 10\\ \hline$</td> <td>$\begin{array}{r} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \hline \infty & 250\\ \hline \infty & 5e6\\ \hline \infty & 5e5\\ \hline \infty & 2805\\ \hline \infty & 500\\ \hline 16(13)\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline \infty & 250\\ \hline 9234(8531)\\ \hline 3.3(3)\\ \hline 15(11)\\ \hline \infty & 500\\ \hline 3.5(3)\\ \hline 50\\ \hline 1.6e{+}0.347\\ \hline 1.5(1.0)\\ \hline 15(11)\\ \hline 5.4(6)\\ 2.7(4)\\ \hline 1.6(0.5)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 4.3(15)\\ 2.4(5)\\ \hline 1.6e{+}0.518\\ \hline \infty & 250\\ \hline 1.0e{+}0.518\\ \hline \end{array}$</td> <td>#succ 15/15 0/15</td> | HOPSIACM HFEs/D HFEs/D HATSuMo RANDOM NEWUOA Imm-CMA SMAC HPOPSIACM HFES/D HOPSIACM HFES/D HOPSIACM HFES/D HOPSIACM HOPSIACM HES/D HOPSIACM HES/D HOPSIACM HES/D HOPSIACM HES/D HOPSIACM HO | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-I:172 \\ \infty \\ 4.2cs(4c5) \\ 1308(2380) \\ \overline{5}s(56) \\ \infty \\ 280(359) \\ 0.5 \\ c.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 2.0(2) \\ 0.5 \\ c.3e+I:3.6 \\ 1.6(2) \\ 2.0(2) \\ 0.5 \\ c.3e+I:3.6 \\ 1.6(2) \\ 1.8(2) \\ 2.0(2) \\ 0.5 \\ c.3e+I:3.6 \\ 1.6(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.6(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 1.8(1) \\ 2.3(2) \\ 1.8(1) \\ 1.8($ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.38(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ $ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \\ \hline \\ 6.3e-2:67:\\ \infty\\ \\ 98(104)\\ 3\\ 0.98(104)\\ 3\\ 3\\ 0.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.0(.3)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ 1.6e+1:31\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ 1.6e+1:31\\ 0.73(0.3)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 1.3(2)\\ 0.93(0.8)\\ 1.3(2)\\ 1$ | $\begin{array}{r} 10\\ \hline 10\\ \hline$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \hline \infty & 250\\ \hline \infty & 5e6\\ \hline \infty & 5e5\\ \hline \infty & 2805\\ \hline \infty & 500\\ \hline 16(13)\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline \infty & 250\\ \hline 9234(8531)\\ \hline 3.3(3)\\ \hline 15(11)\\ \hline \infty & 500\\ \hline 3.5(3)\\ \hline 50\\ \hline 1.6e{+}0.347\\ \hline 1.5(1.0)\\ \hline 15(11)\\ \hline 5.4(6)\\ 2.7(4)\\ \hline 1.6(0.5)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 4.3(15)\\ 2.4(5)\\ \hline 1.6e{+}0.518\\ \hline \infty & 250\\ \hline 1.0e{+}0.518\\ \hline \end{array}$ | #succ 15/15 0/15 |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f10 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f11 MATSUMO RANDOM NEWUOA ima-CMA SMAC IPOPsaACM #FEs/D f11 MATSUMO RANDOM NEWUOA #ANDOM SMAC IPOPsaACM #ES/D MATSUMO <td< td=""><td>$\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5e+6:2.9 \\ 1.5(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(1) \\ 2.3(2) \\ 1.0e+6:3.0 \\ 1.4(2) \\ 0.5 \\ 1.0e+6:3.0 \\ 1.4(2) \\ 1.8(2) \\ 1.5(1) \\ 1.6(2) \\ 1.6(1)$</td><td>$\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.2(2) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 2.9(2) \\ 1.2 \\ 1.6e+1:26 \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^* \\ 3.3(1) \\ 1.2 \\ 2.3e4(4e4) \\ 2.1(0.9)^* \\ 3.3(1) \\ 1.2 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(1) \\ 0.80(0.4) \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.8(9.9) \\ 3.9(9) \\ 3.9(1) \\ 1.8$</td><td>$\begin{array}{r} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(0.9)\\ 2.2(3)\\ 1.5(1)\\ 1.5(0.9)\\ 2.2(42)\\ 3\\ 1.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.4(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ 1.0e+1.35\\ 35(26)\\ 35(26)\\ 35(26)\\ 1.4(1.0)\\ 1.4(1.0)\\ 1.2(0.5)\\ 1.$</td><td>$\begin{array}{r} 10 \\ \hline 10 \\ \hline 4.0e+0.54 \\ 7.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 1.6(0.7) \\ 2.2(0.5) \\ 10 \\ \hline 6.3e+1.54 \\ 2.6(1) \\ 482(412) \\ 10.8) \\ 1.5(0.4) \\ 1.266(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2e6(2e6) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(1.9) \\ 1.2e6(2e6) \\ 1.$</td><td>$\begin{array}{r} 30 \\ \hline 50 \\ \hline 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.988(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline 1.6e+0.258 \\ \infty 566 \\ 1.1(2) \\ 1.7(2) \\ \infty 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e-2.256 \\ \infty 250 \\ 0.566 \\ 2.2(1) \\ 2.4(2) \\ \infty 500 \\ 2.3(0.8) \\ \hline 50 \\ 2.5e+1:297 \\ \infty 250 \\ 1.26(2e) \\ 50 \\ 0.85(0.2) \\ \hline 50 \\ 0.85(0.2) \\ 50 \\ 0.5(2e) \\ 1.26(2e) \\ 3.5(0.8) \\ 0.5(2e) \\ 1.26(2e) \\ 3.5(0.8) \\ 0.5(2e) \\ 1.26(2e) \\ 3.5(0.8) \\ 0.5(2e) \\ 0.5(2e)$</td><td>11/11 15/15<!--</td--><td>HOFSAACM HEESD HIPOPSAACM WATSUMO RANDOM NEWUOA IMM-CMA SMAC HOPSAACM HEESD MATSUMO RANDOM NEWUOA IMM-CMA SMAC IPOPSAACM HEESD HOPSAACM HEESD HOPSAACM HEESD HOPSAACM HEESD HOPSAACM HEESD HOPSAACM HEESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HOPSAACM HOPSAACM HESD HOPSAACM HOP</td><td>$\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-i:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 2.30(7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 1.2($</td><td>$\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0,1) \\ 0.33(0,4) \\ 0.44(0,2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0,3) \\ 1.4(0,6) \\ 1.4(2) \\ 1.8(2) \\$</td><td>$\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ 4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.0(3)\\ 1.8(1)\\ 0.73(0.8)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(3)\\ 1.3(2)\\ 1.3(3)\\ 1.3(2)\\ 1.3(3)\\ 1.3(2)\\ 1.3(3)\\ 1.$</td><td>$\begin{array}{r} 10\\ \hline 10\\ \hline 10\\ \hline 10\\ \hline 10\\ \hline 10\\ \hline 5\\ \hline 10\\ \hline 0\\ \hline 0\\ \hline 0\\ \hline 0\\ \hline 0\\ \hline 0\\ \hline$</td><td>$\begin{array}{r} 50\\ \hline & 2.5e{-}2.4946\\ \propto 2.50\\ \hline & 2.5e{-}2.4946\\ \propto 2.50\\ \hline & 5e6\\ \propto 5.e6\\ \propto 5.e5\\ \propto 2.805\\ \propto 5.00\\ \hline & 50\\ \hline & 1.0e{+}0.851\\ \hline & 2.50\\ \hline & 9234(8531)\\ \hline & 3.3(3)\\ 15(11)\\ \hline & 5.00\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ 15(11)\\ 5.4(6)\\ \hline & 50\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ 15(11)\\ \hline & 5.0\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ 15(11)\\ \hline & 5.0\\ \hline & 1.6e{+}0.518\\ \hline & \infty 2.50\\ \hline & 49(32)\\ \hline & 2.4(4)\\ \hline & 90\\ \hline & 1.0e{+}0.518\\ \hline & \infty 2.50\\ \hline & 49(32)\\ \hline & 2.4(4)\\ \hline & 10(6)\\ \hline &$</td><td>#succ 15/15/15/15/15/15/15/15/15/15/15/15/15/1</td></td></td<> | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5e+6:2.9 \\ 1.5(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(1) \\ 1.6(1) \\ 2.3(2) \\ 1.0e+6:3.0 \\ 1.4(2) \\ 0.5 \\ 1.0e+6:3.0 \\ 1.4(2) \\ 1.8(2) \\ 1.5(1) \\ 1.6(2) \\ 1.6(1) $ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.2(2) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 2.9(2) \\ 1.2 \\ 1.6e+1:26 \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^* \\ 3.3(1) \\ 1.2 \\ 2.3e4(4e4) \\ 2.1(0.9)^* \\ 3.3(1) \\ 1.2 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(1) \\ 0.80(0.4) \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.8(9.9) \\ 3.9(9) \\ 3.9(1) \\ 1.8$ | $\begin{array}{r} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(0.9)\\ 2.2(3)\\ 1.5(1)\\ 1.5(0.9)\\ 2.2(42)\\ 3\\ 1.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.4(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ 1.0e+1.35\\ 35(26)\\ 35(26)\\ 35(26)\\ 1.4(1.0)\\ 1.4(1.0)\\ 1.2(0.5)\\ 1.$ | $\begin{array}{r} 10 \\ \hline 10 \\ \hline 4.0e+0.54 \\ 7.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 1.6(0.7) \\ 2.2(0.5) \\ 10 \\ \hline 6.3e+1.54 \\ 2.6(1) \\ 482(412) \\ 10.8) \\ 1.5(0.4) \\ 1.266(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2e6(2e6) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(1.9) \\ 1.2e6(2e6) \\ 1.$ | $\begin{array}{r} 30 \\ \hline 50 \\ \hline 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.988(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline 1.6e+0.258 \\ \infty 566 \\ 1.1(2) \\ 1.7(2) \\ \infty 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e-2.256 \\ \infty 250 \\ 0.566 \\ 2.2(1) \\ 2.4(2) \\ \infty 500 \\ 2.3(0.8) \\ \hline 50 \\ 2.5e+1:297 \\ \infty 250 \\ 1.26(2e) \\ 50 \\ 0.85(0.2) \\ \hline 50 \\ 0.85(0.2) \\ 50 \\ 0.5(2e) \\ 1.26(2e) \\ 3.5(0.8) \\ 0.5(2e) \\ 1.26(2e) \\ 3.5(0.8) \\ 0.5(2e) \\ 1.26(2e) \\ 3.5(0.8) \\ 0.5(2e) \\ 0.5(2e)$ | 11/11 15/15 </td <td>HOFSAACM HEESD HIPOPSAACM WATSUMO RANDOM NEWUOA IMM-CMA SMAC HOPSAACM HEESD MATSUMO RANDOM NEWUOA IMM-CMA SMAC IPOPSAACM HEESD HOPSAACM HEESD HOPSAACM HEESD HOPSAACM HEESD HOPSAACM HEESD HOPSAACM HEESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HOPSAACM HOPSAACM HESD HOPSAACM HOP</td> <td>$\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-i:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 2.30(7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 1.2($</td> <td>$\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0,1) \\ 0.33(0,4) \\ 0.44(0,2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0,3) \\ 1.4(0,6) \\ 1.4(2) \\ 1.8(2) \\$</td> <td>$\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ 4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.0(3)\\ 1.8(1)\\ 0.73(0.8)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(3)\\ 1.3(2)\\ 1.3(3)\\ 1.3(2)\\ 1.3(3)\\ 1.3(2)\\ 1.3(3)\\ 1.$</td> <td>$\begin{array}{r} 10\\ \hline 10\\ \hline 10\\ \hline 10\\ \hline 10\\ \hline 10\\ \hline 5\\ \hline 10\\ \hline 0\\ \hline 0\\ \hline 0\\ \hline 0\\ \hline 0\\ \hline 0\\ \hline$</td> <td>$\begin{array}{r} 50\\ \hline & 2.5e{-}2.4946\\ \propto 2.50\\ \hline & 2.5e{-}2.4946\\ \propto 2.50\\ \hline & 5e6\\ \propto 5.e6\\ \propto 5.e5\\ \propto 2.805\\ \propto 5.00\\ \hline & 50\\ \hline & 1.0e{+}0.851\\ \hline & 2.50\\ \hline & 9234(8531)\\ \hline & 3.3(3)\\ 15(11)\\ \hline & 5.00\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ 15(11)\\ 5.4(6)\\ \hline & 50\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ 15(11)\\ \hline & 5.0\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ 15(11)\\ \hline & 5.0\\ \hline & 1.6e{+}0.518\\ \hline & \infty 2.50\\ \hline & 49(32)\\ \hline & 2.4(4)\\ \hline & 90\\ \hline & 1.0e{+}0.518\\ \hline & \infty 2.50\\ \hline & 49(32)\\ \hline & 2.4(4)\\ \hline & 10(6)\\ \hline &$</td> <td>#succ 15/15/15/15/15/15/15/15/15/15/15/15/15/1</td> | HOFSAACM HEESD HIPOPSAACM WATSUMO RANDOM NEWUOA IMM-CMA SMAC HOPSAACM HEESD MATSUMO RANDOM NEWUOA IMM-CMA SMAC IPOPSAACM HEESD HOPSAACM HEESD HOPSAACM HEESD HOPSAACM HEESD HOPSAACM HEESD HOPSAACM HEESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HESD HOPSAACM HOPSAACM HOPSAACM HESD HOPSAACM HOP | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-i:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 2.30(7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 1.2($ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0,1) \\ 0.33(0,4) \\ 0.44(0,2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0,3) \\ 1.4(0,6) \\ 1.4(2) \\ 1.8(2) \\ $ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ 4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.0(3)\\ 1.8(1)\\ 0.73(0.8)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(3)\\ 1.3(2)\\ 1.3(3)\\ 1.3(2)\\ 1.3(3)\\ 1.3(2)\\ 1.3(3)\\ 1.$ | $\begin{array}{r} 10\\ \hline 10\\ \hline 10\\ \hline 10\\ \hline 10\\ \hline 10\\ \hline 5\\ \hline 10\\ \hline 0\\ \hline 0\\ \hline 0\\ \hline 0\\ \hline 0\\ \hline 0\\ \hline $ | $\begin{array}{r} 50\\ \hline & 2.5e{-}2.4946\\ \propto 2.50\\ \hline & 2.5e{-}2.4946\\ \propto 2.50\\ \hline & 5e6\\ \propto 5.e6\\ \propto 5.e5\\ \propto 2.805\\ \propto 5.00\\ \hline & 50\\ \hline & 1.0e{+}0.851\\ \hline & 2.50\\ \hline & 9234(8531)\\ \hline & 3.3(3)\\ 15(11)\\ \hline & 5.00\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ 15(11)\\ 5.4(6)\\ \hline & 50\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ 15(11)\\ \hline & 5.0\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ 15(11)\\ \hline & 5.0\\ \hline & 1.6e{+}0.518\\ \hline & \infty 2.50\\ \hline & 49(32)\\ \hline & 2.4(4)\\ \hline & 90\\ \hline & 1.0e{+}0.518\\ \hline & \infty 2.50\\ \hline & 49(32)\\ \hline & 2.4(4)\\ \hline & 10(6)\\ \hline &$ | #succ 15/15/15/15/15/15/15/15/15/15/15/15/15/1 |
| #FEx/D f7 MATSuMo RANDOM NEWUOA imm-CMA SMAC IPOPsa/ACM #FEx/D RANDOM NEWUOA imm-CMA SMAC IPOPsa/ACM #FEx/D #FEx/D MATSUMO RANDOM NEWUOA imm-CMA SMAC IPOPsa/ACM #FEx/D f10 MATSUMO RANDOM NEWUOA imm-CMA SMAC POPsa/ACM #FEx/D f11 MATSUMO RANDOM WEVUOA imm-CMA SMAC POPsa/ACM #Etx/D f11 MATSUMO NEWUOA imm-CMA SMAC | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(1) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ \hline 2.5e+4:20 \\ 1.8(10) \\ 7845(7036) \\ 2.3(2, 6) \\ 1.0(1.0) \\ 1.0(1.0) \\ 0.5 \\ \hline 2.5e+4:20 \\ 1.0(1.0) \\ 1.0(1$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6(e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.14(0.9)^{*} \\ 3.3(1) \\ 1.2 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 1.5(1) \\ 0.80(0.4) \\ 2.0(1) \\ 1.2 \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(1) \\ 0.80(0.4) \\ 2.0(1) \\ 1.2 \\ 2.5(2) \\ 2.5(2) \\ 2.5(1) \\ 1.8(0.9) \\ 2.1(2) \\ 0.90(0.9) \\ 1.2 \\ 0.$ | $\begin{array}{c} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1.6)\\ 2.4(2)\\ 3\\ \hline 1.0e+3.18\\ 1.4(0.3)\\ 10(8)\\ 1.9(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 2.7(0.5)\\ 12(3)\\ 3\\ 5.0(2)\\ 3\\ \hline 2.5e+5.17\\ 1.4(1.0)\\ 1.6(2)\\ 1.0(0.6)\\ 1.6(2)\\ 1.0(0.6)\\ 1.6(2)\\ 1.0(0.6)\\ 1.6(2)\\ 1.0(0.6)\\ 1.1(0.6)\\ 0.58(0.7)\\ 1.5(1)\\ 3\\ \hline 6.3e+2:16\\ 4.7(2)\\ 6.8(5)\\ 1.5(0.4)\\ 2.6(1)\\ 1.9(1)$ | $\begin{array}{r} 10 \\ \hline 10 \\ \hline 4.0e+0.54 \\ 7.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 1.6(0.7) \\ 2.2(0.5) \\ 10 \\ \hline 6.3e+1.54 \\ 2.6(1) \\ 482(412) \\ 1(0.8) \\ 1.5(0.4) \\ 1.5(0.4) \\ 1.5(0.4) \\ 1.2c6(2c6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2c6(2c6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2c6(2c6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2c6(2c6) \\ 2.2(1) \\ 3.7(2) \\ 3.7(2) \\ 1.8(0.8) \\ 1.5(0.5) \\ 2.5(2) \\ 2.5(2) \\ 2.6(2) \\ 1.8(0.8) \\ 1.5(0.5) \\ 2.5(2) \\ 2.5(2) \\ 2.6(2) \\ 1.8(0.8) \\ 1.5(0.5) \\ 2.5(2) \\ 2.5(2) \\ 2.6(2) \\ 1.5(0.5) \\ 2.5(2) \\ 1.5(0.5) \\ 1.5($ | $\begin{array}{r} 30 \\ \hline 50 \\ \hline l.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.98(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline l.6e+0.258 \\ \infty 250 \\ \infty 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e-2.256 \\ \infty 250 \\ \infty 5e6 \\ 2.2(1) \\ 2.4(2) \\ \cos 500 \\ 1.8(2) \\ \hline 50 \\ \hline 2.5e+1.297 \\ \infty 250 \\ 2.5e5(4e5) \\ 2.6(4) \\ 0.83(0.3) \\ \infty 500 \\ 0.85(0.2) \\ \hline 50 \\ \hline 6.3e-1.298 \\ \infty 250 \\ 1.2e5(2e5) \\ 3.5(0.8) \\ 1.3(0.3) \\ \infty 500 \\ \hline \end{array}$ | 115/15 15/15< | HOFSIACU HFESD HFESD HTSUMO RANDOM NEWUOA Imm-CMA SMAC HOPSIACM HESD MATSUMO RANDOM NEWUOA Imm-CMA SMAC HOPSIACM HESD T21 MATSUMO RANDOM NEWUOA Imm-CMA SMAC HOPSIACM HFESD T23 MATSUMO RANDOM NEWUOA Imm-CMA SMAC | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-I:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+J:5.1 \\ 1.7(2) \\ 2.80(359) \\ 0.5 \\ 6.3e+J:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.5 \\ \hline 0.5 \\ 4.0e+J:3.9 \\ 1.3(0.9) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 0.5 \\ \hline 0.5 \\ 6.3e+J:3.6 \\ 1.6(2) \\ 1.8(2) \\ 2.4(2) \\ 1.8(2) \\ 1.$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0,1) \\ 0.83(0,4) \\ 0.44(0,2) \\ 1.7(2) \\ 1.2 \\ 1.5(0,1) \\ 0.33(0,4) \\ 0.44(0,2) \\ 1.7(2) \\ 1.2 \\ 1.2 \\ 1.4(1) \\ 1.4(1) \\ 1.4(1) \\ 1.4(1) \\ 1.4(1) \\ 1.4(1) \\ 1.4(1) \\ 1.4(1) \\ 1.4(1) \\ 1.4(1) \\ 1.4(1) \\ 1.4(1) \\ 1.5(0,9) \\ 1.2 \\ 1.2 \\ 6.3e+\theta 9.0 \\ 1.7(2) \\ 2.5(1) \\ 6.4(13) \\ 2.6(5) \\ 2.9(2) \end{array}$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ -8(104)\\ -3\\ -8(105)\\ -3\\ -8(105)\\ -3\\ -8(105)\\ -3\\ -3\\ -3\\ -3\\ -3\\ -3\\ -3\\ -3\\ -3\\ -3$ | $\begin{array}{r} 10\\ 10\\ \hline 1$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 2.5e{-}2.4946\\ \propto 2.50\\ \hline 50\\ \hline 50\\ \hline 50\\ \hline 50\\ \hline 1.6e{+}0.851\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline 50\\ \hline 1.6e{+}0.347\\ \hline 1.5(11)\\ \hline 5.4(6)\\ \hline 50\\ \hline 1.6e{+}0.347\\ \hline 1.5(11)\\ \hline 5.4(6)\\ \hline 2.7(4)\\ \hline 1.0(0.6)\\ \hline 4.8(6)\\ \hline 1.6e{+}0.341\\ \hline 2.3(2)\\ \hline 1.0e{+}0.518\\ \hline \infty 250\\ \hline 1.0e{+}0.518\\ \hline \infty 250\\ \hline 49(32)\\ \hline 2.4(4)\\ \hline 10(6)\\ \hline \infty 500\\ \hline \end{array}$ | issi issi |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D Ø MATSUMO ASMAC IPOPsaACM #FEs/D Ø MATSUMO NEWUOA Imm-CMA SMAC PIOPsaACM #FEs/D ID MATSUMO NEWUOA Imm-CMA SMAC POPsaACM #FEs/D ID MATSUMO RANDOM NEWUOA Imm-CMA SMAC POPsaACM MATSUMO RANDOM NEWUOA Inm-CMA SMAC IPOPsaACM PUPOPs | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.2(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5e+4:20 \\ 1.8(10) \\ 7845(7036) \\ 2.3(0.6)^{\star} \\ 3.7(1) \\ 14(9) \\ 6.8(1) \\ 0.5 \\ 2.5e+6:2.9 \\ 1.5(1) \\ 1.6(1) \\ 1.6(1) \\ 1.3(0.8) \\ 2.0(5) \\ 0.5 \\ 1.0e+6:3.0 \\ 1.4(2) \\ 1.4(3) \\ 0.73(0.5) \\ 2.3(3) \\ 0.73(0.5) \\ 2.3(3) \\ 0.73(0.5) \\ 2.3(3) \\ 0.5$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^* \\ 3.3(1) \\ 12(3) \\ 5.7(2) \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 2.5(1) \\ 1.8(0.9) \\ 2.1(1) \\ 0.80(0.4) \\ 2.0(1) \\ 1.2 \\ 0.3e+4:6.2 \\ 2.5(2) \\ 2.5(1) \\ 1.8(0.9) \\ 2.1(2) \\ 0.94(0.9) \\ 2.7(4) \\ 0.91(1) \\ $ | $\begin{array}{r} 3\\ \hline 3\\ \hline 2.5e+1:20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(1)\\ 1.5(0.9)\\ 2.4(2)\\ 3\\ \hline 1.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.4(0.5)\\ 1.0(0.6)\\ 1.4(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^*\\ 2.7(0.5)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 3\\ 2.5e+5:17\\ 1.4(1.0)\\ 1.6(2)\\ 1.0(0.6)\\ 1.1(0.6)\\ 0.58(0.7)\\ 1.5(1)\\ 3\\ \hline 6.3e+2:16\\ 4.7(2)\\ 6.8(5)\\ 1.5(0.4)\\ 2.6(1)\\ 1.9(1)\\ 6.7(8)\\ \end{array}$ | 10 10 $4.0e+0.54$ 7.6(14) $151(135)$ 7.6(13) 2.3(3) 1.6(0.7) 2.2(0.5) 10 6.3e+1.54 2.6(1) 482(412) 1(0.8) 1.5(0.4) 3.3(3) 2.0(1) 10 4.0e+0.62 64(75) 1.2e6(2e6) 2.2(1) 2.7(0.9) 1.2e(6(2e6) 2.2(1) 2.7(0.9) 1.2(0(5) 3.7(2) 10 6.3e+3.54 6.4(4) 102(54) 1.8(0.8) 1.5(0.5) 2.5(2) 2.4(0.8) 1.5(0.5) 2.5(2) 2.4(0.8) 1.5(0.5) 2.5(2) 2.4(0.8) 1.5(0.5) 1.2e(2.5(2) 2.4(0.8) 1.5(0.5) 1.2(1,1) 1.5(1 | $\begin{array}{r} 30 \\ \hline 50 \\ \hline 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.98(0.4) \\ 1.2(0.2) \\ 50 \\ \hline 1.6e+0.258 \\ \infty 250 \\ \infty 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty 500 \\ 1.8(2) \\ 50 \\ \hline 1.6e+2.256 \\ \infty 250 \\ \infty 5e6 \\ 2.2(1) \\ 2.4(2) \\ \infty 500 \\ 2.3(0.8) \\ 50 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e(4) \\ 0.83(0.3) \\ \infty 500 \\ 0.85(0.2) \\ 50 \\ \hline 6.3e+1:298 \\ \infty 250 \\ 1.2e5(2e5) \\ 3.5(0.8) \\ 1.2e5(2e5) \\ 3.5(0.8) \\ 1.3(0.3) \\ \infty 500 \\ 1.2e5(2e5) \\ 3.5(0.8) \\ 1.3(0.3) \\ \infty 500 \\ 1.2e5(2e5) \\ 3.5(0.8) \\ 1.3(0.3) \\ \infty 500 \\ 1.2e5(2e5) \\ 3.5(0.8) \\ 1.3(0.3) \\ \infty 500 \\ 1.2(2e5) \\ 3.5(0.8) \\ 1.3(0.3) \\ \infty 500 \\ 1.2(2e5) \\ 3.5(0.8) \\ 1.3(0.3) \\ \infty 500 \\ 1.2(2e5) \\ 3.5(0.8) \\ 1.3(0.3) \\ \infty 500 \\ 1.2(2e5) \\ 3.5(0.8) \\ 1.2(2e5) \\ 1.2(2e5) \\ 3.5(0.8) \\ 1.2(2e5) \\ 1.2$ | 11/11 15/15 </td <td>HOPSIACLI, HFES/D HFES/D HOPSIACK HOPSI</td> <td>$\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-I:172 \\ \infty \\ 4 2cs(4cs) \\ 1308(2380) \\ \overline{5s}(56) \\ \infty \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\$</td> <td>$\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.38(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 10(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(1) \\ 1.2 \\ 6.3e+0:9.0 \\ 1.7(2) \\ 2.5(1) \\ 6.4(13) \\ 2.6(5) \\ 2.9(2) \\ 2.9(2) \end{array}$</td> <td>3 6.3e-2:67: ∞ 1164(1255) 30(35) ∞ 98(104) 3 4.0e+1:15 1.9(0.7) 24(10) 1(0.3) 1.8(1) 0.73(0.3) 2.3(2) 1.3(2) 3 4.0e+0:33 2.4(3) 1.6(1) 2.9(3) 2.6(4) 2.6(4) 2.8(3)</td> <td>$\begin{array}{r} 10\\ \hline 10\\ \hline$</td> <td>$\begin{array}{r} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \simeq 250\\ \simeq 5e6\\ \simeq 5e6\\ \simeq 5805\\ \simeq 5805\\ \simeq 5805\\ \simeq 5805\\ \simeq 5805\\ \simeq 590\\ 16(13)\\ \hline 50\\ 1.0e{+}0.851\\ \simeq 250\\ 9234(8531)\\ \hline 3.3(3)\\ 15(11)\\ \simeq 500\\ \hline 3.5(3)\\ \hline 50\\ \hline 1.6e{+}0.347\\ 1.5(1.0)\\ 15(11)\\ 5.4(6)\\ 2.7(4)\\ 1.6(1)\\ 5.4(6)\\ 2.7(4)\\ 1.6(1)\\ 5.4(6)\\ 2.7(4)\\ 1.6(1)\\ 5.4(6)\\ 2.7(4)\\ 1.6(1)\\ 5.4(6)\\ 2.7(4)\\ 1.6(1)\\ 5.5(1)\\ \hline 1.6e{+}0.341\\ 2.3(2)\\ 4.3(1)\\ 2.4(4)\\ 1.0(0.8)\\ 13(2)\\ 2.4(4)\\ 10(6)\\ \simeq 550\\ 4.3(2)\\ 2.4(4)\\ 10(6)\\ \simeq 550\\ 1.3(2)\\ 2.4(4)\\ 10(6)\\ \simeq 550\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.5(1)\\$</td> <td>#succ #succ 15/15 0/15 0/15 0/15 0/15 0/15 15/15</td> | HOPSIACLI, HFES/D HFES/D HOPSIACK HOPSI | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-I:172 \\ \infty \\ 4 2cs(4cs) \\ 1308(2380) \\ \overline{5s}(56) \\ \infty \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\ 2.0(2) \\ 1.8(2) \\$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.38(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 10(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(1) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(1) \\ 1.2 \\ 6.3e+0:9.0 \\ 1.7(2) \\ 2.5(1) \\ 6.4(13) \\ 2.6(5) \\ 2.9(2) \\ 2.9(2) \end{array}$ | 3 6.3e-2:67: ∞ 1164(1255) 30(35) ∞ 98(104) 3 4.0e+1:15 1.9(0.7) 24(10) 1(0.3) 1.8(1) 0.73(0.3) 2.3(2) 1.3(2) 3 4.0e+0:33 2.4(3) 1.6(1) 2.9(3) 2.6(4) 2.6(4) 2.8(3) | $\begin{array}{r} 10\\ \hline 10\\ \hline$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 8 & 2.5e{-}2.4946\\ \simeq 250\\ \simeq 5e6\\ \simeq 5e6\\ \simeq 5805\\ \simeq 5805\\ \simeq 5805\\ \simeq 5805\\ \simeq 5805\\ \simeq 590\\ 16(13)\\ \hline 50\\ 1.0e{+}0.851\\ \simeq 250\\ 9234(8531)\\ \hline 3.3(3)\\ 15(11)\\ \simeq 500\\ \hline 3.5(3)\\ \hline 50\\ \hline 1.6e{+}0.347\\ 1.5(1.0)\\ 15(11)\\ 5.4(6)\\ 2.7(4)\\ 1.6(1)\\ 5.4(6)\\ 2.7(4)\\ 1.6(1)\\ 5.4(6)\\ 2.7(4)\\ 1.6(1)\\ 5.4(6)\\ 2.7(4)\\ 1.6(1)\\ 5.4(6)\\ 2.7(4)\\ 1.6(1)\\ 5.5(1)\\ \hline 1.6e{+}0.341\\ 2.3(2)\\ 4.3(1)\\ 2.4(4)\\ 1.0(0.8)\\ 13(2)\\ 2.4(4)\\ 10(6)\\ \simeq 550\\ 4.3(2)\\ 2.4(4)\\ 10(6)\\ \simeq 550\\ 1.3(2)\\ 2.4(4)\\ 10(6)\\ \simeq 550\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.3(2)\\ 1.5(1)\\$ | #succ #succ 15/15 0/15 0/15 0/15 0/15 0/15 15/15 |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FES/D MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FES/D f10 MATSUMO NEWUOA Imm-CMA SMAC IPOPsaACM #FES/D MATSUMO NEWUOA Imm-CMA SMAC IPOPsaACM #FES/D MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #HES/D GI MATSUMO RANDOM NEWUOA Imm-CMA | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.090(0.7) \\ 2.4(2) \\ 0.5 \\ \hline 1.25e+6:2.9 \\ 1.5(1) \\ 1.4(9) \\ 6.8(1) \\ 0.5 \\ \hline 1.2e+6:2.9 \\ 1.5(1) \\ 1.4(2) \\ 0.5 \\ \hline 1.0e+6:3.0 \\ 1.4(2) \\ 1.4(3) \\ 0.73(0.5) \\ 2.3(5) \\ 0.5 \\ \hline 0.5 \\ 0.5 \\ \hline 0.5 \\ \hline 0.5 \\ 0.5 \\ \hline 0.5 \\ 0.5 \\ \hline 0.5 \\ \hline 0.5 \\ 0.5 \\ \hline 0.5 \\ 0.5 \\ \hline 0.5 \\ 0.5 \\ \hline 0$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^* \\ 3.3(1) \\ 1.2(3) \\ 5.7(2) \\ 1.2 \\ 6.3e+5:7.0 \\ 1.5(2) \\ 1.40(.6) \\ 1.5(1) \\ 0.80(0.4) \\ 2.5(1) \\ 1.8(0.9) \\ 2.1(2) \\ 0.94(0.9) \\ 2.7(4) \\ 1.2 \\ \end{array}$ | $\begin{array}{c} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1)\\ 1.5(0.9)\\ 2.2(4)\\ 3\\ 1.0e+3.18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 1.2(0.5)\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 1.2(0.5)\\ 35(26)\\ 3.5(26)\\ 3.5(26)\\ 1.5(0.4)\\ 1.5(1)\\ 3\\ 6.3e+2.16\\ 6.8(5)\\ 1.5(0.4)\\ 2.6(1)\\ 1.9(1)\\ 6.7(8)\\ 3\\ \end{array}$ | $\begin{array}{r} 10 \\ \hline 10 \\ \hline 4.0e+0.54 \\ 7.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 1.6(0.7) \\ 2.2(0.5) \\ \hline 10 \\ 6.3e+1:54 \\ 2.6(1) \\ 482(412) \\ 1(0.8) \\ 1.5(0.4) \\ 3.3(3) \\ 2.0(1) \\ 10 \\ \hline 4.0e+0.62 \\ 64(75) \\ 1.2e6(2e6) \\ 2.2(1) \\ 1.2e6(2e6) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2e6(2e6) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.4(0.8) \\ 1.5(0.5) \\ 2.5(2) \\ 2.4(0.8) \\ 1.5(0.5) \\ 2.5(2) \\ 2.4(0.8) \\ 1.5(0.5) \\ 2.5(2) \\ 2.4(0.8) \\ 1.5(1) \\ 1.2e6(2e6) \\ 1.2e6(2e$ | $\begin{array}{r} 30\\ \hline 50\\ \hline 1.0e+6.324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.98(0.4)\\ 1.2(0.2)\\ \hline 50\\ \hline 1.6e+0.258\\ \infty 250\\ \infty 5e6\\ 1.1(2)\\ 1.7(2)\\ \infty 500\\ 1.8(2)\\ \hline 50\\ \hline 1.6e-2.256\\ \infty 250\\ 1.8(2)\\ \hline 50\\ \hline 2.4(2)\\ \infty 500\\ 2.3(0.8)\\ \hline 50\\ 2.5e+1:297\\ \infty 250\\ 2.5e+1:297\\ \infty 250\\ 2.5e+1:297\\ \infty 250\\ 2.5e+1:297\\ \infty 250\\ 0.85(0.2)\\ \hline 50\\ \hline 6.5e-1:298\\ \infty 250\\ 1.2e(2e5)\\ 3.5(0.8)\\ 1.3(0.3)\\ \infty 500\\ 1.1(0.2)\\ \hline 50\\ \end{array}$ | 1[5]15 15/15 2/15 2/15 15/15 15/15 15/15 15/15 | IFOFSAACM #FE3/D #FE3/D MATSUMO RANDOM NEWUOA Imm-CMA SMAC HOPsaACM #FE3/D <u>720</u> MATSUMO RANDOM NEWUOA Imm-CMA SMAC HOPsaACM #FE3/D <u>721</u> MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FE3/D <u>722</u> MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FE3/D <u>723</u> MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FE3/D 723 MATSUMO RANDOM | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-i:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.057(0.2) \\ 1.2(0.1) \\ 0.057(0.2) \\ 1.2(0.1) \\ 0.057(0.2) \\ 1.2(0.1) \\ 0.057(0.2) \\ 1.2(0.1) \\ 0.057(0.2) \\ 1.2(0.1) \\ 0.057(0.2) \\ 1.2(0.1) \\ 0.057(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.2(0.1)$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.33(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.7(2) \\ 1.7(2) \\ 1.2 \\ 1.8(1) \\ 1.8(2$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \\ 98(104)\\ 3\\ 4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.0(3)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ 1.6e+1:31\\ 0.73(0.8)\\ 1.3(2)\\ 0.93(0.8)\\ 1.0(0.9)\\ 1.1(0.5)\\ 3\\ 2.5e+1:32\\ 1.1(0.5)\\ 1.3(6)\\ 1.3(5)\\ 1.3(6)\\ 1.3(5)\\ 1.3(6)\\ 1.3$ | $\begin{array}{r} 10\\ 10\\ \hline 1$ | $\begin{array}{c} 50\\ \hline & 2.5e{-}2.4946\\ \varpropto 250\\ \hline & 250\\ \hline & 566\\ \hline & 5e5\\ \hline & 5e5\\ \hline & 560\\ \hline & 500\\ \hline & 500\\ \hline & 1.6e{+}0.851\\ \hline & 250\\ \hline & 9234(8531)\\ \hline & 3.3(3)\\ \hline & 15(11)\\ \hline & & 500\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ \hline & 1.5(1.1)\\ \hline & 5.00\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ \hline & 1.6(1)\\ \hline & 50\\ \hline & 1.6e{+}0.341\\ \hline & 2.3(2)\\ \hline & 2.4(5)\\ \hline & 2.4(5)\\ \hline & 2.4(5)\\ \hline & 2.4(5)\\ \hline & 1.6e{+}0.518\\ \hline & & 0\\ \hline & 1.0e{+}0.518\\ \hline & & 0\\ \hline \hline & & 0\\ \hline \hline & & 0\\ \hline & & 0\\ \hline & & 0\\ \hline \hline \hline & & 0\\ \hline \hline \hline & & 0\\ \hline \hline \hline \hline & & 0\\ \hline \hline \hline \hline \hline & & 0\\ \hline \hline$ | #succ #succ 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 #succ 5/15 5/15 15/15 |
| #FEs/D r MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D Ø MATSUMO RANDOM NEWUOA Inm-CMA SMAC IPOPsaACM #FEs/D mATSUMO RANDOM NEWUOA Inm-CMA SMAC IPOPsaACM #FEs/D fl1 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #EFs/D Ø FI2 | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.2(1) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 1.0(1.0) \\$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 2.9(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.2(3) \\ 1.2 \\ 1.2(3) \\ 1.2 \\ 1.2 \\ 1.2(3) \\ 1.2 \\ 1$ | $\begin{array}{c} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1.6)\\ 1.5(1.6)\\ 2.4(2)\\ 3\\ \hline 1.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.0(0.6)\\ 1.0(0.6)\\ 1.0(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.4(1.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.4(1.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1.35\\ 35(26)\\ 1.2(0.8)\\ 2.5e+5:17\\ 1.4(1.0)\\ 1.6(2)\\ 1.0(0.6)\\ 1.1(0.6)\\ 0.58(0.7)\\ 1.5(0.4)\\ 2.6(1)\\ 1.9(1)\\ 6.7(8)\\ \hline 3\\ 4.0e+6:19\\ \hline \end{array}$ | $\begin{array}{r} 10 \\ \hline 10 \\ \hline 4.0e+0.54 \\ 7.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 1.6(0.7) \\ 2.2(0.5) \\ 10 \\ \hline 6.3e+1.54 \\ 2.6(1) \\ 482(412) \\ 1(0.8) \\ 1.5(0.4) \\ 1.5(0.4) \\ 1.3(3) \\ 2.0(1) \\ 10 \\ \hline 4.0e+0.62 \\ 64(75) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2e(2e6) \\ 1.2e6(2e6) \\ 1.2e$ | $\begin{array}{r} 30 \\ \hline 50 \\ \hline 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.98(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline 1.6e+0.286 \\ \infty 250 \\ \infty 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e-2:256 \\ \infty 250 \\ \infty 5e6 \\ 2.2(1) \\ 2.4(2) \\ \infty 500 \\ 2.3(0.8) \\ \hline 50 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e+1:298 \\ \infty 250 \\ 1.2e5(2e5) \\ 50 \\ \hline 6.3e-1:298 \\ \infty 250 \\ 1.2e5(2e5) \\ 3.5(0.8) \\ 1.3(0.3) \\ \infty 500 \\ 1.3(0.3) \\ \infty 500 \\ 1.2e5(2e5) \\ 1.2e5(2e5) \\ 1.2e5(2e5) \\ 3.5(0.8) \\ 1.3(0.3) \\ \infty 500 \\ 1.1(0.2) \\ 50 \\ \hline \end{array}$ | 1[57]15 15715 | HOFSAACM #FE3/D MATSUMO RANDOM NEWUOA NEWUOA MATSUMO F20 MATSUMO RANDOM HEEVD MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM #FE2/D 72 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM #FE3/D 72 MATSUMO RANDOM REWUOA Imm-CMA SMAC IPOPSAACM #FE3/D 72 MATSUMO RANDOM REWUOA Imm-CMA SMAC IPOPSAACM #FE3/D 72 MATSUMO RANDOM REWUOA Imm-CMA SMAC | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-I:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 56.3e+J:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 1.4$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3.8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.33(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(1) \\ 1.2 \\ 4.0e+1:15 \\ 1.1(0.9) \\ 1.9(2) \\ 1.2 \\ 6.3e+0.90 \\ 1.7(2) \\ 2.5(1) \\ 6.4(13) \\ 2.6(5) \\ 2.9(2) \\ 2.9(2) \\ 2.9(2) \\ 2.9(2) \\ 1.2 \\ 4.0e+1:37 \\ 1.2 \\ 1.$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \\ \hline \\ 6.3e-2:67:\\ \infty\\ \\ 1164(1255)\\ 30(35)\\ \\ \hline \\ 98(104)\\ 3\\ -3\\ -4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.0(3)\\ 1.8(1)\\ 0.73(0.8)\\ 1.0(2)\\ 1.3$ | $\begin{array}{r} 10\\ 10\\ 10\\ 5\\ 4.0e-2:307\\ \infty\\ 398(447)\\ 14(13)\\ \infty\\ 255(21)\\ 10\\ 2.5e+0:69\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 10\\ 6.3e+0:73\\ 1.2(1)\\ 7.7(7)\\ 1.3(1)\\ 1.6(0.5)\\ 1.0(0$ | $\begin{array}{r} 50\\ \hline & 2.5e{-}2.4946\\ & \infty 250\\ \hline & \infty 5c6\\ & \infty 5c5\\ & \infty 5c6\\ & \infty 5c5\\ & \infty 2805\\ & \infty 500\\ \hline & 1.6e{+}0.851\\ \hline & \infty 250\\ \hline & 2.3(3)\\ \hline & 15(11)\\ & \infty 500\\ \hline & 3.3(3)\\ \hline & 15(11)\\ & \infty 500\\ \hline & 3.5(3)\\ \hline & 50\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ \hline & 15(11)\\ \hline & 5.0\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ \hline & 1.5(11)\\ \hline & 5.0\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ \hline & 1.6e{+}0.347\\ \hline & 1.5(1.0)\\ \hline & 1.6e{+}0.341\\ \hline & 2.3(2)\\ \hline & 2.4(3)\\ \hline & 4.2(4)\\ \hline & 1.0(0.8)\\ \hline & 1.3(4)\\ \hline & 50\\ \hline & 1.0e{+}0.518\\ \hline & \infty 550\\ \hline & 1.3(24)\\ \hline & 50\\ \hline & 1.6e{+}1.692\\ \hline & 1.6e{+}1.6$ | #succ #succ 15/15 0/1 |
| #FEx/D f7 MATSuMo RANDOM NEWUGA imm-CMA SMAC IPOPsaACM #FEx/D MATSUMo NEWUGA imm-CMA SMAC IPOPsaACM #FEx/D Ø MATSUMO RANDOM NEWUGA imm-CMA SMAC IPOPsaACM #FEx/D MTSUMO RANDOM NEWUGA imm-CMA SMAC IPOPsaACM #FEx/D mm-CMA SMAC IPOPsaACM #FEx/D f11 MATSUMO NEWUOA imm-CMA SMAC IPOPsaACM #FEx/D f11 MATSUMO MEVEOA IPOPsaACM #FEx/D f12 | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(1) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5e+4:20 \\ 1.8(10) \\ 7845(7036) \\ 2.3(0.6)^* \\ 3.7(1) \\ 14(9) \\ 6.8(1) \\ 0.5 \\ 2.5e+6:2.9 \\ 1.5(1) \\ 1.4(2) \\ 1.5(1) \\ 1.4(3) \\ 0.5 \\ 1.0e+6:3.0 \\ 1.4(2) \\ 1.8(2) \\ 1.5(1) \\ 1.4(3) \\ 0.5 \\ 0.5 \\ 1.0e+6:3.0 \\ 1.4(3) \\ 0.5 \\ 0.5 \\ 1.0e+7:3.6 \\ 1.2(1) \\$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^{\times} \\ 3.3(1) \\ 12(3) \\ 5.7(2) \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 0.8(0.4) \\ 2.0(1) \\ 1.2 \\ 1.$ | $\begin{array}{r} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ \hline 8.8(6)\\ 2.2(3)\\ \hline 1.5(1.6)\\ 2.4(2)\\ 3\\ \hline 1.0e+3:18\\ \hline 1.4(0.3)\\ 10(8)\\ \hline 1.0(0.6)\\ \hline 1.6(0.6)\\ \hline 1.6(0.6)\\ \hline 1.2(0.8)\\ 2.1(2)\\ \hline 3\\ \hline 352(26)\\ \hline 4.1e4(3c4)\\ \hline 1.4e(43c4)\\ \hline 1.4e(43c4)\\ \hline 1.4e(43c4)\\ \hline 1.4e(43c4)\\ \hline 1.4e(43c4)\\ \hline 1.4e(43c4)\\ \hline 1.2(0.8)\\ 2.7(0.5)\\ \hline 1.2(0.8)\\ 2.1(2)\\ \hline 3\\ \hline 352(26)\\ \hline 1.2(0.8)\\ \hline 3\\ \hline 6.3e+2:16\\ \hline 4.7(2)\\ \hline 6.8(5)\\ \hline 1.5(0.4)\\ 2.6(1)\\ \hline 1.9(1)\\ \hline 6.7(8)\\ \hline 3\\ \hline 4.0e+6:19\\ \hline 1.7(0.7)\\ \hline 1.7(0.7)\\ \hline 1.5(1)\\ \hline 3\\ \hline 3\\ \hline 3.5(26)\\ \hline 1.7(1.6)\\ \hline 1.7(1.$ | 10 10 $4.0e+0.54$ $7.6(14)$ $151(135)$ $7.6(13)$ $2.3(3)$ $1.6(0.7)$ $2.2(0.5)$ 10 $6.3e+1:54$ $2.6(1)$ $482(412)$ $1(0.8)$ $1.5(0.4)$ $3.3(3)$ $2.0(1)$ 10 $4.0e+0.62$ $64(75)$ $1.2e6(2e6)$ $2.2(1)$ $2.7(0.9)$ $1.2e6(2e6)$ $2.2(1)$ $3.7(2)$ 10 $6.3e+3:54$ $6.4(4)$ $102(54)$ $1.8(0.8)$ $1.5(0.5)$ $2.5(2)$ $2.4(0.8)$ 10 $6.3e+1:74$ $8.9(12)$ $1.9(1)$ $0.94(1)$ $2.8(2)$ 10 $1.6e+4:52$ $3.2(2)$ 3 | $\begin{array}{r} 30\\ 50\\ \hline 1.0e+0.324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.98(0.4)\\ 1.2(0.2)\\ 50\\ \hline 1.6e+0.258\\ \infty \ 250\\ \infty \ 5e6\\ 1.1(2)\\ 1.7(2)\\ \infty \ 500\\ 1.1(2)\\ 1.7(2)\\ \infty \ 500\\ 1.8(2)\\ 50\\ \hline 0.5e-2:256\\ \infty \ 250\\ \infty \ 5e6\\ 2.2(1)\\ 2.4(2)\\ \infty \ 500\\ 2.3(0.8)\\ 50\\ \hline 0.83(0.3)\\ \infty \ 500\\ 0.85(0.2)\\ 50\\ \hline 0.85(0.2)\\ 50\\ \hline 0.85(0.2)\\ 50\\ \hline 0.85(0.2)\\ 50\\ \hline 1.2e5(2e5)\\ 3.5(0.8)\\ 1.3(0.3)\\ \infty \ 500\\ 1.3(0.3)\\ \infty \ 500\\ 1.3(0.3)\\ \infty \ 500\\ 1.2e5(2e5)\\ 3.5(0.8)\\ 1.3(0.3)\\ \infty \ 500\\ 1.1(0.2)\\ 50\\ \hline 1.0e+0.268\\ \infty \ 2.5e-0.268\\ \hline 0.82(1-200)\\ 50\\ \hline 1.0e+0.268\\ \infty \ 2.5e-0.268\\ \hline 0.82(1-200)\\ 1.2e+0.268\\ \hline 0.82(1-200)\\ 1.2e+0.268\\ \hline 0.82(1-200)\\ 1.2e+0.268\\ \hline 0.82(1-200)\\ 1.2e+0.268\\ \hline 0.82(1-200)\\ \hline 0.82(1-200)\\$ | 1[37]15 15/15 | HOFSAACM HFEs/D HFS/D MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HES/D RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HES/D RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HES/D RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HFES/D RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HES/D RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HES/D RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HES/D RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HES/D RANDOM NEWUOA | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-l:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.67(0.2) \\ 1.8(2) \\ 0.5$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.33(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.7(2) \\ 1.2(2) \\ 1.7(2) \\ 1.4(1) \\ 1.4(2) \\ 1.8(2) \\ 1.8(2) \\ 1.4(1) \\ 1.4(2) \\ 1.8(1) \\ 1.4(2) \\ 1.8(2) \\ 1.8(1) \\ 1.4(2) \\ 1.8(2) \\ 1.8(1) \\ 1.4(1) \\ 1.5(0.9) \\ 1.4(1) \\ 1.5(0.9) \\ 1.4(1) \\ 1.5(0.9) \\ 1.2(2) \\ 2.5(1) \\ 6.3e+0:9.0 \\ 1.7(2) \\ 2.5(1) \\ 6.4(13) \\ 2.6(5) \\ 2.9(2) \\ 2.9(2) \\ 1.2 \\ 4.0e+1:37 \\ 3.1(2) \\ 19(10) \end{array}$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \\ \hline \\ 6.3e-2:67:\\ \infty\\ \\ 0 \\ 30(35)\\ \\ 0 \\ 98(104)\\ 3\\ \hline \\ 0.73(0.8)\\ 1.8(2)\\ 1.3(2)\\ 1$ | $\begin{array}{r} 10\\ \hline 10\\ \hline$ | $\begin{array}{r} 50\\ \hline 50\\ \hline$ | issues is |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f10 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f10 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f11 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f12 M | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.2(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5e+1:20 \\ 18(10) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5e+1:20 \\ 18(10) \\ 0.99(0.7) \\ 2.4(2) \\ 1.3(0.8) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.5 \\ 1.0(1.0) \\ 2.3(2) \\ 1.5(1) \\ 1.4(3) \\ 0.5 \\ 1.0e+6:3.0 \\ 1.4(2) \\ 1.5(1) \\ 1.4(3) \\ 0.5 \\ 1.0e+6:3.0 \\ 1.4(3) \\ 0.5 \\ 1.0e+6:3.0 \\ 1.4(3) \\ 0.5 \\ 1.0e+7:3.6 \\ 1.2(1) \\ 2.2(3) \\ 1.2(3) $ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.6e+1:26 \\ 3.3(1) \\ 1.2(3) \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^{8} \\ 3.3(1) \\ 1.2(3) \\ 5.7(2) \\ 1.2 \\ 1.6e+5:7.0 \\ 1.9(1) \\ 1.5(2) \\ 1.4(0.6) \\ 1.5(1) \\ 0.80(0.4) \\ 2.0(1) \\ 1.2 \\ 6.3e+4:6.2 \\ 2.5(2) \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 4.0(6) \\ 3.9(0) \\ 2.7(4) \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 4.0(6) \\ 3.9(0) \\ 2.7(4) \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 4.0(6) \\ 3.9(0) \\ 1.2 \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 4.0(6) \\ 3.9(0) \\ 1.2 \\ $ | $\begin{array}{r} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(0.9)\\ 2.2(4)\\ 1.5(0.9)\\ 2.2(4)\\ 3\\ 1.0e+3.18\\ 1.4(0.3)\\ 10(8)\\ 10(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 1.2(0.5)\\ $ | $\begin{array}{r} 10 \\ \hline 10 \\ \hline 10 \\ \hline 2.1000 \\ \hline 3.1000 \\ \hline 3.100$ | $\begin{array}{r} 30 \\ \hline & 50 \\ \hline & 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.88(0.4) \\ 1.2(0.2) \\ \hline & 50 \\ \hline & 1.6e+0.258 \\ \infty 250 \\ \infty 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty 500 \\ 1.8(2) \\ \hline & 50 \\ 2.4(2) \\ \infty 500 \\ 2.4(2) \\ \infty 500 \\ 2.4(2) \\ \infty 500 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e+1:297 \\ \infty 250 \\ 0.85(0.2) \\ 50 \\ \hline & 0.85(0.2) \\ 50 \\ 0.85(0.2) \\ 50 \\ 1.2e(2e5) \\ 3.5(0.8) \\ 1.3(0.3) \\ \infty 500 \\ 1.10e+0.268 \\ \infty 250 \\ 1.0e+0.268 \\ \infty 250 \\ 0.85(0.2) \\$ | 11/11 15/15 </td <td>HOPSAACM HFEs/D HFEs/D HOPSAACM HFES/D HOPSAACM HOPSAACM HOPSAACM HOPSAACM</td> <td>$\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-I:172 \\ \infty \\ 4.2cs(4c5) \\ 1308(2380) \\ \overline{55}(56) \\ \infty \\ 280(359) \\ 0.5 \\ c.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 2.0(2) \\ 0.5 \\ c.3e+I:3.6 \\ 1.6(2) \\ 2.0(2) \\ 0.5 \\ c.3e+I:3.6 \\ 1.6(2) \\ 1.8(2) \\ 2.0(2) \\ 0.5 \\ c.3e+I:1.5 \\ 1.9(2) \\ 1.3(0.5) \\ 1.3(0.5) \\ 0.5 \\ 0.5 \\ c.3e+I:15 \\ 1.9(2) \\ 3.6(3) \\ 1.3(0.5) \\ 0.5 \\ 0$</td> <td>$\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.38(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1$</td> <td>$\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \\ \hline \\ 6.3e-2:67:\\ \infty\\ \\ 98(104)\\ 3\\ -3\\ -4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.0(3)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ -1.6e+1:31\\ 0.73(0.8)\\ 1.3(2)\\ 1.3$</td> <td>$\begin{array}{r} 10\\ \hline 10\\ \hline$</td> <td>$\begin{array}{r} 50\\ \hline 50\\ \hline \$2.5e-2:4946\\ \simeq 250\\ \simeq 5e6\\ \simeq 5e6\\ \simeq 5e5\\ \simeq 2805\\ \simeq 500\\ 16(13)\\ \hline \$0\\ 2234(8531)\\ 3.3(3)\\ 15(11)\\ \simeq 500\\ 1.6e+0:341\\ 2.3(2)\\ 3.4(5)\\ 2.4(5)\\ 4.8(6)\\ \hline \$1.6e+0:341\\ 2.3(2)\\ 4.3(15)\\ 2.4(5)\\ 4.2(4)\\ 1.0(0.6)\\ 4.8(6)\\ \hline \$1.6e+0:341\\ 2.3(2)\\ 4.3(15)\\ 2.4(5)\\ 4.2(4)\\ 1.0(0.8)\\ 13(24)\\ \hline \$0\\ 1.6e+1:692\\ 5.3(6)\\ 4.18(582)\\ 2.3(2)\\ \hline \$1.6e+1:692\\ 5.3(6)\\ 4.18(582)\\ 2.3(2)\\ \hline \$1.6e+1:692\\ 5.3(6)\\ \hline \$1.6e+1:692\\ 5.3(6)\\ \hline \$1.6e+1:692\\ 5.3(6)\\ \hline \$3.2(2)\\ \hline \$3.$</td> <td>#succe #succe #succe #succe 0/15</td> | HOPSAACM HFEs/D HFEs/D HOPSAACM HFES/D HOPSAACM HOPSAACM HOPSAACM HOPSAACM | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-I:172 \\ \infty \\ 4.2cs(4c5) \\ 1308(2380) \\ \overline{55}(56) \\ \infty \\ 280(359) \\ 0.5 \\ c.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 2.0(2) \\ 0.5 \\ c.3e+I:3.6 \\ 1.6(2) \\ 2.0(2) \\ 0.5 \\ c.3e+I:3.6 \\ 1.6(2) \\ 1.8(2) \\ 2.0(2) \\ 0.5 \\ c.3e+I:1.5 \\ 1.9(2) \\ 1.3(0.5) \\ 1.3(0.5) \\ 0.5 \\ 0.5 \\ c.3e+I:15 \\ 1.9(2) \\ 3.6(3) \\ 1.3(0.5) \\ 0.5 \\ 0$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.38(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \\ \hline \\ 6.3e-2:67:\\ \infty\\ \\ 98(104)\\ 3\\ -3\\ -4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.0(3)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ -1.6e+1:31\\ 0.73(0.8)\\ 1.3(2)\\ 1.3$ | $\begin{array}{r} 10\\ \hline 10\\ \hline$ | $\begin{array}{r} 50\\ \hline 50\\ \hline $2.5e-2:4946\\ \simeq 250\\ \simeq 5e6\\ \simeq 5e6\\ \simeq 5e5\\ \simeq 2805\\ \simeq 500\\ 16(13)\\ \hline $0\\ 2234(8531)\\ 3.3(3)\\ 15(11)\\ \simeq 500\\ 1.6e+0:341\\ 2.3(2)\\ 3.4(5)\\ 2.4(5)\\ 4.8(6)\\ \hline $1.6e+0:341\\ 2.3(2)\\ 4.3(15)\\ 2.4(5)\\ 4.2(4)\\ 1.0(0.6)\\ 4.8(6)\\ \hline $1.6e+0:341\\ 2.3(2)\\ 4.3(15)\\ 2.4(5)\\ 4.2(4)\\ 1.0(0.8)\\ 13(24)\\ \hline $0\\ 1.6e+1:692\\ 5.3(6)\\ 4.18(582)\\ 2.3(2)\\ \hline $1.6e+1:692\\ 5.3(6)\\ 4.18(582)\\ 2.3(2)\\ \hline $1.6e+1:692\\ 5.3(6)\\ \hline $1.6e+1:692\\ 5.3(6)\\ \hline $1.6e+1:692\\ 5.3(6)\\ \hline $3.2(2)\\ \hline $3.$ | #succe #succe #succe #succe 0/15 |
| #FEx/D r MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEx/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEx/D Ø Ø MATSUMO RANDOM NEWUOA Inm-CMA SMAC IPOPsaACM #FEx/D ft0 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEx/D ft1 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEx/D ft1 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEx/D <td>$\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 1.0(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 1.0e+4:3.0 \\ 1.0(1.0)$</td> <td>$\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.2(2) \\ 2.9(2) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^{*} \\ 3.3(1) \\ 1.2(3) \\ 5.7(2) \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 1.6e+7:7.0 \\ 1.5(1) \\ 0.80(0.4) \\ 2.0(1) \\ 1.5(2) \\ 1.40(6) \\ 1.5(1) \\ 0.80(0.4) \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 4.0(6) \\ 2.8(0.9) \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 4.0(6) \\ 2.8(0.9) \\ 1.6(2) \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 1.6(2) \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 1.6(2) \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 1.6(2$</td> <td>$\begin{array}{r} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(0.9)\\ 2.2(3)\\ 1.5(1)\\ 1.5(0.9)\\ 2.2(42)\\ 3\\ 1.0e+3.18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 2.7(0.5)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ 35(26)\\ 4.1e4(3e4)\\ 1.48(4.7)^{\star}\\ 1.2(0.8)\\ 2.5e+5:17\\ 1.4(1.0)\\ 1.6(2)\\ 1.0(0.6)\\ 1.1(0.6)\\ 1.5(1)\\ 3\\ 6.3e+2:16\\ 4.7(2)\\ 6.8(5)\\ 1.5(0.4)\\ 2.6(1)\\ 1.9(1)\\ 6.7(8)\\ 3\\ 4.0e+6:19\\ 1.7(0.7)\\ 16(29)\\ 1.5(0.3)\\ 1.6(0.7)\\ 1.5(0.3)\\ 1.6(0.7)\\ 1.5(1)\\ 3\\ 1.5(0.4)\\ 2.6(1)\\ 1.9(1)\\ 6.7(8)\\ 3\\ 1.5(0.3)\\ 1.5(0.3)\\ 1.5(0.3)\\ 1.5(0.3)\\ 1.5(0.3)\\ 1.5(0.4)\\ 2.6(1)\\ 1.5(1)\\ 3\\ 1.5(0.4)\\ 2.6(1)\\ 1.5(1)\\ 3\\ 1.5(0.4)\\ 2.6(1)\\ 1.5(1)\\ 1.5(1)\\ 3\\ 1.5(0.4)\\ 2.6(1)\\ 1.5(1)\\$</td> <td>$\begin{array}{r} 10 \\ 10 \\ \hline 151(135) \\ \hline 7.6(13) \\ 2.3(3) \\ \hline 10 \\ \hline 10 \\ \hline 0.3e+1:54 \\ 2.6(0.7) \\ 2.2(0.5) \\ \hline 10 \\ \hline 0.3e+1:54 \\ 2.6(1) \\ \hline 10 \\ \hline 0.3e+1:54 \\ 2.6(1) \\ \hline 10 \\ \hline 0.3e+0:62 \\ 64(75) \\ 1.2e6(2e6) \\ 2.2(1) \\ 1.2e6(2e6) \\ 1.2e6(2e6) \\ 2.2(1) \\ 1.2e6(2e6) \\ 1.2e6(2e6$</td> <td>$\begin{array}{r} 30 \\ \hline 50 \\ \hline 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.98(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline 1.6e+0.258 \\ \infty 250 \\ \infty 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e-2:256 \\ \infty 250 \\ 0.566 \\ 2.2(1) \\ 2.4(2) \\ \infty 500 \\ 2.3e+1:297 \\ \infty 250 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e+1:298 \\ \infty 250 \\ 1.2e(2e) \\ 3.5(0.8) \\ 1.0(3) \\ \infty 500 \\ 1.2e(2e) \\ 3.5(0.8) \\ 1.0(3) \\ \infty 500 \\ 1.2e(2e) \\ 3.5(0.8) \\ 1.2e(2e) \\ 1.2e(2e) \\ 3.5(0.8) \\ 1.2e(2e) \\$</td> <td>1[37]15 159175 2/15 159175</td> <td>HOFSAACM HFEs/D HIPOPSAACM WATSUMO RANDOM NEWUOA Imm-CMA SMAC HOPSSACM HES/D MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HFEs/D T21 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HFES/D T22 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HES/D T23 MATSUMO RANDOM NEWUOA Imm-CMA SMAC</td> <td>$\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-i:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 50, 0.5 \\ \hline 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0,7) \\ 1.2(0,1) \\ 0.57(0,2) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1$</td> <td>$\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0,1) \\ 0.33(0,4) \\ 0.44(0,2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0,3) \\ 1.4(0,6) \\ 1.4(2) \\ 1.8(2) \\ 1.3(1) \\ 1.4(2) \\ 1.8(2) \\ 1.8(2) \\ 1.4(1) \\ 1.4(2) \\ 1.8(2) \\ 1.4(2) \\ 1.8(2) \\ 1.4(1) \\ 1.5(0,9) \\ 1.7(2) \\ 2.5(1) \\ 6.3e+0:9.0 \\ 1.7(2) \\ 2.5(1) \\ 6.4(13) \\ 2.6(5) \\ 2.9(2) \\ 1.2 \\ 4.0e+1:37 \\ 3.1(2) \\ 19(10) \\ 2.7(7) \\ 2.0(1) \end{array}$</td> <td>$\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ -3\\ -4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ -1.6e+1:15\\ 0.73(0.8)\\ 1.3(2)\\ 1.3$</td> <td>$\begin{array}{r} 10\\ 10\\ 10\\ 5\\ 4.0e-2:307\\ \infty\\ 398(447)\\ 14(13)\\ \infty\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 1.0\\ 1.0(6)\\ 5.1(3)\\ 1.2(1)\\ 7.7(7)\\ 1.3(1)\\ 1.6(0.5)\\ 1.0(0.9)\\ 3.8(4)\\ 10\\ 1.0e+1:71\\ 1.3(1)\\ 1.6(0.5)\\ 1.0(0.9)\\ 3.8(4)\\ 10\\ 1.0e+1:71\\ 1.3(1)\\ 2.5(10)\\ 0.90(0.7)\\ 3.3(3)\\ 5.1(8)\\ 10\\ 2.5e+0:84\\ 3.9(3)\\ 5.1(8)\\ 10\\ 2.5e+1:118\\ 10(8)\\ 119(35)\\ 2.4(2)\\ 1.7(1)\\ 10\\ 10\\ 10\\ 10\\ 10\\ 10\\ 10\\ 10\\ 10\\ 10$</td> <td>$\begin{array}{r} 50\\ \hline 50\\ \hline 2.5e{-}2.4946\\ \hline \infty 250\\ \hline \infty 5e6\\ \hline \infty 5e5\\ \hline \infty 5e5\\ \hline \infty 2805\\ \hline \infty 500\\ \hline 16(13)\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline \infty 250\\ \hline 9234(8531)\\ \hline 3.3(3)\\ \hline 15(11)\\ \hline \infty 500\\ \hline 3.5(3)\\ \hline 50\\ \hline 1.6e{+}0.347\\ \hline 1.5(11)\\ \hline 5.0\\ \hline 1.6e{+}0.51\\ \hline 0.0\\ \hline$</td> <td>#succe #succe fs/15/15 0/15 0/15 0/15 0/15 15/15</td> | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 1.0(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 1.0e+4:3.0 \\ 1.0(1.0)$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.2(2) \\ 2.9(2) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.6e+1:26 \\ 3.4(51) \\ 2.3e4(4e4) \\ 2.1(0.9)^{*} \\ 3.3(1) \\ 1.2(3) \\ 5.7(2) \\ 1.2 \\ 6.3e+5:7.0 \\ 1.2 \\ 1.6e+7:7.0 \\ 1.5(1) \\ 0.80(0.4) \\ 2.0(1) \\ 1.5(2) \\ 1.40(6) \\ 1.5(1) \\ 0.80(0.4) \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 2.5(1) \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 4.0(6) \\ 2.8(0.9) \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 4.0(6) \\ 2.8(0.9) \\ 1.6(2) \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 1.6(2) \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 1.6(2) \\ 1.2 \\ 1.6e+7:7.6 \\ 1.4(1) \\ 1.6(2$ | $\begin{array}{r} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(0.9)\\ 2.2(3)\\ 1.5(1)\\ 1.5(0.9)\\ 2.2(42)\\ 3\\ 1.0e+3.18\\ 1.4(0.3)\\ 10(8)\\ 1.0(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 2.7(0.5)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ 35(26)\\ 4.1e4(3e4)\\ 1.48(4.7)^{\star}\\ 1.2(0.8)\\ 2.5e+5:17\\ 1.4(1.0)\\ 1.6(2)\\ 1.0(0.6)\\ 1.1(0.6)\\ 1.5(1)\\ 3\\ 6.3e+2:16\\ 4.7(2)\\ 6.8(5)\\ 1.5(0.4)\\ 2.6(1)\\ 1.9(1)\\ 6.7(8)\\ 3\\ 4.0e+6:19\\ 1.7(0.7)\\ 16(29)\\ 1.5(0.3)\\ 1.6(0.7)\\ 1.5(0.3)\\ 1.6(0.7)\\ 1.5(1)\\ 3\\ 1.5(0.4)\\ 2.6(1)\\ 1.9(1)\\ 6.7(8)\\ 3\\ 1.5(0.3)\\ 1.5(0.3)\\ 1.5(0.3)\\ 1.5(0.3)\\ 1.5(0.3)\\ 1.5(0.4)\\ 2.6(1)\\ 1.5(1)\\ 3\\ 1.5(0.4)\\ 2.6(1)\\ 1.5(1)\\ 3\\ 1.5(0.4)\\ 2.6(1)\\ 1.5(1)\\ 1.5(1)\\ 3\\ 1.5(0.4)\\ 2.6(1)\\ 1.5(1)\\ $ | $\begin{array}{r} 10 \\ 10 \\ \hline 151(135) \\ \hline 7.6(13) \\ 2.3(3) \\ \hline 10 \\ \hline 10 \\ \hline 0.3e+1:54 \\ 2.6(0.7) \\ 2.2(0.5) \\ \hline 10 \\ \hline 0.3e+1:54 \\ 2.6(1) \\ \hline 10 \\ \hline 0.3e+1:54 \\ 2.6(1) \\ \hline 10 \\ \hline 0.3e+0:62 \\ 64(75) \\ 1.2e6(2e6) \\ 2.2(1) \\ 1.2e6(2e6) \\ 1.2e6(2e6) \\ 2.2(1) \\ 1.2e6(2e6) \\ 1.2e6(2e6$ | $\begin{array}{r} 30 \\ \hline 50 \\ \hline 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.98(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline 1.6e+0.258 \\ \infty 250 \\ \infty 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e-2:256 \\ \infty 250 \\ 0.566 \\ 2.2(1) \\ 2.4(2) \\ \infty 500 \\ 2.3e+1:297 \\ \infty 250 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e+1:297 \\ \infty 250 \\ 2.5e+1:298 \\ \infty 250 \\ 1.2e(2e) \\ 3.5(0.8) \\ 1.0(3) \\ \infty 500 \\ 1.2e(2e) \\ 3.5(0.8) \\ 1.0(3) \\ \infty 500 \\ 1.2e(2e) \\ 3.5(0.8) \\ 1.2e(2e) \\ 1.2e(2e) \\ 3.5(0.8) \\ 1.2e(2e) \\ $ | 1[37]15 159175 2/15 159175 | HOFSAACM HFEs/D HIPOPSAACM WATSUMO RANDOM NEWUOA Imm-CMA SMAC HOPSSACM HES/D MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HFEs/D T21 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HFES/D T22 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPSAACM HES/D T23 MATSUMO RANDOM NEWUOA Imm-CMA SMAC | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-i:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 50, 0.5 \\ \hline 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0,7) \\ 1.2(0,1) \\ 0.57(0,2) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1) \\ 1.2(0,1) \\ 0.057(0,2) \\ 1.2(0,1$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0,1) \\ 0.33(0,4) \\ 0.44(0,2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0,3) \\ 1.4(0,6) \\ 1.4(2) \\ 1.8(2) \\ 1.3(1) \\ 1.4(2) \\ 1.8(2) \\ 1.8(2) \\ 1.4(1) \\ 1.4(2) \\ 1.8(2) \\ 1.4(2) \\ 1.8(2) \\ 1.4(1) \\ 1.5(0,9) \\ 1.7(2) \\ 2.5(1) \\ 6.3e+0:9.0 \\ 1.7(2) \\ 2.5(1) \\ 6.4(13) \\ 2.6(5) \\ 2.9(2) \\ 1.2 \\ 4.0e+1:37 \\ 3.1(2) \\ 19(10) \\ 2.7(7) \\ 2.0(1) \end{array}$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ -3\\ -4.0e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.8(1)\\ 0.73(0.3)\\ 2.3(2)\\ 3\\ -1.6e+1:15\\ 0.73(0.8)\\ 1.3(2)\\ 1.3$ | $\begin{array}{r} 10\\ 10\\ 10\\ 5\\ 4.0e-2:307\\ \infty\\ 398(447)\\ 14(13)\\ \infty\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 1.0\\ 1.0(6)\\ 5.1(3)\\ 1.2(1)\\ 7.7(7)\\ 1.3(1)\\ 1.6(0.5)\\ 1.0(0.9)\\ 3.8(4)\\ 10\\ 1.0e+1:71\\ 1.3(1)\\ 1.6(0.5)\\ 1.0(0.9)\\ 3.8(4)\\ 10\\ 1.0e+1:71\\ 1.3(1)\\ 2.5(10)\\ 0.90(0.7)\\ 3.3(3)\\ 5.1(8)\\ 10\\ 2.5e+0:84\\ 3.9(3)\\ 5.1(8)\\ 10\\ 2.5e+1:118\\ 10(8)\\ 119(35)\\ 2.4(2)\\ 1.7(1)\\ 10\\ 10\\ 10\\ 10\\ 10\\ 10\\ 10\\ 10\\ 10\\ 10$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 2.5e{-}2.4946\\ \hline \infty 250\\ \hline \infty 5e6\\ \hline \infty 5e5\\ \hline \infty 5e5\\ \hline \infty 2805\\ \hline \infty 500\\ \hline 16(13)\\ \hline 50\\ \hline 1.0e{+}0.851\\ \hline \infty 250\\ \hline 9234(8531)\\ \hline 3.3(3)\\ \hline 15(11)\\ \hline \infty 500\\ \hline 3.5(3)\\ \hline 50\\ \hline 1.6e{+}0.347\\ \hline 1.5(11)\\ \hline 5.0\\ \hline 1.6e{+}0.51\\ \hline 0.0\\ \hline $ | #succe #succe fs/15/15 0/15 0/15 0/15 0/15 15/15 |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D B MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D Ø MATSUMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D MTSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f11 MATSUMO NEWUOA Imm-CMA SMAC IPOPsaACM #EFE/D MATSUMO NEWUOA Imm-CMA SMAC IPOPsaACM #EFE/D MATSUMO NEWUOA I | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.6e+$ | $\begin{array}{c} 1.2 \\ 1.0e+2:6.2 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 3.1(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.8(0.1) \\ 0.91(1) \\ 2.2(3) \\ 1.2 \\ 1.8(0.1) \\ 0.91(1) \\ 2.2(3) \\ 1.2$ | $\begin{array}{c} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(1.6)\\ 1.5(1.6)\\ 2.4(2)\\ 3\\ \hline 1.0e+3:18\\ 1.4(0.3)\\ 10(8)\\ 1.9(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 2.7(0.5)\\ 12(3)\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)^{\star}\\ 2.7(0.5)\\ 12(3)\\ 3\\ \hline 3.5e+5:17\\ 1.4(1.0)\\ 1.6(2)\\ 1.0(0.6)\\ 1.1(0.6)\\ 0.58(0.7)\\ 1.5(1)\\ 3\\ \hline 6.3e+2:16\\ 4.7(2)\\ 6.8(5)\\ 1.5(0.4)\\ 2.6(1)\\ 1.9(1)\\ 6.7(8)\\ 3\\ \hline 4.0e+6:19\\ 1.7(0.7)\\ 1.5(0.3)\\ 1.6(0.7)\\ 1.5(0.3)\\ $ | $\begin{array}{r} 10 \\ 10 \\ \hline 10 \\ \hline 2.6(14) \\ 151(135) \\ 7.6(13) \\ 2.3(3) \\ 1.6(0.7) \\ 2.2(0.5) \\ 10 \\ \hline 6.3e+1:54 \\ 2.6(1) \\ 10(.8) \\ 1.5(0.4) \\ 1.6(.8) \\ 1.5(0.4) \\ 10(.8) \\ 1.5(0.4) \\ 1.2e6(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2e6(2e6) \\ 2.2(1) \\ 3.3(2) \\ 1.2e(2e6) \\ 1.2e(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2e(2e6) \\ 1.2e(2e6) \\ 2.2(1) \\ 2.7(0.9) \\ 1.2e(2e6) $ | $\begin{array}{r} 30 \\ \hline 50 \\ \hline 1.0e+0.324 \\ 5.4(4) \\ 1207(1290) \\ 13(15) \\ 0.92(2) \\ 0.98(0.4) \\ 1.2(0.2) \\ \hline 50 \\ \hline 1.6e+0.258 \\ \infty 250 \\ \infty 5e6 \\ 1.1(2) \\ 1.7(2) \\ \infty 500 \\ 1.8(2) \\ \hline 50 \\ \hline 1.6e-2.256 \\ \infty 250 \\ \infty 5e6 \\ 2.2(1) \\ 2.4(2) \\ \cos 500 \\ 2.36e+1.297 \\ \infty 250 \\ 2.5e+4.297 \\ \infty 250 \\ 2.5e5(4e5) \\ 2.6(4) \\ 0.83(0.3) \\ \infty 500 \\ 0.85(0.2) \\ \hline 50 \\ \hline 6.3e-1.298 \\ \infty 250 \\ 1.2e5(2e5) \\ 3.5(0.8) \\ 1.3(0.3) \\ \infty 500 \\ 1.3(0.3) \\ \infty 500 \\ 1.2e5(2e5) \\ 3.5(0.8) \\ 1.3(0.3) \\ \infty 500 \\ 1.1(0.2) \\ \hline 50 \\ 1.0e+0.268 \\ \infty 250 \\ 0.85(0.2) \\ \hline 50 \\ 1.1(0.2) \\ 50 \\ 1.0e+0.268 \\ \infty 250 \\ 0.560 \\ 1.4(0.6) \\ \infty 500 \\ 1.4(0.6) \\ \infty 500 \\ \hline \end{array}$ | 1[37]15 15/15 | HOFSAACM HEEAD HEEAD MATSUMO RANDOM NEWUOA Imm-CMA SMAC HOPSSAACM HEEAD RANDOM NEWUOA Imm-CMA SMAC HOPSSACM HEEAD RANDOM NEWUOA Imm-CMA SMAC HOPSSACM HEEAD RANDOM NEWUOA Imm-CMA SMAC HOPSSACM HEEAD RANDOM NEWUOA Imm-CMA SMAC HOPSSACM HEEAD RANDOM NEWUOA Imm-CMA SMAC HOPSSACM HEEAD RANDOM NEWUOA Imm-CMA SMAC HOPSSACM HEEAD RANDOM NEWUOA Imm-CMA SMAC | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 1.6e-I:172 \\ \infty \\ 4.2e5(4e5) \\ 1308(2380) \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(3) $ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.33(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 1.5(0.1) \\ 0.34(0.4) \\ 1.5(0.1) \\ 1.4(2) \\ 1.8(2) \\ 1.8(1) \\ 1.4(2) \\ 1.8(2) \\ 1.8(1) \\ 1.4(2) \\ 1.8(2) \\ 1.8(1) \\ 1.4(2) \\ 1.8(2) \\ 1.8(1) \\ 1.4(1) \\ 1.4(1) \\ 1.4(1) \\ 1.5(0.9) \\ 1.2 \\ 4.0e+1:15 \\ 1.1(0.9) \\ 1.2 \\ 0.3(4) \\ 2.1(4) \\ 1.4(1) \\ 1.5(0.9) \\ 1.2 $ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ 1164(1255)\\ 30(35)\\ \infty\\ 98(104)\\ 3\\ -8(104)\\ 3\\ -8(104)\\ 3\\ -8(104)\\ -3\\ -8(104)\\ -3\\ -8(104)\\ -3\\ -3\\ -3\\ -3\\ -3\\ -3\\ -3\\ -3\\ -3\\ -3$ | $\begin{array}{r} 10\\ 10\\ 10\\ 5\\ 4.0e-2:307\\ \infty\\ 398(447)\\ 14(13)\\ \infty\\ 255(21)\\ 10\\ 2.5e+0:69\\ 4.1(3)\\ 251(328)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 1.1(1)\\ 4.0(6)\\ 4.3(2)\\ 3.2(2)\\ 1.1(1)\\ 4.0(6)\\ 1.0e+1:71\\ 1.3(1)\\ 1.6(0.5)\\ 1.0(0.5$ | $\begin{array}{r} 50\\ \hline 50\\ \hline 2.5e-2.4946\\ \propto 2.50\\ \hline 50\\ \hline 50\\ \hline 50\\ \hline 50\\ \hline 1.6e+0.851\\ \hline 50\\ \hline 1.6e+0.851\\ \hline 50\\ \hline 1.6e+0.851\\ \hline 50\\ \hline 1.6e+0.347\\ \hline 1.5(11)\\ \hline 5.4(6)\\ \hline 50\\ \hline 1.6e+0.347\\ \hline 1.5(1.0)\\ \hline 15(11)\\ \hline 5.4(6)\\ \hline 2.7(4)\\ \hline 1.0(0.6)\\ \hline 4.8(6)\\ \hline 2.7(4)\\ \hline 1.0(0.6)\\ \hline 4.2(4)\\ \hline 1.0(0.6)\\ \hline 4.2(4)\\ \hline 1.0(0.8)\\ \hline 1.3(2)\\ \hline 50\\ \hline 1.6e+0.518\\ \hline 50\\ \hline 1.6e+0.518\\ \hline 50\\ \hline 1.6e+1.692\\ \hline 5.3(6)\\ \hline 4.18(52)\\ \hline 2.3(2)\\ \hline 50\\ \hline 1.6e+1.692\\ \hline 5.3(6)\\ \hline 4.18(52)\\ \hline 2.3(2)\\ \hline 50\\ \hline 1.6e+1.692\\ \hline 5.3(6)\\ \hline 1.6e+1.692\\ \hline 5.3(6)\\ \hline 4.8(52)\\ \hline 2.3(2)\\ \hline 0.9(11)\\ \hline 50\\ \hline 0.500\\ \hline 0.50$ | #succ #succ #succ 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 |
| #FEs/D f7 MATSuMo RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D Ø MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f10 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f10 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f11 MATSUMO RANDOM NEWUOA Imm-CMA SMAC IPOPsaACM #FEs/D f12 | $\begin{array}{c} 0.5 \\ 1.6e+2:4.2 \\ 1.3(1) \\ 2.0(2) \\ 2.6(2) \\ 1.3(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.2(2) \\ 0.5 \\ 1.0e+4:4.6 \\ 1.7(2) \\ 3.0(3) \\ 2.5(0.6) \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 2.5e+1:20 \\ 18(10) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 1.0(1.0) \\ 0.99(0.7) \\ 2.4(2) \\ 0.5 \\ 1.0(1.0) \\ 0.5 $ | $\begin{array}{c} 12 \\ 1.0e+2:6.2 \\ 1.8(1) \\ 2.9(0.8) \\ 2.2(0.2) \\ 1.3(0.8) \\ 1.1(0.8) \\ 2.9(2) \\ 1.2 \\ 6.3e+3:6.8 \\ 1.9(1) \\ 2.2(3) \\ 1.8(0.1) \\ 0.96(1.0) \\ 0.9$ | $\begin{array}{r} 3\\ \hline 3\\ \hline 2.5e+1.20\\ 1.5(0.6)\\ 8.8(6)\\ 2.2(3)\\ 1.5(0.9)\\ 2.2(42)\\ 3\\ \hline 1.6(0.9)\\ 2.2(42)\\ 3\\ \hline 1.0e+3.18\\ 1.4(0.3)\\ 10(8)\\ 10(0.6)\\ 1.6(0.6)\\ 1.6(0.6)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1.35\\ 35(26)\\ 4.1e4(3e4)\\ 1.8(0.7)*\\ 1.2(0.5)\\ 1.2(0.8)\\ 2.1(2)\\ 3\\ \hline 1.0e+1.35\\ 35(26)\\ 3.5(26)\\ 3.5(26)\\ 3.5(26)\\ 1.5(1)\\ 3\\ \hline 2.5e+5.17\\ 1.4(1.0)\\ 1.6(2)\\ 1.0(0.5)\\ 1.2(0.5)\\ 1.2(0.5)\\ 1.2(0.5)\\ 1.2(0.5)\\ 3\\ \hline 3\\ \hline 3\\ 2.5e+5.17\\ 1.4(1.0)\\ 1.6(2)\\ 1.0(0.5)\\ 1.5(1)\\ 3\\ \hline 6.3e+2.16\\ 4.7(2)\\ 6.8(5)\\ 1.5(0.4)\\ 2.6(1)\\ 1.9(1)\\ 6.7(8)\\ 3\\ \hline 4.0e+6.19\\ 1.7(0.7)\\ 1.6(29)\\ 1.5(0.3)\\ 1.6(0.7)\\ 3.6(8)\\ 2.6(1)\\ \end{array}$ | $\begin{array}{r} 10 \\ \hline 151(135) \\ \hline 7.6(13) \\ \hline 2.3(3) \\ \hline 16(0.7) \\ 2.2(0.5) \\ \hline 10 \\ \hline 6.3e+1:54 \\ 2.6(1) \\ \hline 482(412) \\ \hline 10 \\ \hline 4.0e+0:62 \\ \hline 6.4(75) \\ \hline 1.2e6(2e6) \\ \hline 2.2(1) \\ \hline 1.2e6(2e6) \\ 1$ | $\begin{array}{r} 30\\ 50\\ \hline 1.0e+0.324\\ 5.4(4)\\ 1207(1290)\\ 13(15)\\ 0.92(2)\\ 0.988(0.4)\\ 1.2(0.2)\\ 50\\ \hline 1.6e+0.258\\ \infty 250\\ \infty 5e6\\ 1.1(2)\\ 1.7(2)\\ \infty 500\\ 1.18(2)\\ 50\\ \hline 1.6e+0.258\\ \infty 250\\ \infty 5e6\\ 2.2(1)\\ 2.4(2)\\ \infty 500\\ 2.3(0.8)\\ 50\\ \hline 2.5e+1:297\\ \infty 250\\ 2.5e(4)\\ 50\\ \hline 2.5e(4)\\ 50\\ 0.85(0.2)\\ 50\\ \hline 6.3e+1:298\\ \infty 250\\ 2.5e(4)\\ 3.5(0.2)\\ 50\\ \hline 1.2e(2c5)\\ 3.5(0.8)\\ 1.3(0.3)\\ \infty 500\\ 1.2e(2c5)\\ 3.5(0.8)\\ 1.3(0.3)\\ \infty 550\\ 1.1(0.2)\\ 50\\ \hline 1.0e+0.268\\ \infty 250\\ \infty 5e6\\ 2.6(3)\\ 1.4(0.6)\\ \infty 500\\ 2.9(4)\\ \end{array}$ | 1[37]15 15/15 | HOPSACA, HFEs/D HFEs/D HFEs/D HOPSaACA HOPSaACA HOPSaACA HOPSaACA HOPSaACA HOPSaACA HOPSaACA HOPSaACA HOPSAACA HOPSAACA HOPSAACA HES/D HOPSAACA HOP | $\begin{array}{c} 0.5 \\ \hline 0.5 \\ \hline 0.6e-l:172 \\ \infty \\ 4 2cs(4c5) \\ 1308(2380) \\ \overline{55}(56) \\ \infty \\ 55(56) \\ \infty \\ 280(359) \\ 0.5 \\ 6.3e+3:5.1 \\ 1.7(2) \\ 1.6(2) \\ 2.3(0.7) \\ 1.2(0.1) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.57(0.2) \\ 1.8(2) \\ 0.5 \\ 6.3e+l:3.6 \\ 1.6(2) \\ 1.8(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.8(2) \\ 1.4(3) \\ 2.7(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.6(2) \\ 1.8(2) \\ 1.8(2) \\ 1.6(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.6(2) \\ 1.8(2) \\$ | $\begin{array}{c} 1.2 \\ 1.0e-1:242 \\ \hline 0.0e-1:242 \\ \infty \\ 1415(1586) \\ 56(58) \\ \infty \\ 250(295) \\ 1.2 \\ 4.0e+3:8.4 \\ 1.4(1) \\ 3.5(6) \\ 1.5(0.1) \\ 0.38(0.4) \\ 0.44(0.2) \\ 1.7(2) \\ 1.2 \\ 2.5e+1:11 \\ 1.3(1) \\ 1(0.3) \\ 1.4(0.6) \\ 1.4(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(2) \\ 1.8(1) \\ 1.4(1) \\ 1.5(0.9) \\ 3.0(4) \\ 2.1(4) \\ 1.4(1) \\ 1.5(0.9) \\ 1.9(2) \\ 2.5(1) \\ 6.3e+0:9.0 \\ 1.7(2) \\ 2.5(1) \\ 6.3e+0:9.0 \\ 1.7(2) \\ 2.5(1) \\ 6.4(13) \\ 2.6(5) \\ 2.9(2) \\ 2.9(2) \\ 2.9(2) \\ 2.9(2) \\ 1.2 \\ 4.0e+1:37 \\ 3.1(2) \\ 1.9(10) \\ 2.7(7) \\ 2.0(1) \\ 2.6(2) \\ 2.2(0.6) \end{array}$ | $\begin{array}{c} 3\\ 6.3e-2:67:\\ \infty\\ \\ \hline \\ 6.3e-2:67:\\ \infty\\ \\ 0 \\ 30(35)\\ \\ 0 \\ 98(104)\\ 3\\ 3\\ 0.6e+1:15\\ 1.9(0.7)\\ 24(10)\\ 1.0(0.7)\\ 24(10)\\ 1.0(0.7)\\ 1.8(1)\\ 0.73(0.8)\\ 1.3(2)\\ 1$ | $\begin{array}{r} 10\\ \hline 10\\ \hline$ | $\begin{array}{r} 50\\ \hline 50\\ \hline $2.5e-2:4946\\ \simeq 250\\ \simeq 5.66\\ \simeq 5.65\\ \simeq 2805\\ \simeq 5.00\\ 16(13)\\ \hline 50\\ \hline 1.0e+0:851\\ \simeq 250\\ 9234(8531)\\ \hline 50\\ \hline 1.0e+0:851\\ \simeq 250\\ 9234(8531)\\ \hline 50\\ \hline 1.0e+0:851\\ \simeq 50\\ \hline 1.6e+0:341\\ \hline 2.3(2)\\ 4.3(3)\\ \hline 15(11)\\ 5.4(6)\\ 2.7(4)\\ \hline 1.6(e+0:341\\ \hline 2.3(2)\\ 4.3(5)\\ \hline 2.4(4)\\ \hline 1.0(0.6)\\ \hline 4.8(6)\\ \hline 50\\ \hline 1.6e+0:341\\ \hline 2.3(2)\\ 4.3(15)\\ \hline 2.4(4)\\ \hline 1.0(0.8)\\ \hline 1.6e+0:518\\ \simeq 250\\ \hline 1.0e+0:518\\ \hline 50\\ \hline 1.0e+0:518\\ \hline 50\\ \hline 1.0e+0:518\\ \hline 50\\ \hline 1.0e+0:518\\ \hline 50\\ \hline 1.0e+1:592\\ \hline 5.3(6)\\ \hline 41(8(52)\\ \hline 2.3(2)\\ \hline 0.91(1)\\ \hline 50\\ \hline 1.6(2)\\ \hline \end{array}$ | #succ #succ 15/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 0/15 15/15 |

Expected running time (ERT in number of function evaluations) divided by the respective best ERT measured during BBOB-2009 in dimension 5. The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding best ERT (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries, succeeded by a star, are statistically significantly better (according to the rank-sum test) when compared to all other algorithms of the table, with p = 0.05 or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni correction by the number of instances.

| #FEs/D | 0.5 | 1.2 | 3 | 10 | 50 | #succ | #FEs/D | 0.5 | 1.2 | 3 | 10 | 50 | #succ |
|---------------------|--|--------------------------|----------------------|---------------------|---------------------------------|----------------|---------------------|--------------------------------|---|---|---|------------------------------|----------------|
| f1 MATSuMo | 6.3e+1:24 | 4.0e+1:42 | 1.0e-8:43 | 1.0e-8:43 | 1.0e-8:43 | 15/15 | f13 MATSuMo | 1.6e+3:28 | 1.0e+3:64 | 6.3e+2:79 | 4.0e+1:211 8.0(8) | 2.5e+0:1724 ~ 1000 | 15/15 |
| RANDOM | 892(1140) | 3.7e4(3e4) | ~ | ~ | ∞ 2e7 | 0/15 | RANDOM | 358(119) | 1.5e5(1e5) | ∞ 2.0(2) | ∞ | ∞ 2e7 | 0/15 |
| NEWUOA | 1.7(0) | 1.0(0.0) | 1.0(0.0)*4 | 1.0(6e-3)*4 | 1.0(0.0)*4 | 15/15 | NEWUOA | 1.7(0.3) | 1(0.1) | 1(0.2) | 1(0.1)* ³ | 1.5(2) | 15/15 |
| lmm-CMA | 2.5(2) | 2.5(0.9) | 10(0.1) | 10(0.3) | 10(0.3) | 15/15 | lmm-CMA | 1.6(0.5) | 2.6(0.8) | 3.3(0.9) | 4.2(0.3) | 1.1 (0.2) | 15/15 |
| SMAC IPOPer ACM | 0.80 (0.3)*3 | 0.67(0.2)*** 2.8(0.5) | ∞ 18(0.0) | ∞ 18(0.7) | ∞ 2000 18(0 8) | 0/15 | SMAC IPOPen ACM | 0.81(0.5)** | 0.66(0.1)*3 2.6(0.2) | 0.84(0.1)* 2.5(0.1) | 1.4(0.2) | ∞ 2000 1 2(0 7) | 0/15 |
| #FEs/D | 0.5 | 1.2 | 3 | 10(0.7) | 50 | #succ | #FEs/D | 0.5 | 1.2 | 2.5(0.1) | 2.5(5) | 50 | #succ |
| f2 | 4.0e+6:29 | 2.5e+6:42 | 1.0e+5:65 | 1.0e+4:207 | 1.0e-8:412 | 15/15 | f14 | 2.5e+1:15 | 1.6e+1:42 | 1.0e+1:75 | 1.6e+0:219 | 6.3e-4:1106 | 15/15 |
| MATSuMo | 0.79(0.7) | 1.3(0.7) | 9.3(10) | 71(90) | ∞ 1000 ∞ 2±7 | 0/15 | MATSuMo | 5.7(2) | 3.1(0.8) | 2.9(1) | 9.5(14) | ∞ 1000 ∞ 2±7 | 0/15 |
| NEWLIOA | 1 4(0) | 1(0) | 1(0.4)*4 | 1(0.5)*4 | 303(190) | 15/15 | NEWLIOA | 43(1) | 2.0(0.8) | 15(0.6)* | 1(0 3)*3 | 10(0.2) | 15/15 |
| lmm-CMA | 0.53(0.5) | 0.68(0.8) | 7.2(1) | 3.8(0.9) | 14(2) | 15/15 | lmm-CMA | 3.8(4) | 2.9(2) | 3.0(1) | 2.2(0.5) | 1.9(0.2) | 15/15 |
| SMAC | 0.54(0.5) | 0.70(0.4) | 23(19) | 143(131) | ∞ 2000 | 0/15 | SMAC | 2.0(1) | 3.3(8) | 19(21) | ~ | ∞ 2000 | 0/15 |
| #FEs/D | 0.5 | 1.4(1) | 9.1(3) | 4.3(0.8) | 10(1) 50 | 15/15 #succ | #FEs/D | 0.5 | 4.2(0.6) | 3.0(0.6) | 1.8(0.2) | 1.3(0.1) 50 | 15/15 #succ |
| f3 | 6.3e+2:33 | 4.0e+2:44 | 1.6e+2:109 | 1.0e+2:255 | 2.5e+1:3277 | 15/15 | f15 | 6.3e+2:15 | 4.0e+2:67 | 2.5e+2:292 | 1.6e+2:846 | 1.0e+2:1671 | 15/15 |
| MATSuMo | 1.9(0.3) | 2.5(0.8) | 8.0(5) | 10(16) | ∞ <i>1000</i> | 0/15 | MATSuMo | 3.5(2) | 1.7(0.9) | 1.1(1) | 2.0(2) | 8.8(10) | 1/15 |
| NEWLIOA | 9.1(4) | 1397(1067) 24(27) | ∞ 359(561) | ∞ 7468(9609) | ∞ 2e7 ∞ 1e5 | 0/15 | NEWLIOA | 35(45) | 1316(1904) | 1.6e5(2e5) 14(27) | ∞ 41(65) | ∞ 2e7 1078(772) | 0/15 |
| lmm-CMA | 1.0(0.4) | 2.3(1) | 5.9(2) | 4.8(0.9) | 2.1(1.0) | 14/15 | lmm-CMA | 1.4(2) | 1.3(1) | 0.77(0.2) | 0.72(0.3) | 0.86(0.1) | 15/15 |
| SMAC | 0.49 (0.5)↓2 | 2.1(0.9) | 124(120) | 114(157) | ∞ 2000 | 0/15 | SMAC | 1.1(2) | 2.9(0.9) | 2.8(1) | ∞ | ∞ 2000 | 0/15 |
| IPOPsaACM #FEs/D | 2.2(2) | 3.3(0.7) | 6.4(3) | 5.1(0.8) | 2.6(1) 50 | 5/5 #succ | #FEs/D | 0.5 | 2.1(0.6) | 0.78(0.1) | 0.96(0.6) | 1.1(0.4) 50 | 15/15 #succ |
| f4 | 6.3e+2:22 | 4.0e+2:91 | 2.5e+2:250 | 1.6e+2:332 | 6.3e+1:1927 | 15/15 | f16 | 4.0e+1:26 | 2.5e+1:127 | 1.6e+1:540 | 1.6e+1:540 | 1.0e+1:1384 | 15/15 |
| MATSuMo | 7.6(3) | 5.1(6) | 10(17) | ~ | ∞ <i>1000</i> | 0/15 | MATSuMo | 3.4(4) | 4.9(5) | 3.3(2) | 3.3(3) | 11(11) | 1/15 |
| RANDOM | 254(335) | 3.2e4(4e4) | ∞ 104(65) | ∞ 1704(1523) | $\infty 2e7$ $\infty 2e5$ | 0/15 | NEWUOA | 2.4(2) | 33(35) 6.5(9) | 830(1404) 7.8(13) | 7.8(8) | 6.5e4(/e4) 16(27) | 3/15 |
| lmm-CMA | 1.3(1) | 2.2(0.6) | 2.0(0.8) | 3.0(0.8) | 2.0(2) | 13/15 | lmm-CMA | 4.8(2) | 8.1(2) | 2.7(0.8) | 2.7(1) | 1.2(0.5) | 15/15 |
| SMAC | 6.9(10) | 102(78) | ~ | ~ | ∞ 2000 | 0/15 | SMAC | 2.4 (3) | 1.5(2) | 0.78 (0.2) | 0.78 (0.5) | 0.76 (0.4)* | 14/15 |
| IPOPsaACM #FEs/D | 5.8(2) | 2.3(0.2) | 1.7(0.4) | 4.0(0.8) | 2.7(2) 50 | 5/5 #succ | IPOPsaACM #FEs/D | 4.5(6) | 14(6) | 4.0(1) | 4.0(2) | 1.8(2) 50 | 15/15 #succ |
| f5 | 2.5e+2:19 | 1.6e+2:34 | 1.0e-8:41 | 1.0e-8:41 | 1.0e-8:41 | 15/15 | f17 | 1.6e+1:11 | 1.0e+1:63 | 6.3e+0:305 | 4.0e+0:468 | 1.0e+0:1030 | 15/15 |
| MATSuMo | 1.8(0.9) | 1.3(0.1) | 2.4(0.1) | 2.4(1) | 2.4(0.2) | 15/15 | MATSuMo | 3.3(2) | 2.2(2) | 1.3(0.9) | 32(23) | ∞ <i>1000</i> | 0/15 |
| NEWLIOA | 8.0(9) | 1833(2303) 1 2(7e=3) | ∞ 1.6(0.4) | ∞ 1.6(0.4) | $\infty 2e/$ 1 6(0 4) | 0/15 | NEWLIOA | 16(2) | 120(98) | 4216(7687) | ∞ 3447(4325) | $\infty 2e7$ $\infty 2e6$ | 0/15 |
| lmm-CMA | 1.8(0.5) | 2.1(0.5) | 6.1(1) | 6.1(0.8) | 6.1(0.8) | 15/15 | lmm-CMA | 0.62(2) | 1(0.6) | 0.65(0.3) | 0.79(0.2) | 1.4(0.4) | 14/15 |
| SMAC | 0.46 (0.1) [*] ₁₂ | 0.33 (0.1)*4 | 0.66 (0.1)*3 | 0.66 (0.1)*3 | 0.66 (0.1)* ³ | 15/15 | SMAC | 0.52 (0.1) | 0.92 (2) | 15(15) | 61(62) | ∞ 2000 | 0/15 |
| IPOPsaACM | 2.2(1) | 2.3(0.7) | 5.2(0.6) | 5.2(0.5) | 5.2(2) | 15/15 | IPOPsaACM #FEs/D | 6.2(5) | 2.5(0.9) | 1.0(0.4) | 1.0(0.3) | 0.91(0.2) 50 | 15/15 #succ |
| #FEs/D | 0.5 | 1.2 6 3 at 4:43 | 3 | 10 | 50 | #succ | f18 | 4.0e+1:116 | 2.5e+1:252 | 1.6e+1:430 | 1.0e+1:621 | 4.0e+0:1090 | 15/15 |
| MATSuMo | 2.4(1) | 1.4(0.3) | 1.4(0.8) | 9.5(13) | ∞ 1000 | 0/15 | MATSuMo | 1.0(1) | 2.4(2) | 8.3(9) | ∞ | ∞ <i>1000</i> | 0/15 |
| RANDOM | 263(608) | 3.2e4(9e4) | 1.7e5(4e5) | ~ | ∞ 2e7 | 0/15 | NEWLIOA | 23(70) 20(56) | 1995(613) 47(36) | ∞ 1013(1571) | ∞ 1.2e4(6117) | ∞ 2e7 ∞ 2e6 | 0/15 |
| NEWUOA | 2.4(1) | 1.2(0.3) | 1(0.3) | 1(0.7) 6 8(3) | 1(0.2) 9 0(4) | 15/15 | lmm-CMA | 0.41(0.6) | 0.57(0.3) | 0.77 (0.3) | 0.76(0.3) | 0.85(0.2) | 15/15 |
| SMAC | 1.6(1) 1.6(1) | 1.2(0.9) | 1.6(0.7) | 2.8(4) | ∞ 2000 | 0/15 | SMAC | 0.31(0.2)↓2 | 8.3(4) | 20(25) | 22(41) | ∞ 2000 | 0/15 |
| IPOPsaACM | 3.5(2) | 2.4(0.5) | 2.1(0.6) | 2.3(1.0) | 1.6(0.4) | 15/15 | IPOPsaACM #EE=/D | 1 1.1(0.7) | 0.94(0.5) | 0.99(0.4) | 0.96(0.3) | 0.99(0.3) | 15/15 |
| #FEs/D | 0.5 | 1.2 | 2 5e+2.74 | 10 6 3a+1:310 | 50 1.0e+1:1351 | #succ | f19 | 1.6e-1:2.5e5 | 1.0e-1:3.4e5 | 6.3e-2:3.4e5 | 4.0e-2:3.4e5 | 2.5e-2:3.4e5 | 3/15 |
| MATSuMo | 1.2(1) | 2.2(0.4) | 2.0(2) | 5.6(6) | ∞ 1000 | 0/15 | MATSuMo | ~ | ∞ | ∞ | ~ | ∞ <i>1000</i> | 0/15 |
| RANDOM | 3.2(11) | 76(55) | 1020(588) | 9.2e5(9e5) | ∞ 2e7 | 0/15 | NEWLIOA | ~ | ~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~ | ~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~ | ~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~ | ∞ 2e7 ∞ 2e6 | 0/15 |
| lmm-CMA | 0.49 (0.6) | 1.4(0.3) | 1.7(1) | 1.0(0.3) | ∞ ses 0.48(0,1) | 15/15 | lmm-CMA | ~ | ~ | ~ | ~ | ∞ 8805 | 0/15 |
| SMAC | 0.58(0.5) | 0.61 (0.5) | 0.49 (0.3)* | 0.39 (0.2)* | 0.57(0.3) | 15/15 | SMAC | ~ | ~ | ~ | ~ | ∞ 2000 | 0/15 |
| IPOPsaACM | 1.9(2) | 2.1(2) | 1.8(0.8) | 1.0(0.2) | 1.0(0.5) | 15/15 | #FEs/D | 0.65(0.9) | 1.2 | 0.93(0.7) | 2.2(1) | 3.3(2) 50 | #succ |
| #FES/D | 0.5 4 0e+4:19 | 2 5e+4:35 | 3 4 0e+3:67 | 2 5e+2:231 | 50 1.6e+1:1470 | #succ | f20 | 1.6e+4:38 | 1.0e+4:42 | 2.5e+2:62 | 2.5e+0:250 | 1.6e+0:2536 | 15/15 |
| MATSuMo | 4.5(1) | 2.9(0.7) | 3.3(2) | 4.0(2) | ∞ <i>1000</i> | 0/15 | MATSuMo | 2.2(0.8) | 2.4(1) | 4.6(1) | 4.1(2) | ∞ 1000 | 0/15 |
| RANDOM | 809(908) | 4532(3126) | 4.2e6(3e6) | ~ | ∞ 2e7 | 0/15 | NEWLIOA | 1 1(0) | 100 | 1(0.3) | 1(0 5)*4 | 2.1(3) | 15/15 |
| NEWUOA | 2.2(0) | 1.3(0.4) 2.5(1) | 1(0.4) * 0 3 3(1) | 1(0.6) 2 6(0.6) | 1(0.4) | 15/15 | lmm-CMA | 0.91(0.7) | 1.4(1.0) | 3.9(0.7) | 6.6(5) | 23(24) | 2/15 |
| SMAC | 1.4(2) | 1.5(1) | 2.5(0.6) | 4.1(5) | ∞ 2000 | 0/15 | SMAC | 0.25 (0.2) [★] | 0.46 (0.2)↓4 | 0.90 (0.1) | ~ | ∞ 2000 | 0/15 |
| IPOPsaACM | 5.2(2) | 3.4(0.7) | 2.9(0.4) | 1.5(0.6) | 1.0(0.2) | 15/15 | IPOPsaACM | 2.4(1) | 2.7(1) | 3.2(0.3) | 4.0(2) | 8.8(9) | 15/15 |
| #FEs/D | 0.5 | 6.3e+1:560 | 3 4 0e+1:684 | 2.54+1:756 | 50 1.0e+1:1716 | #succ | #FEs/D | 0.5 | 1.2 | 3 4 0e+1:77 | 10 | 50 4.0e+0:1094 | #succ |
| MATSuMo | 7.9(6) | ~ | ~ | ~ | ∞ 1000 | 0/15 | MATSuMo | 2.7(0.7) | 1.9(1) | 1.9(0.4) | 0.56(0.5) | 0.97 (2) | 9/15 |
| RANDOM | ∞ 1.2/0.5) | ∞ 11/0 2) | ∞ 1/0.4) | ∞ 1.0(0.2) | ∞ 2e7 | 0/15 | RANDOM | 943(230) | 2.0e4(3e4) | 2.0e4(3e4) | ~ | ∞ 2e7 | 0/15 |
| Imm-CMA | 1.6(0.4) | 1.1(0.2) 1.3(0.1) | 1(0.4) | 1.0(0.3) | 1.0(0.2) 2.1(0.5) | 15/15 | NEWUOA | 1.8(0.2)* 2 3 5(1) | 1(0.2)*3 2 5(0.0) | 1(0.2)*3 | 1.4(3) | 2.9(0.8) | 15/15 |
| SMAC | 5.0(3) | 26(13) | ~ | ~ | ∞ 2000 | 0/15 | SMAC | 7.5(6) | 4.2(1) | 4.2(7) | 2.7(6) | 5.2(10) | 4/15 |
| IPOPsaACM #EEc/D | 1.4(0.5) | 1.4(2) | 1.2(2) | 1.2(0.4) | 1.6(0.4) | 15/15 | IPOPsaACM | 4.5(3) | 4.5(0.8) | 4.5(14) | 2.5(2) | 5.3(0.1) | 15/15 |
| f10 | 1.6e+6:15 | 1.0e+6:27 | 4.0e+5:70 | 6.3e+4:231 | 4.0e+3:1015 | 15/15 | #FEs/D | 0.5 | 1.2 4.0e±1:68 | 3 4 0e+1:68 | 10 | 50 6 3a+0:1219 | #succ |
| MATSuMo | 4.4(1) | 3.1(0.9) | 3.4(0.8) | 9.1(13) | $\infty 1000$ | 0/15 | MATSuMo | 2.2(0.5) | 2.1(0.6) | 2.1(2) | 1.5(2) | 0.58(0.6) | 11/15 |
| RANDOM | 28(44) | 77(45) | 894(954) | ∞ *****3 | ∞ 2e7 | 0/15 | RANDOM | 1986(3156) | 9.2e4(2e5) | 9.2e4(1e5) | 1.3e6(2e6) | ∞ 2e7 | 0/15 |
| Imm-CMA | 4.2(1) | 2.6(0.4) 3.5(3) | 4.2(0.7) | 2.3(0.5) | 1(0.5) | 15/15 | NEWUOA | 1.5(0.2)*2 | 1.3(0.5)*2 5.8(11) | 1.3(0.3)*2 | 1(0.9) | 1.4(4) | 15/15 |
| SMAC | 3.7(7) | 5.5(10) | 6.2(3) | 18(9) | ∞ 2000 | 0/15 | IMM-CMA SMAC | 10(13) | 7.3(2) | 5.8(1) 7.3(9) | 5.9(6) 4.2(9) | 2.0(2) | 7/15 |
| IPOPsaACM | 4.9(5) | 5.1(5) | 4.9(3) | 3.0(0.5) | 1.0(0.2) | 15/15 | IPOPsaACM | 3.8(1) | 22(127) | 22(7) | 47(142) | 177(36) | 15/15 |
| #FEs/D | 0.5 4 0e+4:11 | 2.5e+3.27 | 3 1.6e+2:313 | 10 | 50 1.0e+1:1002 | #succ | #FEs/D | 0.5 | 1.2 | 3 | 10 | 50 | #succ |
| MATSuMo | 1.7(3) | 2.5(2) | 21(19) | ~ | ∞ 1000 | 0/15 | MATSuMo | 2.0(2) | 4.0e+0.118 10(10) | 2.5e+0.500 ∞ | 2.5e+0.500 ∞ | 1.0e+0.1014 ∞ 1000 | 0/15 |
| RANDOM | 2.0(3) | 3.2(3) | 34(37) | 929(744) | ∞ 2e7 | 0/15 | RANDOM | 2.3(2) | 7.0(5) | 92(123) | 92(68) | 5.5e4(6e4) | 3/15 |
| INEWUOA | 2.0(2) 1.3(0.7) | 1.4(0.7) | 4.5(3) | 13(5) 3.7(0.4) | 2.1 (1.0) | 15/15 | NEWUOA | 7.3(35) | 2.8(0.3) 8 2(9) | 2.1(4) 408(375) | 2.1(3) 408(354) | 3.5(3) 2.8823 | 15/15 |
| SMAC | 0.59 (0.2) | 0.68 (0.5) | 2.5 (1) | 7.3(8) | ∞ 2000 | 0/15 | SMAC | 1.6(2) | 5.0(8) | 46(69) | 46(31) | ∞ 2000 | 0/15 |
| IPOPsaACM | 1.7(0.9) | 3.4(6) | 7.5(0.9) | 4.9(0.6) | 2.5(0.2) | 15/15 | IPOPsaACM | 5.1(6) | 13(12) | 71(105) | 71(54) | 2.9e4(3e4) | 5/15 |
| #FES/D f12 | 0.5 1.0e+8:23 | 6.3e+7:39 | 2.5e+7:76 | 4.0e+6:209 | 1.0e+1:1042 | #succ 15/15 | #FEs/D | 0.5 | 1.2 | 3 | 10 6 3e±1.0885 | 50 4 0e+1:31620 | #succ |
| MATSuMo | 3.1(1) | 2.9(0.8) | 3.0(0.8) | 3.6(0.5) | ∞ <i>1000</i> | 0/15 | MATSuMo | 15(18) | 1.0e∓2.718 ∞ | × × × × × × × × × × × × × × × × × × × | ∞ ∞ | ∞ 1000 | 0/15 |
| RANDOM | 294(299) | 2589(3038) | 8.3e5(1e6) | ∞ 1.2(0.4) | ∞ 2e7 3 0(3) | 0/15 | RANDOM | 1.7e5(1e5) | ~ | ~ | ~ | ∞ 2e7 | 0/15 |
| lmm-CMA | 2.0(0.9) | 2.3(0.0) 2.4(0.9) | 2.6(0.6) | 1.9(0.3) | 1.1(0.1) | 15/15 | NEWUOA | 0.74(0.2) | 1.2(0.9) 1.1(0.9) | 4.3(4) 1.4(0.7) | 247(148) 1.2(1) | ∞ 2e5 1.2(2) | 3/15 |
| SMAC | 2.8(3) | 38(16) | ~ | ~ | ∞ 2000 | 0/15 | SMAC | 0.65 (1) | 10(12) | ~ | ~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~~ | ∞ 2000 | 0/15 |
| IPOPsaACM | 4.6(2) | 3.7(0.9) | 2.7(0.2) | 1.4(0.1) | 0.67(0.1) | 15/15 | IPOPsaACM | 1.2(0.5) | 1.4(1) | 4.9(9) | 8.7(9) | 2.9(5) | 15/15 |
| | | | | | | | | | | | | | |

Expected running time (ERT in number of function evaluations) divided by the respective best ERT measured during BBOB-2009 in dimension 20. The ERT and in braces, as dispersion measure, the half difference between 90 and 10%-tile of bootstrapped run lengths appear for each algorithm and run-length based target, the corresponding best ERT (preceded by the target Δf -value in *italics*) in the first row. #succ is the number of trials that reached the target value of the last column. The median number of conducted function evaluations is additionally given in *italics*, if the target in the last column was never reached. Entries, succeeded by a star, are statistically significantly better (according to the rank-sum test) when compared to all other algorithms of the table, with p = 0.05 or $p = 10^{-k}$ when the number k following the star is larger than 1, with Bonferroni

CORRECTION BY THE NUMBER OF INSTANCES.

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